

ATSC 201 Fall 2025

Homework 1 Answer Key

Total mark out of 25

Chapter 1: A1g, A3g, A5g, A6g, A9g, A14g, A15g

Chapter 1

A1g)

(4 marks)

Find the wind direction (degrees) and speed (m/s), given the (U,V) components: g) (-2,-10) mi/h

Given:            U =                                -2 mi/h  
                     V =                                -10 mi/h

Find:            alpha (wind direction)            M (wind speed)

Using eq. 1.1:

$$M = (U^2 + V^2)^{0.5}$$

Using eq. 1.2a:

$$\alpha = 90\text{deg} - (360\text{deg}/C) * \arctan(V/U) + \alpha_0$$

$$C = 360 \text{ deg}$$

if  $U < 0$              $\alpha_0 = 0 \text{ deg}$

$$M = 10.198039 \text{ mi/h}$$

$$= 4.55893137 \text{ m/s}$$

M =                                4.56 m/s  
alpha =                            11.31 deg

Checks:            Units ok. Physics ok.

Discussion:       The wind is coming from the NNE with a magnitude of 4.56 m/s.

A3g)

(3 marks)

Convert the following UTC time to local time in your own time zone: g) 18:00

Given:                                18:00 UTC

Find:                                local time

Using eqs. from Table 1-1

$$DT = UTC - \beta$$

$$ST = UTC - \alpha$$

Vancouver's time zone is "U" (Pacific)

$$\beta = 7:00 \text{ PDT}$$

$$\alpha = 8:00 \text{ PST}$$

Currently, local time is PDT.

$$DT = 11:00 \text{ PDT}$$

$$\text{for partial marks: } ST = 10:00 \text{ PST}$$

**Checks:** Units ok.

**Discussion:** Vancouver is currently in Pacific Daylight Time, so it is presently 7 hours behind UTC time.

**A5g)**  
(2.5 marks)

**Find the pressure in kPa at the following heights above sea level, assuming an average  $T = 250\text{K}$ : g) 2 km**

$$\text{Given: } z \text{ (m)} = 2 \text{ km} \quad " = " \quad 2000$$

$$\text{avg } T = 250 \text{ K}$$

$$\text{Find: } P \quad ? \quad \text{kPa}$$

Using eq. 1.9a:

$$P = P_0 * e^{-(a/T)*z}$$

$$\text{where: } P_0 = 101.3250 \text{ kPa}$$

$$a = 0.0342 \text{ K/m}$$

$$P = 77.1 \text{ kPa}$$

**Checks:** Units ok. Physics ok.

**Discussion:**

At 2 km above sea level, pressure is about 76% of what it is at sea level. There are fewer air molecules above 2 km above sea level, than at sea level.

A6g)  
(3 marks)

Use the definition of pressure as a force per unit area, and consider a column of air that is above a horizontal area of 1 square meter. What is the mass of air in that column: g) Between pressure levels 100 and 50 kPa

Given:  $P_{\text{bottom}} = 100 \text{ kPa}$   
 $P_{\text{top}} = 50 \text{ kPa}$   
 $A = 1 \text{ m}^2$

Find:  $\Delta m = ? \text{ kg}$   
mass of air between  $P_{\text{bottom}}$  and  $P_{\text{top}}$

Using eq. 1.11:

$$\Delta m = (A/g) * (P_{\text{bottom}} - P_{\text{top}}) \quad \text{where } g = 9.81 \text{ m/s}^2$$

Convert  $P_{\text{bottom}}(\text{kPa})$  and  $P_{\text{top}}(\text{kPa})$  to  $P_{\text{bottom}}(\text{Pa})$  and  $P_{\text{top}}(\text{Pa})$ :

$P_{\text{bottom}} = 100000 \text{ Pa}$   
 $P_{\text{top}} = 50000 \text{ Pa}$

$\Delta m = 5096.84 \text{ kg}$

**Checks:** Units ok. Physics ok.

**Discussion:** This is a calculation of the air mass between 100 and 50 kPa pressure that exists over 1 square meter of area.

A9g)  
(2.5 marks)

Convert the following temperatures: g)  $2000^\circ\text{C} = ?\text{K}$

Given:  $T_c = 2000 \text{ }^\circ\text{C}$

Find:  $T_K = ? \text{ K}$

Using equation 1.7b:

$$T_K = T^{\circ}\text{C} + 273.15$$

<b>T<sub>F</sub> =</b>	<b>2273.15 K</b>
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**Checks:**      Units ok.

**Discussion:** 2273.15K is hot enough to instantly melt pure iron

**A14g)**

(4.5 marks)

**What is the geopotential height and geopotential, given the geometric height? g) 5 km**

Given:  $z = 5 \text{ km} = 5000$

Find:  $H = ?$  m  
 $\Phi = ?$  m<sup>2</sup>/s<sup>2</sup>

Using eq. 1.14a or b:

$$H = R_o * z(R_o + z)$$

where the radius of the Earth,  $R_o = 6356.766\text{km} = 6,356,766\text{m}$ .

Ro = 6356766 m

And using eq. 1.15:

$$\Phi = g^* H \quad \text{where } g = 9.81 \text{ m/s}^2$$

H =	4996.07 m
Φ =	49011.45 m <sup>2</sup> /s <sup>2</sup>

**Checks:** Units ok. Physics ok.

**Discussion:** The difference between the geometric height and the geopotential height is relatively small at 5 km.

A15g)  
(5.5 marks)

What is the standard atmospheric temperature, pressure, and density at the following geopotential height: g) 40 km ?

Given:        H =                                40 km

Find:        T =                ?                degC  
              P =                ?                kPa  
               $\rho$  =                ?                kg/m<sup>3</sup>

Using eqs. 1.16 for  $32\text{km} \leq H \leq 47\text{km}$ :

$$T = 228.65 + 2.8 \cdot (H - 32)$$

**T =                                251.05 K  
                                     -22.10 degC**

Using eq. 1.17 for  $32\text{km} \leq H \leq 47\text{km}$ :

$$P = 0.868 \cdot (228.65/T)^{[12.2011]}$$

**P =                                0.28 kPa**

Using and rearranging eq. 1.18:

$$\rho = P / R_d \cdot T$$

where  $R_d = 0.287053 \text{ kPa} \cdot \text{m}^3 / \text{K} \cdot \text{kg}$   
gas constant for dry air

**$\rho$  =                                0.00385094 kg/m<sup>3</sup>**

**Checks:**        Units ok. Physics ok.

**Discussion:**

At 40 km, the pressure and density of  
the air is much less than at the surface