ATSC 2012023
Total mark out of 44
Ch2: A5g, A13e, A15e.
Ch10: A1e, A4e, A5e, A6a, A8e, A9e.

## Chapter 2

A5g)
(10.5 marks)

Plot the local solar elevation angle vs. local time for 22 December, 23 March, and 22 June for the following city: g) Montreal, Canada

Given: The location Montreal, Canada
d (22-Dec) $=\quad 356$
$d(23-M a r)=\quad 82$
d (22-Jun $)=173$

Find: $\quad \Psi(\mathrm{deg})=\quad$ ?

Use eq. 2.5: $\delta s=\Phi r^{*} \cos \left(C^{*}(d-d r) / d y\right)$
where: $\quad \Phi r=\quad 0.40910518 \mathrm{rad}$
$\mathrm{C}=\quad 6.28318531 \mathrm{rad}$
$\mathrm{dr}=\quad 172$ for 2023
$d y=\quad 365$

|  | 22-Dec | 23-Mar | 22-Jun |
| :--- | ---: | ---: | ---: |
| $\boldsymbol{\delta s}$ (rads) | -0.4089688 | 0.00880235 | 0.40904456 |
| $\boldsymbol{\delta} \boldsymbol{s}$ (deg) | -23.4321862 | 0.50433732 | 23.4365271 |

Use eq. 2.6: $\quad \sin (\Psi)=\sin (\phi) * \sin (\delta s)-\cos (\phi)^{*} \cos (\delta \mathrm{~s}) * \cos \left(\left(C^{*} \mathrm{tUTC} / \mathrm{td}\right)+\lambda e\right)$
where: $\quad \phi=\quad 45.5019 \mathrm{degN}=\quad 0.794157971 \mathrm{rad}$
$\lambda e=\quad-73.5674 \mathrm{deg}=\quad-1.28399335 \mathrm{rad}$
$t d=\quad 24.0 \mathrm{~h}$
time zone of Montreal:
tUTC $=\mathrm{t}+4$ hours
(for Mar23 and Jun22)
tUTC $=\mathrm{t}+5$ hours
EST
(for Dec22)

t(h) | $\boldsymbol{\Psi}$ (deg) |  |  |  |
| ---: | ---: | ---: | ---: |
|  | 0 | 22-Dec | 23-Mar | 22-Jun

Check: Units ok. Physics ok.
Discussion: Montreal's winters are a similar to Vancouver's


A13e)
(2.5 marks)
(W/m^2): e) 600.

Given: $\quad$ FH $=\quad 600 \mathrm{~W} / \mathrm{m}^{\wedge} 2$

Find: $\quad \mathrm{FH}=\quad$ ? $\quad \mathrm{K}^{*} \mathrm{~m} / \mathrm{s}$

Use eq. 2.11: $\mathrm{FH}=\mathrm{FH} / \mathrm{rho}^{*} \mathrm{Cp}$
where rho * $\mathrm{Cp}=\quad 1231\left(\mathrm{~W} / \mathrm{m}^{\wedge} 2\right) /\left(\mathrm{K}^{*} \mathrm{~m} / \mathrm{s}\right)$
$\mathrm{FH}=\quad 0.487408611 \mathrm{~K} * \mathrm{~m} / \mathrm{s}$

Check: Units ok. Physics ok.
Discussion: This amount of heat flux is just slightly higher than the advective heat flux of a $1 \mathrm{~m} / \mathrm{s}$ wind blowing air with a temperature excess of about 0.5 C

A15e)
Plot Planck curves for the following blackbody temperatures (K): e) 2500.
(5 marks)
Given: $\quad \mathrm{T}=\quad 2500 \mathrm{~K}$

Find: Planck curve of blackbody object with temp T.

Use eq. 2.13: $\mathrm{E} \lambda^{*}=\mathrm{c} 1 /\left(\lambda^{\wedge} 5^{*}\left(\mathrm{e}^{\wedge}\left(\mathrm{c} 2 / \lambda^{*} \mathrm{~T}\right)-1\right)\right)$

| where $\mathrm{c} 1=$ | $3.74 \mathrm{E}+08 \mathrm{~W}^{*} \mu \mathrm{~m}^{\wedge} 4 / \mathrm{m}^{\wedge} 2$ |
| :--- | :--- |
| $\mathrm{c} 2=$ | $1.44 \mathrm{E}+04 \mu \mathrm{~m}^{*} \mathrm{~K}$ |


| $\lambda(\mu \mathrm{m}) \quad \mathrm{E} \lambda^{*}$ |  |
| :--- | :--- | :--- |
| 0 | 0 |

$0.2 \quad 3.63 \mathrm{E}-01$
$0.3 \quad$ 7.06E +02
$0.4 \quad 2.04 \mathrm{E}+04$
0.5 1.19E+05
$0.6 \quad 3.26 \mathrm{E}+05$
0.7 5.94E+05
$0.8 \quad 8.53 \mathrm{E}+05$
$0.9 \quad 1.05 \mathrm{E}+06$
$1 \quad 1.18 \mathrm{E}+06$
1.1 1.24E+06
$1.2 \quad 1.25 \mathrm{E}+06$
1.3 1.21E+06
$1.4 \quad 1.15 \mathrm{E}+06$
$1.5 \quad 1.08 \mathrm{E}+06$
$1.6 \quad 1.00 \mathrm{E}+06$
1.7 9.21E+05
$1.8 \quad 8.41 \mathrm{E}+05$
1.9 7.66E+05
$2 \quad 6.95 \mathrm{E}+05$
2.1 6.30E+05
$2.2 \quad 5.71 \mathrm{E}+05$
$2.3 \quad 5.17 \mathrm{E}+05$
$2.4 \quad 4.69 E+05$
2.5 4.25E+05
2.6 3.86E+05
2.7 3.50E+05


Check: Units ok. Physics ok.
Discussion: The temperature of this object (2500K) is about the temperature of an incandescent light bulb The peak wavelength is higher energy than visible light.

## Chapter 10

A1e)
(3 marks)
Plot the wind symbol for winds with the following directions and speeds:
e) $S$ at 48kt.

Given: $\quad M=\quad 48 \mathrm{kt}$
direction $=S$

Find: Applicable wind symbol.

From Table 10-1:
Pennant 50 speed units

48 knots its closer to 50 than 45 , so draw the symbol for 50.
$48 \mathrm{kt}=$ shaft with one pennant

Check: direction and symbol ok.
Discussion: If only the pressure
gradient force was acting here, high pressure would be to the S and low pressure would be to the N

A4e)
(4 marks)

Find the advective "force" per unit mass given the following wind
components (m/s) and horizontal distances (km): e) $V=3, \Delta U=10, \Delta y=10$.

Given:

| $V=$ | $3 \mathrm{~m} / \mathrm{s}$ |
| :--- | ---: |
| $\Delta U=$ | $10 \mathrm{~m} / \mathrm{s}$ |
| $\Delta y=$ | 10 km |

Find:

| $\mathrm{FxAD} / \mathrm{m}=$ | $?$ | $\mathrm{~m} / \mathrm{s}^{\wedge} 2$ |
| :--- | :--- | :--- |
| $\mathrm{FyAD} / \mathrm{m}=$ | $?$ | $\mathrm{~m} / \mathrm{s}^{\wedge} 2$ |

Use eq. 10.8a:

$$
\mathrm{FxAD} / \mathrm{m}=-\mathrm{U}^{*}(\Delta \mathrm{U} / \Delta \mathrm{x})-\mathrm{V}^{*}(\Delta \mathrm{U} / \Delta \mathrm{y})-\mathrm{W}^{*}(\Delta \mathrm{U} / \Delta \mathrm{z})
$$

Use eq. 10.8b:

$$
\mathrm{FyAD} / \mathrm{m}=-\mathrm{U}^{*}(\Delta \mathrm{~V} / \Delta \mathrm{x})-\mathrm{V}^{*}(\Delta \mathrm{~V} / \Delta \mathrm{y})-\mathrm{W}^{*}(\Delta \mathrm{~V} / \Delta \mathrm{z})
$$

Convert $\Delta x(k m)$ to $\Delta x(m)$ :

$$
\Delta y=\quad 10000 \mathrm{~m}
$$

Since $\Delta V$ is not given, we can assume $\Delta V=0$. Therefore, $F y A D / m=0$.

Since U and W were not given, we can assume that $\mathrm{V}=0$ and $\mathrm{W}=0$.
Hence:

$$
\mathrm{FxAD} / \mathrm{m}=-\mathrm{V}^{*}(\Delta \mathrm{U} / \Delta \mathrm{y})
$$

| FyAD $/ \mathrm{m}=$ | $0 \mathrm{~m} / \mathrm{s}^{\wedge 2}$ |
| :--- | :---: |
| FXAD $/ \mathrm{m}=$ | $-0.003 \mathrm{~m} / \mathrm{s}^{\wedge} 2$ |

Check: Units ok. Physics ok.
Discussion: The advective force is negative, therefore advection is accelerating the wind to the West.
(slowly)

A5e)
(4 marks)

Town A is 500 km west of town $B$. The pressure at town $A$ is given below, and the pressure at town $B$ is 100.1 kPa . Calculate the pressure-gradient force/mass in between these two towns: e) 99.4 kPa .

| $\Delta \mathrm{x}=$ | 500 km |
| :--- | ---: |
| P @ $=$ | 99.4 kPa |
| P @ $=$ | 100.1 kPa |

Find:

| $\mathrm{FxPG} / \mathrm{m}=$ | $?$ | $\mathrm{~m} / \mathrm{s}^{\wedge} 2$ |
| :--- | :--- | :--- |
| $\mathrm{FyPG} / \mathrm{m}=$ | $?$ | $\mathrm{~m} / \mathrm{s}^{\wedge} 2$ |

Use eq. 10.9a: FxPG/m =-(1/p)*( $\Delta \mathrm{P} / \Delta x)$
where $\rho=$
$1.2 \mathrm{~kg} / \mathrm{m}^{\wedge} 3$

Convert $\Delta x(k m)$ to $\Delta x(m)$ :

$$
\Delta x=\quad 500000 \mathrm{~m}
$$

Convert P@A(kPa) to P@A(Pa) and P@B(kPa) to P@B(Pa):

| $\mathrm{P} @ \mathrm{~A}=$ | 99400 Pa |
| :--- | ---: |
| $\mathrm{P} @ \mathrm{~B}=$ | 100100 Pa |
| $\Delta \mathrm{P}=$ | 700 Pa |

Since town $A$ is 500 km to the west of town $B$, there is no pressure change in the North - South direction.

```
FxPG/m = -0.00116667 m/s^2
```

Check: Units ok. Physics ok.
Discussion: The PGF is negative because air flows east to west from town $B$ to town $A$.
The force is very small because the pressure difference is very small.

Suppose that $\mathrm{U}=8 \mathrm{~m} / \mathrm{s}$ and $\mathrm{V}=-\mathbf{3} \mathrm{m} / \mathrm{s}$, and latitude $=45 \mathrm{deg}$. Calculate

Given:

| $\mathrm{U}=$ | $8 \mathrm{~m} / \mathrm{s}$ |
| :--- | ---: |
| $\mathrm{V}=$ | $-3 \mathrm{~m} / \mathrm{s}$ |
| lat $=$ | 45 degS |
| $\mathrm{R}=$ | 500 km |

Find: $\quad \mathrm{FxCN} / \mathrm{m}=\quad$ ? $\quad \mathrm{m} / \mathrm{s}^{\wedge} 2$
$\mathrm{FyCN} / \mathrm{m}=$ ? $\mathrm{m} / \mathrm{s}^{\wedge} 2$

Use eq. 10.13a: $\mathrm{FxCN} / \mathrm{m}=+\mathrm{s} *(\mathrm{~V} * \mathrm{M}) / \mathrm{R}$
Use eq. 10.13b: $\mathrm{FyCN} / \mathrm{m}=-\mathrm{s}^{*}(\mathrm{U} * \mathrm{M}) / \mathrm{R}$
where $M=\left(U^{\wedge} 2+V^{\wedge} 2\right)^{\wedge} 1 / 2$

North Hemisphere, low pressure:
The force is $90^{\circ}$ to the wind's right in the N.H so the coriolis force will be towards the east

Convert R(km

$$
R=\quad 500000 \mathrm{~m}
$$

$$
\mathrm{M}=\quad 8.54400375 \mathrm{~m} / \mathrm{s}
$$

| FxCN $/ \mathrm{m}=$ | $-5.1264 \mathrm{E}-05 \mathrm{~m} / \mathrm{s}^{\wedge 2}$ |
| :--- | :--- |
| FyCN $/ \mathrm{m}=$ | $-0.0001367 \mathrm{~m} / \mathrm{s}^{\wedge} 2$ |

Check: Units ok. Physics ok.
Discussion: These components correspond
to a force pointing SSW.

A8e)
(4 marks)
What is the magnitude and direction of Coriolis force/mass in Los Angeles,
USA, given: e) $U(m / s)=0, V(m / s)=-5$.

Given:
$\mathrm{U}=$
$\mathrm{V}=$
lat $=$
$0 \mathrm{~m} / \mathrm{s}$
34.0522 degN of Los Angeles, USA

Find: $\quad|\mathrm{FCF} / \mathrm{m}|=\quad$ ? $\quad \mathrm{m} / \mathrm{s}^{\wedge} 2$
Direction of FCF/m.
Use eq. 10.18a: $|F C F / m|=2^{*} \Omega^{*}\left|\sin (\phi)^{*} M\right|$
or
use eq. 10.18b: $|\mathrm{FCF} / \mathrm{m}|=|\mathrm{fc} * \mathrm{M}|$
and eq. 10.16: $\mathrm{fc}=2^{*} \Omega^{*} \sin (\phi)$
where $M=\left(U^{\wedge} 2+V^{\wedge} 2\right)^{\wedge} 1 / 2$

$$
M=\quad 5 \mathrm{~m} / \mathrm{s}
$$

and

$$
\Omega=\quad 7.29 \mathrm{E}-05 \mathrm{~s}^{\wedge}-1
$$

$\mid$ FCF $/ \mathrm{m} \mid=\quad 4.08 \mathrm{E}-04 \mathrm{~m} / \mathrm{s}^{\wedge 2}$

Direction is towards the West
or 270deg

Check: The wind is blowing towards north and the drag force is directly
Discussion:
opposite the wind so is therefore towards the south.

A9e)
(5.5 marks)

Same wind components as exercise A8, but find the magnitude and direction of turbulent drag force/mass in a statically neutral atmospheric boundary layer over an extensive forested region.

| Given: | $U=$ | $0 \mathrm{~m} / \mathrm{s}$ |
| :--- | :--- | ---: |
|  | $\mathrm{V}=$ | $-5 \mathrm{~m} / \mathrm{s}$ |
|  | lat $=$ | 34.0522 degN |
| Find: | $\mid$ FTD $/ \mathrm{m} \mid=$ | $?$ |

## Direction of FTD/m.

Use eq. 10.20: |FTD/m| = wt *(M/zi)
where $\mathrm{M}=\left(\mathrm{U}^{\wedge} 2+\mathrm{V}^{\wedge} 2\right)^{\wedge} 1 / 2$
and $w t=C D * M$ for statically neutral conditions

Hence:

$$
\begin{array}{lc}
\mathrm{CD}= & 0.02 \text { over forests. } \\
\mathrm{zi}= & 1 \mathrm{~km} \\
& \text { (other zi values allowed) }
\end{array}
$$

Convert zi(km) to zi(m):

$$
z i=\quad 1000 \mathrm{~m}
$$

(values of CD and zi given in Sample Application pg. 300; or could be estimated given the latitude of LA)

$$
\begin{array}{lr}
\mathrm{M}= & 5 \mathrm{~m} / \mathrm{s} \\
\mathrm{wt}= & 0.10 \mathrm{~m} / \mathrm{s}
\end{array}
$$

|FTD/m| = $0.0005 \mathrm{~m} / \mathrm{s}^{\wedge} 2$

Direction: towards North

Check: Units ok. Physics ok.
Discussion:

