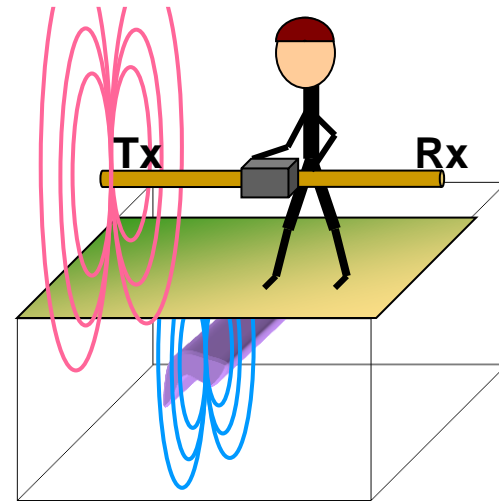
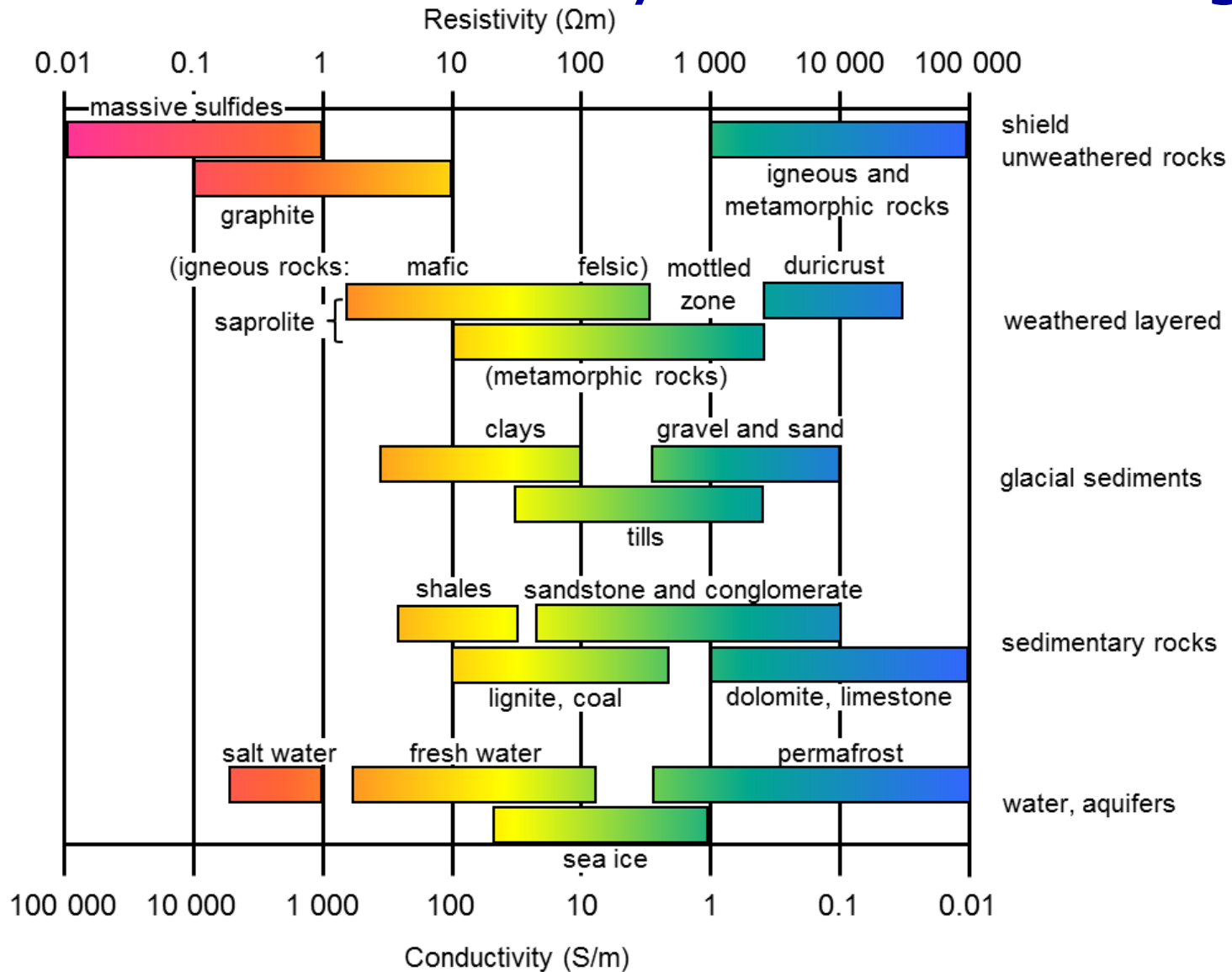


Applied Geophysics – Electromagnetics

- EM induction methods
- Amperes Law
- Faradays Law
- Basics of EM induction
- Use EM31 as a specific learning example

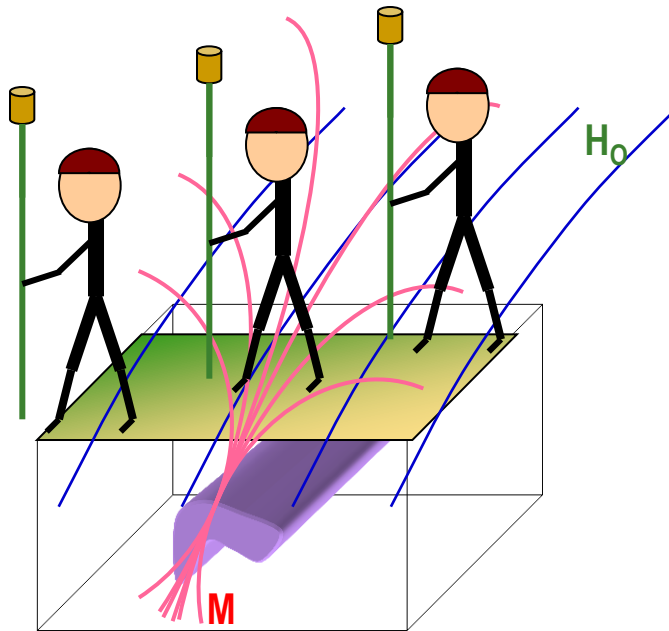


Electrical conductivity: units and range



Previous work: Magnetic induction

- Instrument is a sensor only
- Source is Earth's field – always present.
- Relatively uniform at survey scales
- Source field does not change with time.

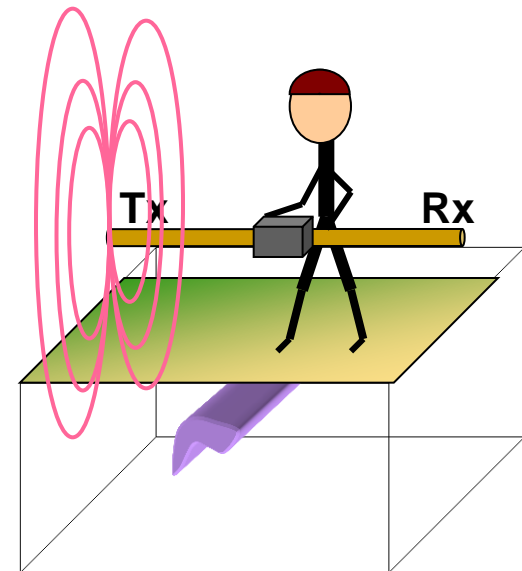


Electromagnetic induction

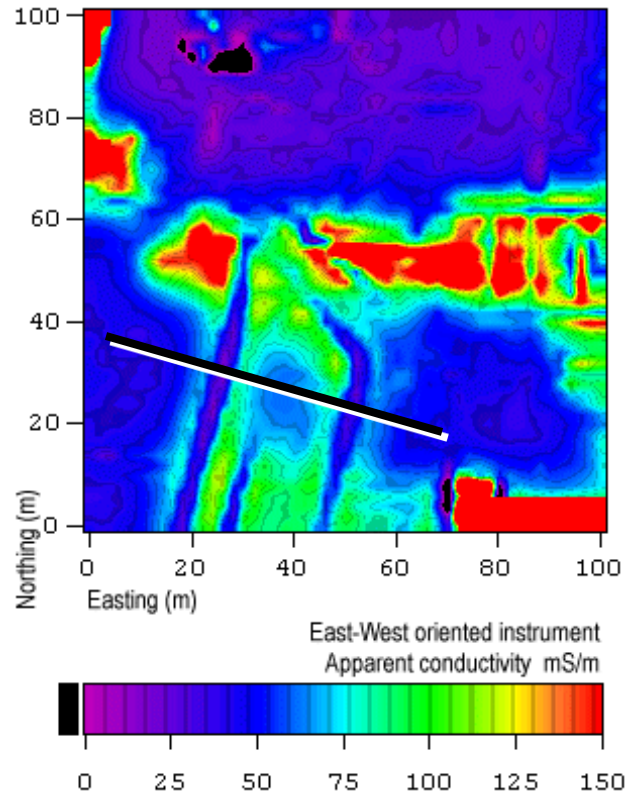
- Survey involves a transmitter and receiver
- Source field changes – it is NOT a static field

- Frequency $\sim 10^1 - 10^4$ Hz

(GPR is $\sim 10^6 - 10^9$ Hz)



EM 31 Data from Expo Site



Electromagnetics

- **Faraday's Law:** A time varying magnetic field generates an electric field

$$\nabla \times \mathbf{E} = -dB / dt$$

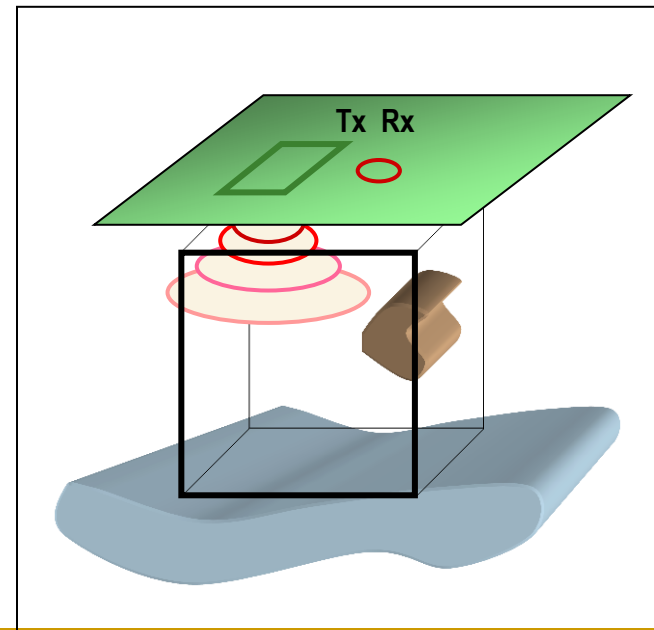
E: electric field

B: magnetic field

Think about electric field as voltage in a circuit.

Units of E are Volts/meter

Electromagnetic induction



Electromagnetics

- **Ohm's Law:**

$$\mathbf{J} = \sigma \mathbf{E}$$

J : current density (Amp/m²)

σ : electrical conductivity

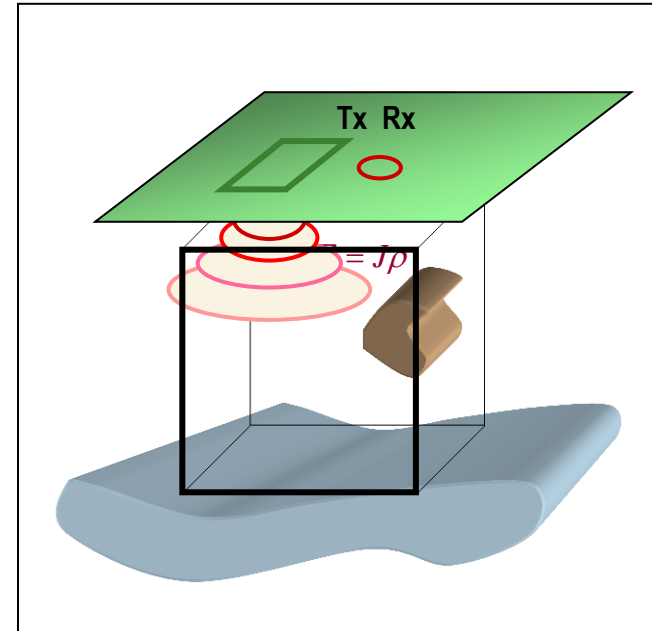
Think about $V = IR$ for a circuit

V: voltage (Volts)

I: current (Amperes).

R: Resistance (Ohms)

Electromagnetic induction



$$\mathbf{E} = \mathbf{J} \rho$$

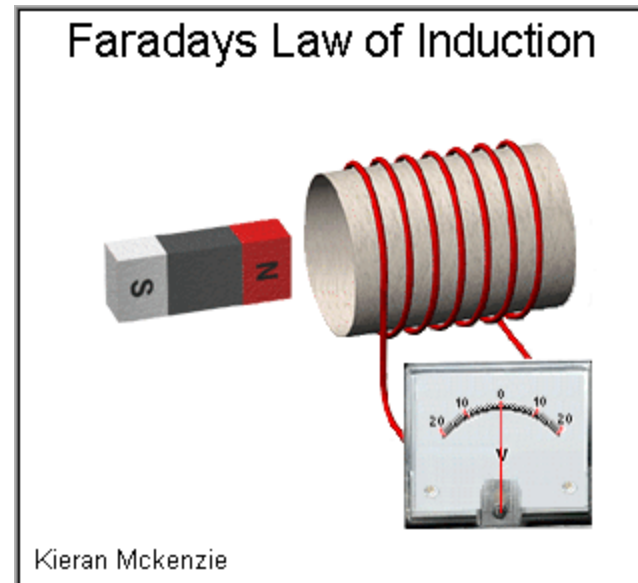
$$\rho = 1/\sigma$$



EM induction

- Faraday's law

- Time varying magnetic fields cause electric fields
- Electric fields produce currents in a conductor
- Hence current flows in conductors that are near an oscillating magnetic field



Electromagnetics

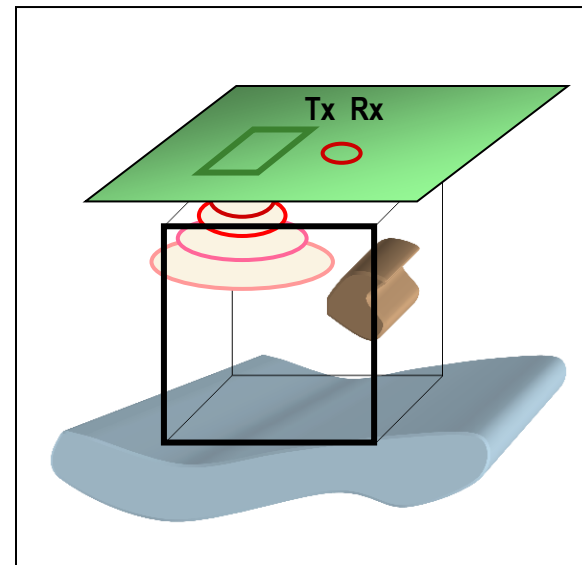
- **Amperes Law:**
A current generates a magnetic field

$$\nabla \times \mathbf{H} = \mathbf{J}$$

H: magnetic field

J: current source density

Electromagnetic induction



EM induction

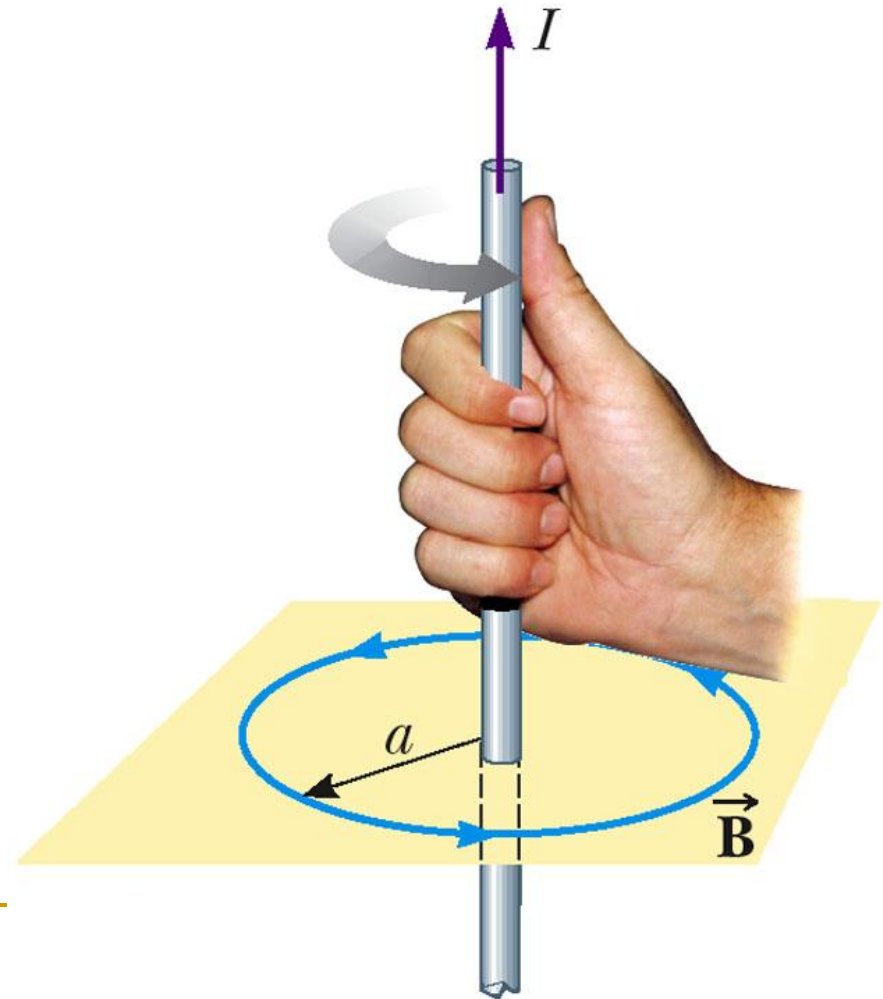
- Ampere's law -
 - Currents generate magnetic fields
 - Oscillating current will cause an oscillating magnetic field



Current in wire causes a magnetic field to surround it (iron filings).

Direction of the Field of a Long Straight Wire

- Right Hand Rule
 - Grasp the wire in your right hand
 - Point your thumb in the direction of the current
 - Your fingers will curl in the direction of the field



EM induction

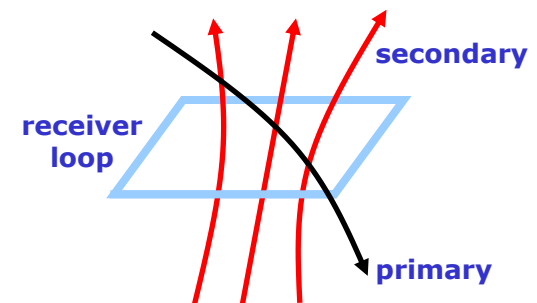
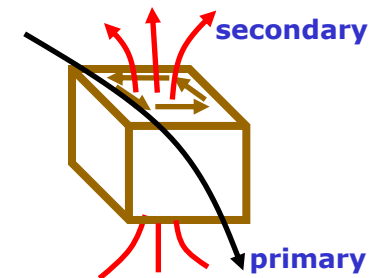
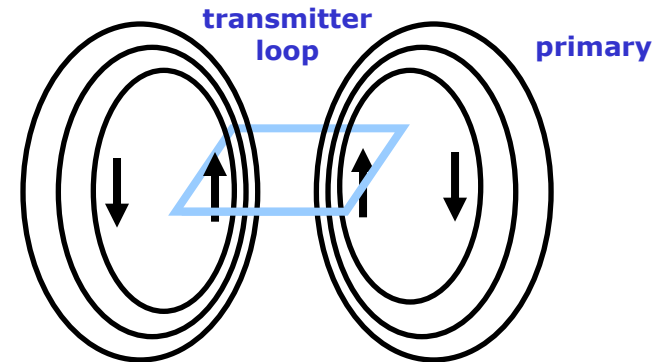
- Lens' law -
 - The direction of the induced currents will be in such a direction as to oppose any change in magnetic flux.



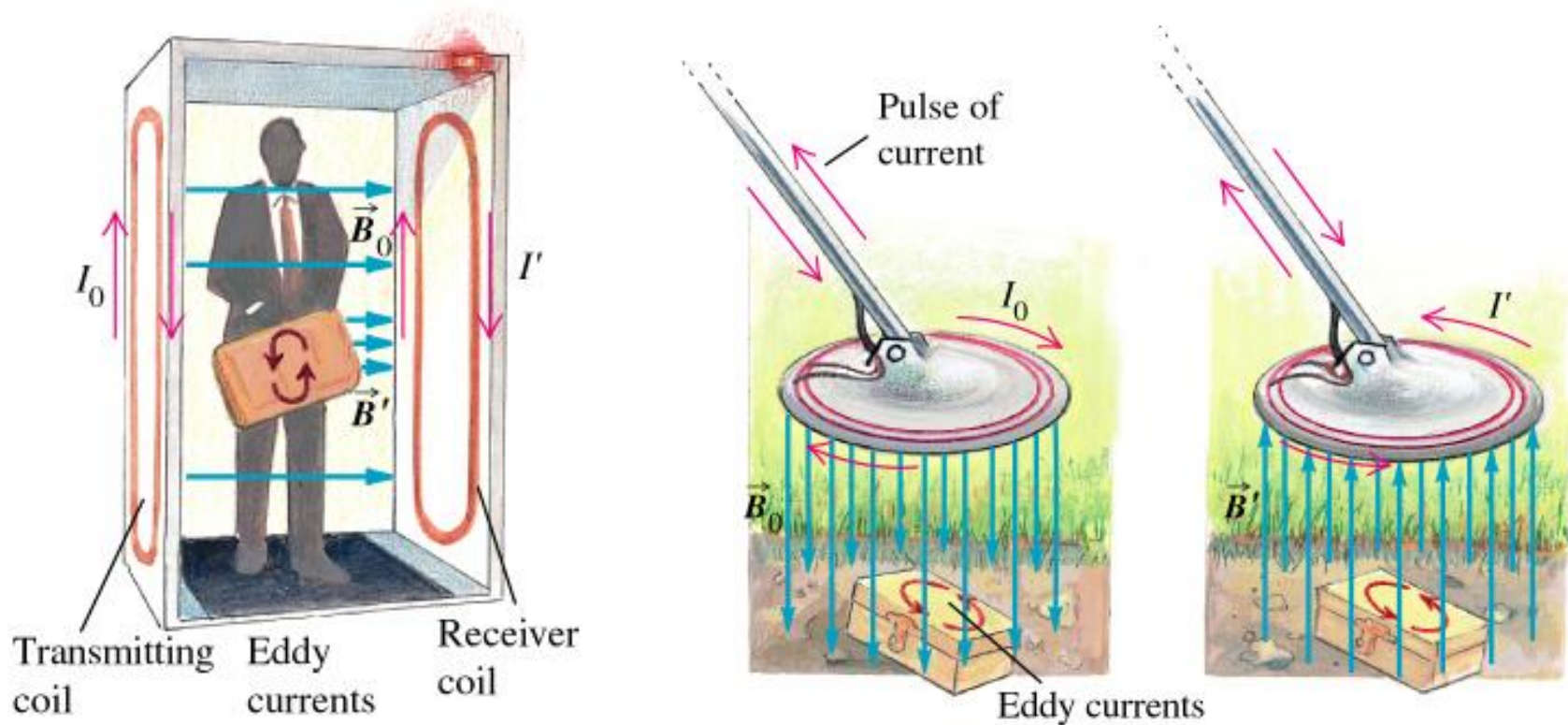
Current in wire causes a magnetic field to surround it (iron filings).

Basic principles of EM induction

- Time-varying transmitter current generates a time-varying magnetic field
- Time-varying magnetic field generates an EMF (i.e. electric field) in the earth
- Currents are generated ($\mathbf{J} = \sigma \mathbf{E}$)
- Currents in the conductor generate magnetic fields (secondary)
- Measure the secondary fields and the primary fields of the transmitter



EM induction example: small scale



- Transmit alternating **primary** magnetic field
 - Induces eddy currents in conducting object
- Eddy currents produce **secondary** magnetic field
 - Induces current in receiver coil

Important elements

- Primary field must couple with the target
- Strength of the induced currents must be big enough to generate signal
- Need to choose which fields to measure

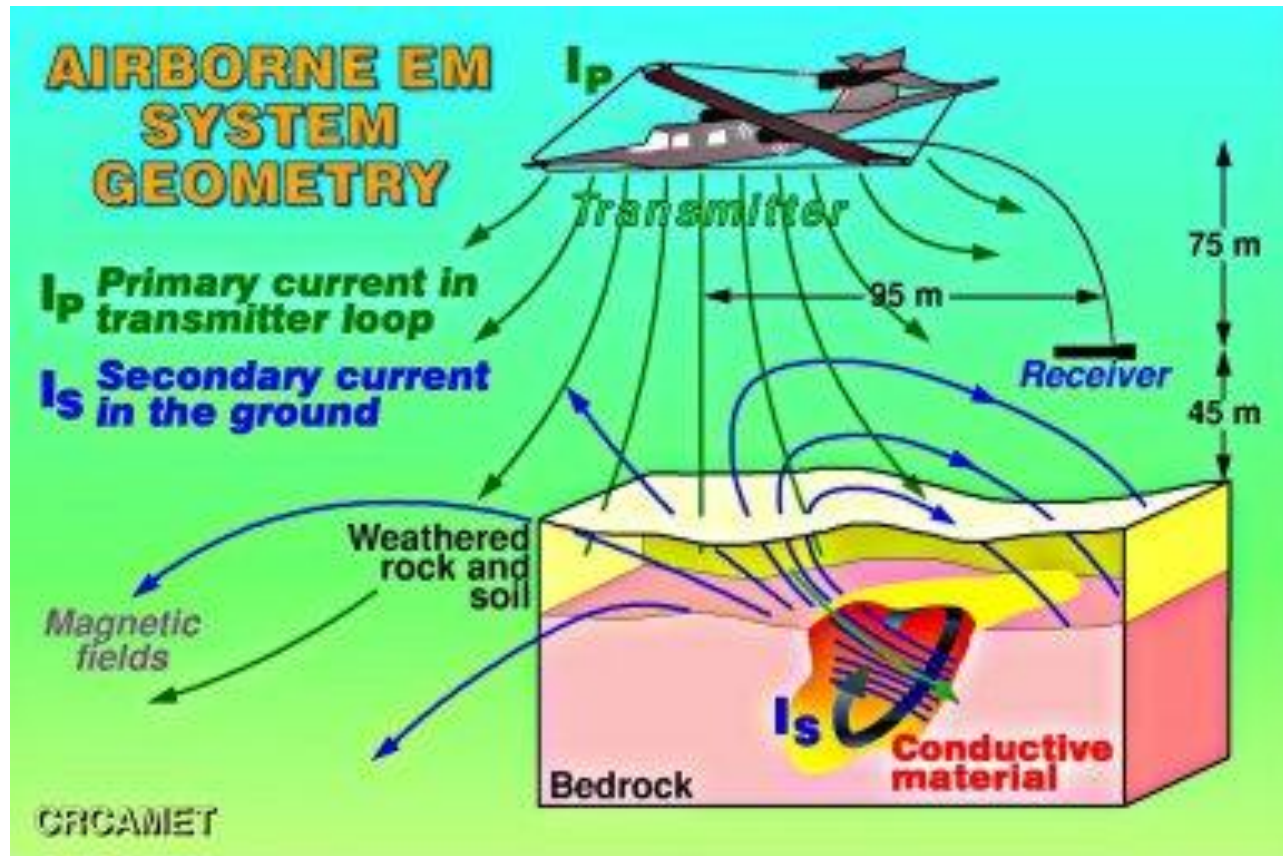


Important elements

- Primary field must couple with the target
- Strength of the induced currents must be big enough to generate signal
- Need to choose which fields to measure



Airborne (Inductive source)

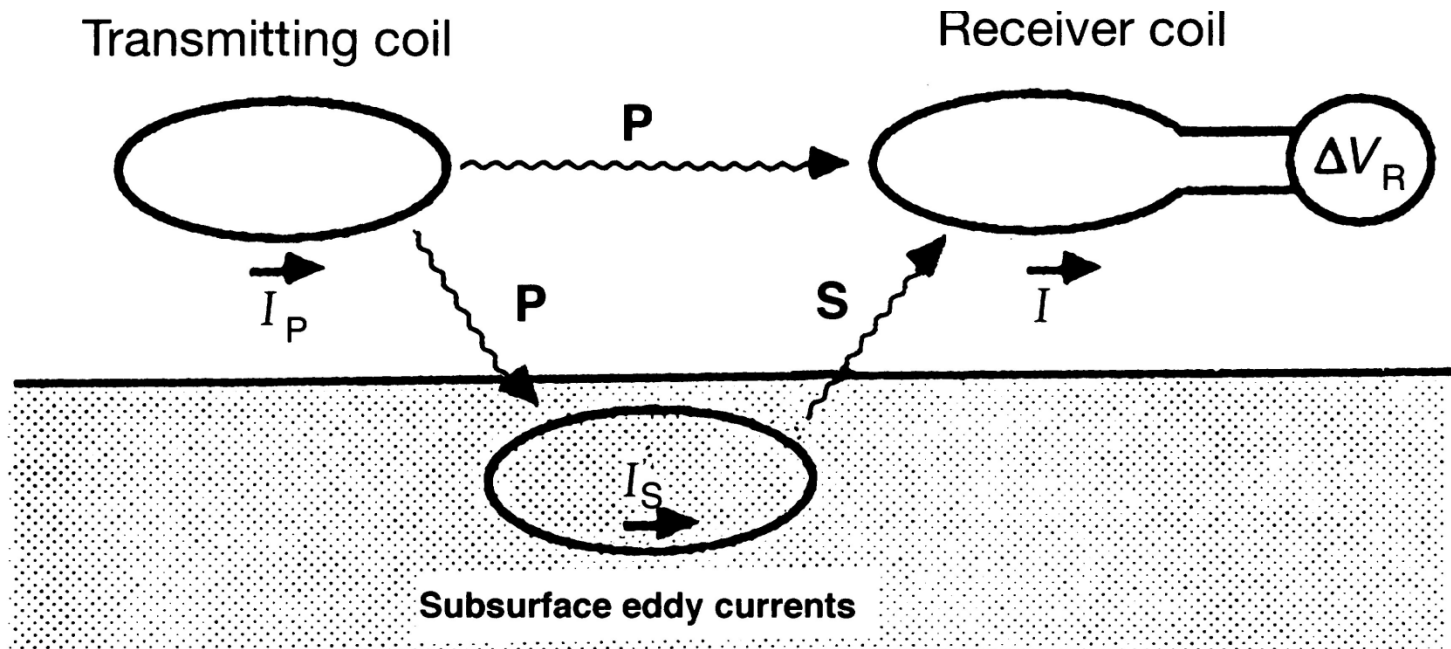


Elements of EM Induction

- Transmitter and primary magnetic field
- Magnetic flux and coupling
- Target and induced currents
- Secondary magnetic fields
- Receiver
- Data



Generic EM system

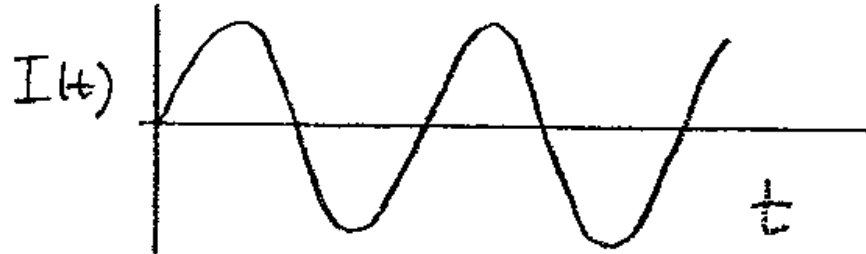
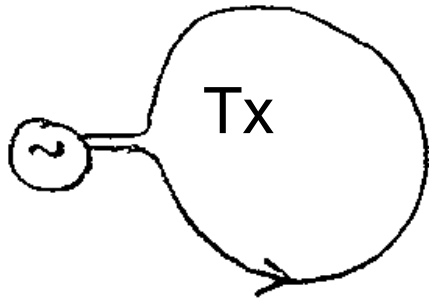


Tx: transmitter Rx: receiver

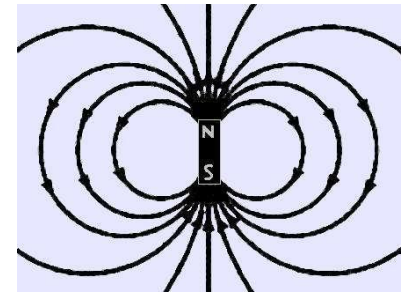
Tx, Rx, target body are represented as circuits



Transmitter



Magnetic field of a loop of current is like a magnetic dipole

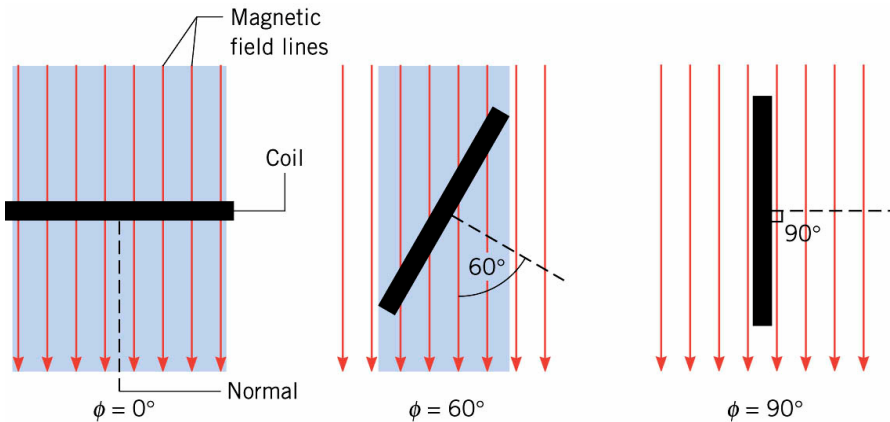
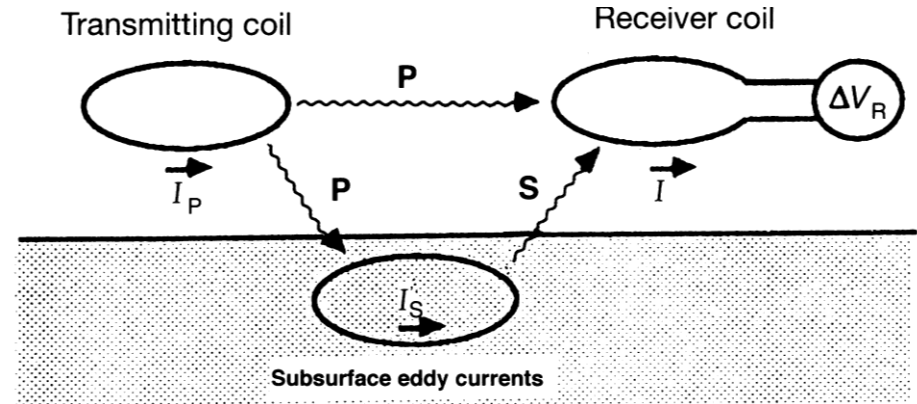
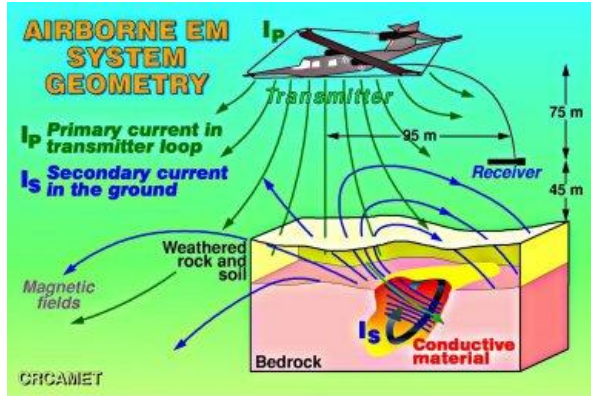


Dipole moment $m = I A$ (current x area)

Orientation of loop shows direction of primary field



Couple with the target



Max flux

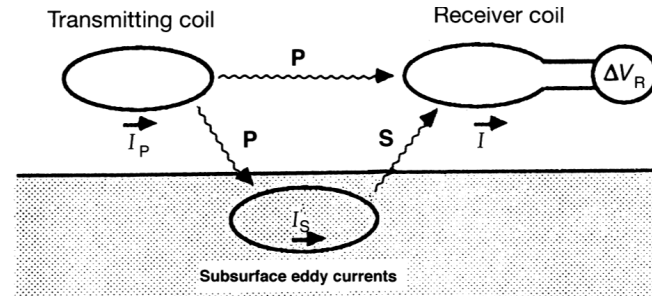
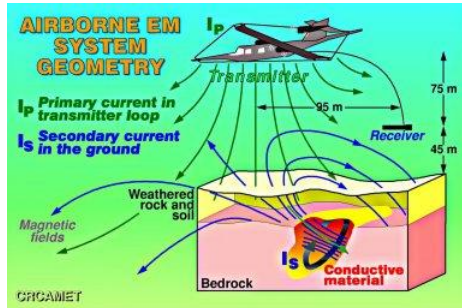
Zero flux

$$\phi_B = \int_{\text{area}} \vec{B} \cdot \hat{n} \, da$$

$$V = -\frac{d\phi_B}{dt}$$



Induced Currents in the Target



Think of target as an electrical circuit

$$\phi_B = \int_{\text{area}} \vec{B} \cdot \hat{n} \, da$$

Resistance R (small R means large current)

$$V = -\frac{d\phi_B}{dt}$$

Inductance L (accounts for interaction of currents in the target)

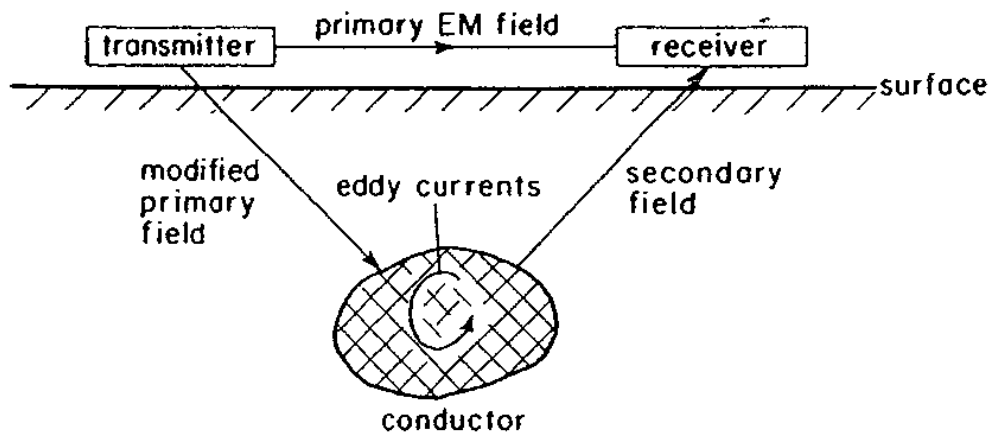
Max flux

Zero flux



Secondary Magnetic Fields

- Currents in the target generate magnetic fields
- If target is modelled by a current circuit then secondary magnetic fields are like those of a magnetic dipole.

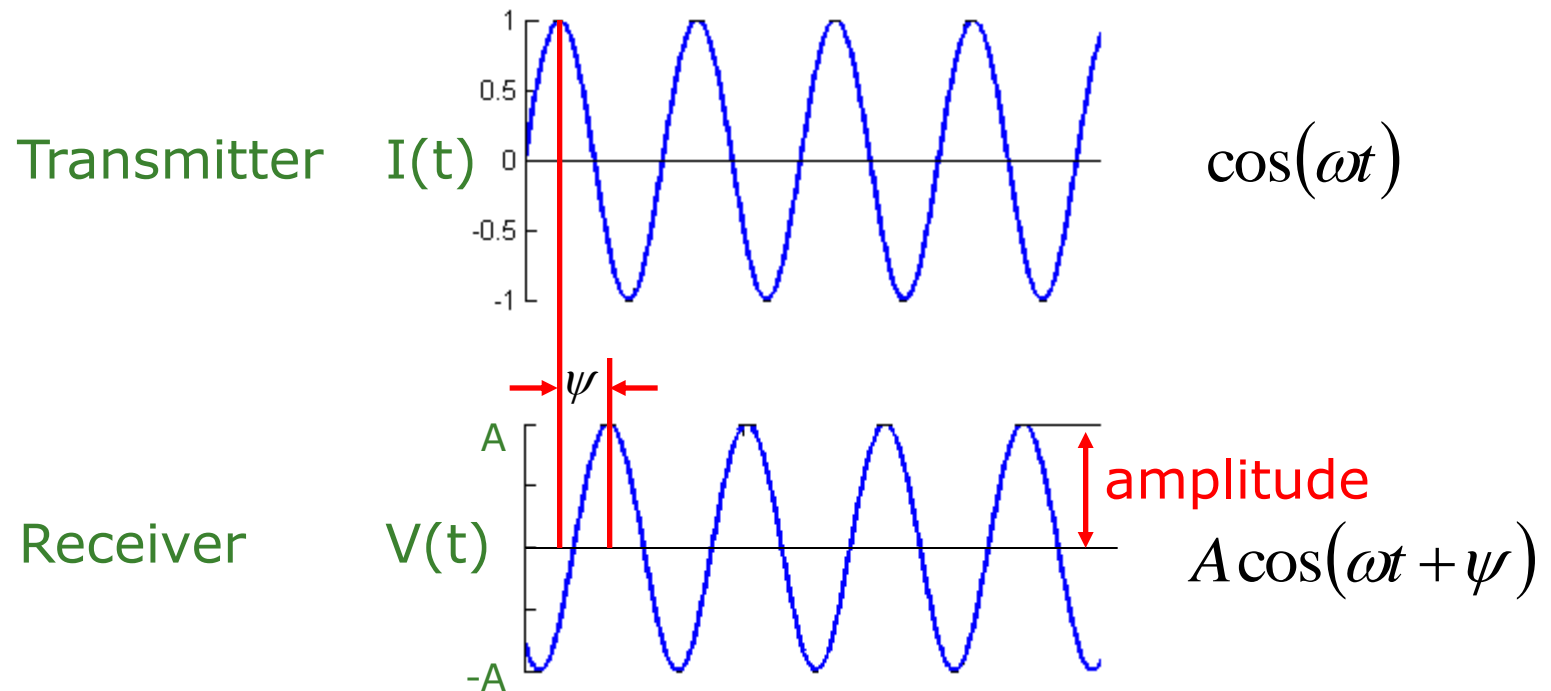


Receiver

- Receiver is a coil. A time varying flux generates a voltage.
- For some instruments H_p is known and subtracted. Then receiver measures only H_s .



Frequency domain EM data



Measure amplitude and phase (A, ψ)

$$\text{Or } A \cos(\omega t + \psi) = \underbrace{(A \cos \psi)}_{\text{In-phase}} \cos \omega t + \underbrace{(A \sin \psi)}_{\text{Out-of-phase}} \sin \omega t$$

In-phase
Real

Out-of-phase
Imaginary



Data

- Signal in receiver is harmonic (sinusoid) but not in phase with the primary.

- Decompose into portion

$$\psi = \frac{\pi}{2} + \tan^{-1}\left(\frac{\omega L}{R}\right)$$

- In-Phase (Real)
- Out-of-phase (Quadrature, Imaginary)

$$\begin{aligned}H_s \cos(\omega t + \psi) &= H_s \{ \cos(\omega t) \cos \psi - \sin(\omega t) \sin \psi \} \\ &= \{ H_s \cos \psi \} \cos(\omega t) - \{ H_s \sin \psi \} \sin(\omega t)\end{aligned}$$

$$\text{In - phase : } \frac{H_s \cos(\psi)}{H_p}$$

$$\text{Out - of - phase : } \frac{H_s \sin \psi}{H_p}$$



Understanding the Data

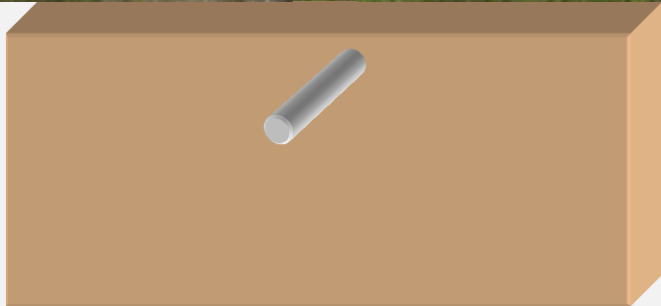
- Read the electromagnetic notes
- Learn how to understand the response of a system like the EM31 as it goes over a conductive plate.
- The first task is to work with the basic principles of EM induction and sketch out the signal caused by geometry



Effect of buried objects

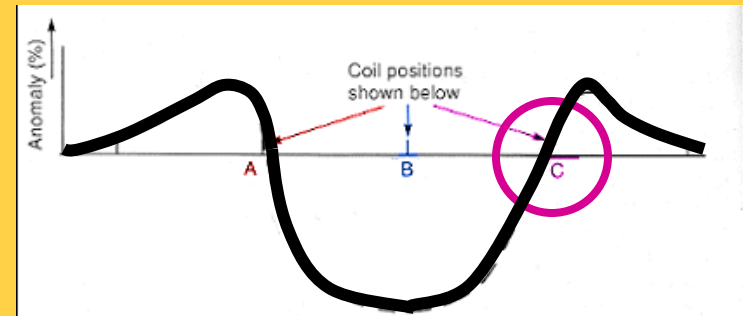
- See GPG Ch3.h.
- Source field moves with receiver.

FIELD



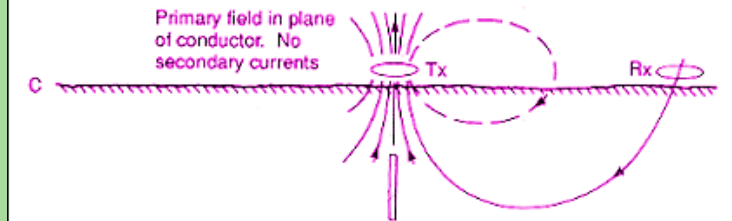
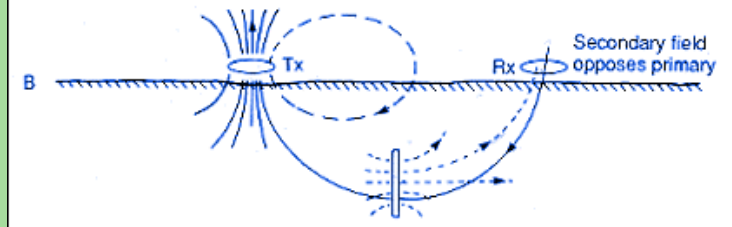
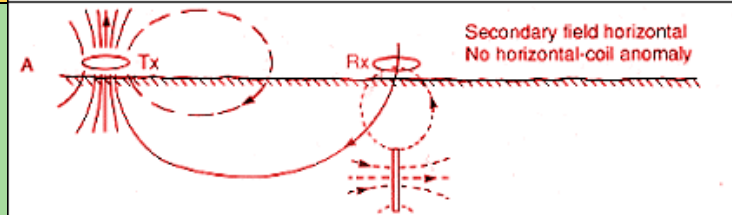
DATA

Graph measurements vs line position

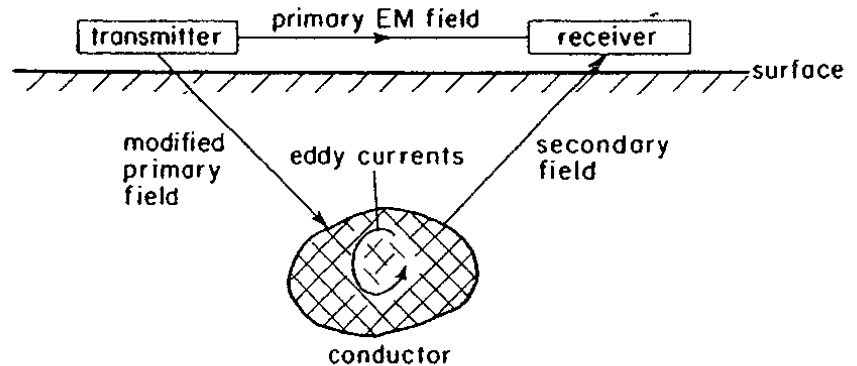


PHYSICS

Instrument, fields, and target



EM Induction: Sun



- Time varying magnetic magnetic field generates an electric field E
- $J = \sigma E$ (induced currents) (Coupling is important)
- Induced currents generate secondary magnetic fields
- Secondary magnetic fields are recorded at the receiver. Coupling is important.
- Receiver outputs In-Phase and Out-of-phase data

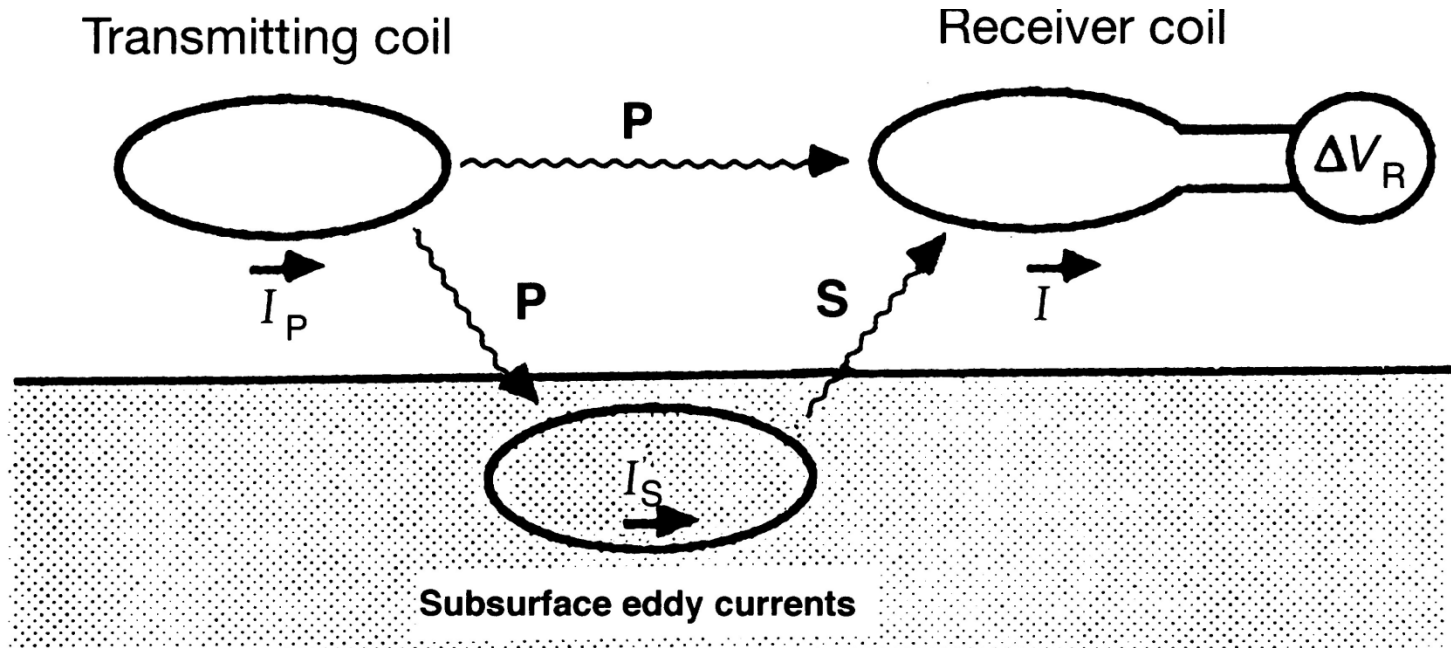


Understanding the Data

- We can now sketch the effects of geometry and coupling on an EM31 as it passes over a plate. This is essentially controlled by geometry and coupling.
- Next we'll consider the information in the in-phase and quadrature phase
- Read the EM notes
- Matlab routine to estimate the responses.
- demos.....



Earth is also a conductor

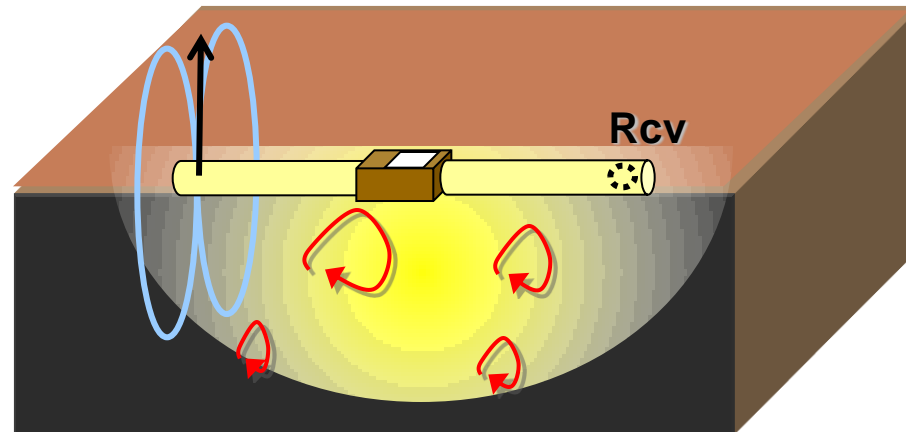


Depth of investigation depends upon
skin depth
source receiver geometry



Meaning of readings over earth

- Earth is a conductor so currents are induced everywhere.
- Reading is two numbers.



Inphase/Quadrature

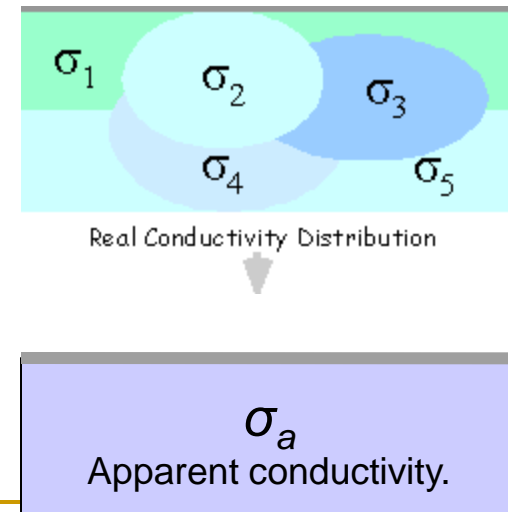
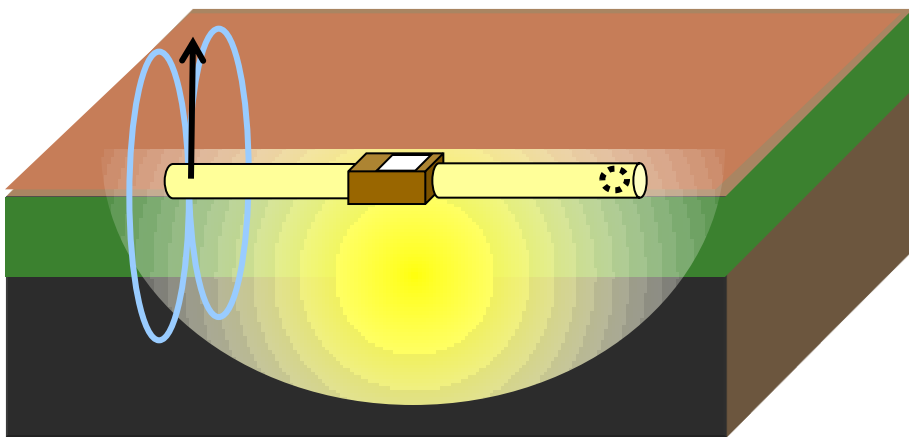
The EM-31 gives two measurements called the In-phase and Quadrature

- In-phase: (also called “real”)
Particularly useful for find good conductors
(metal pipes, drums)
- Quadrature: (also called “imaginary” or (out of phase)
Yields apparent conductivity (if $s > \delta$)



Implications over “real” earth

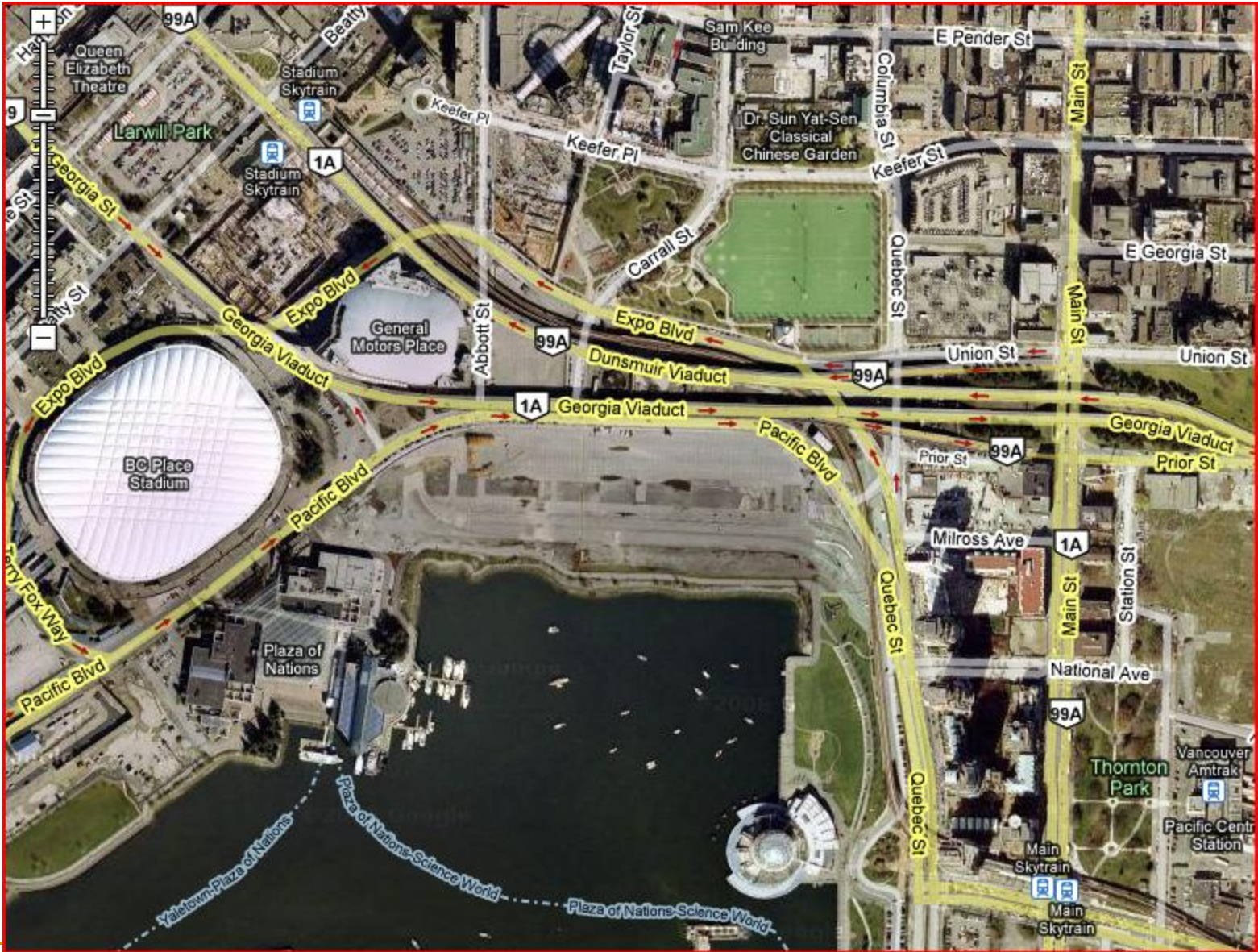
- Reading are “true” values of the ground’s physical property ONLY over uniform ground.
- Therefore, result is “**apparent**” conductivity.
- Result over NON-uniform ground is a complicated weighted average of all materials.



Case History Project: Expo Site

- Integrated site investigation of contaminated waste site in Vancouver
- Combines all the geophysical methods covered in EOSC 350: Magnetism, GPR, Seismic refraction and EM induction





Industrial Site

Resources

Introduction

- Problem outline
- All text in PDF format

Contractor's report:

- ch1: Site history
- ch2: Site characteristics
- ch3: EM-31 results
- ch4: Gradient mag
- ch5: GPR results
- ch6: Seismic refraction

Additional information

- Comment: hydrocarbons
- Overlay data plots
- Flicker animations
- mag dipole applet

Outlines of survey methods

| EM-31 | GradMag | GPR |

Data spreadsheets

| em31 | seis | gradmag |

Activities

- Background tasks
- Interpretation tasks
- 2 blank site maps

Disclaimer

These geotechnical questions and geophysical problems were created using photos and sketches of a real field site and data were gathered to suit the teaching and learning needs of the exercises. Therefore, they are not necessarily applicable to a real field location.

The context

The field site in question is an urban area with a complex industrial construction of public space. There are many questions about the results of the geophysical surveys. Examples include:

- What is the thickness of the mixed fill layer (i.e. what is the depth of the fill)?
- What is the distribution of buried objects? Many objects are small pieces of industrial trash, to railway lines, reinforced concrete structures.
- Can geophysics contribute any information about the extent of the fill? The fill consists of a wide range of fill materials?
- Where is fill material dominated by wood waste, making geophysics difficult?
- You can probably think of other questions that might be of interest.

Finally, it is worth noting that the actual field site was fully remediated by the Soils and Remediation Group, May 1992. For a brief discussion see [information on hydrocarbons](#) after the contractor's report

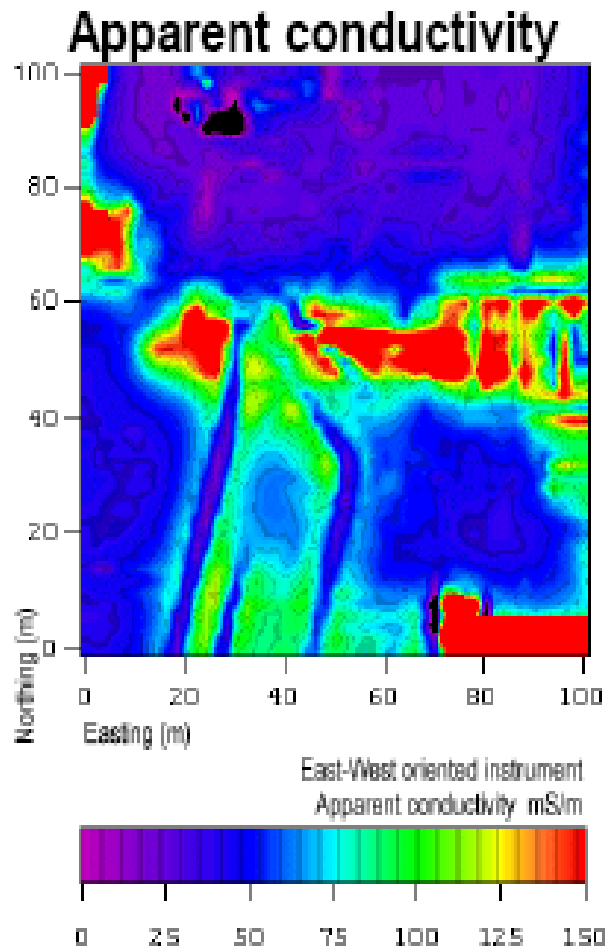
Instructions

This exercise involves using geophysics to address an environmental problem. The EM-31, gradient magnetics data, and GPR results are all involved. Proceed as follows:

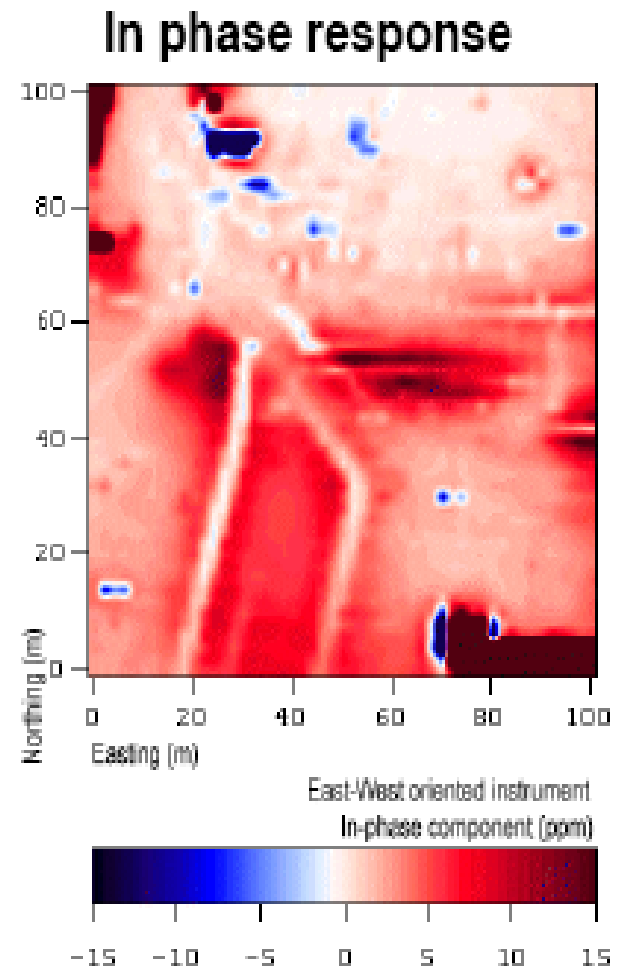
1. Read all content pages, and familiarize yourself with all the data.
2. You will have chosen ONE survey method to work up some



EM in phase and quad phase?

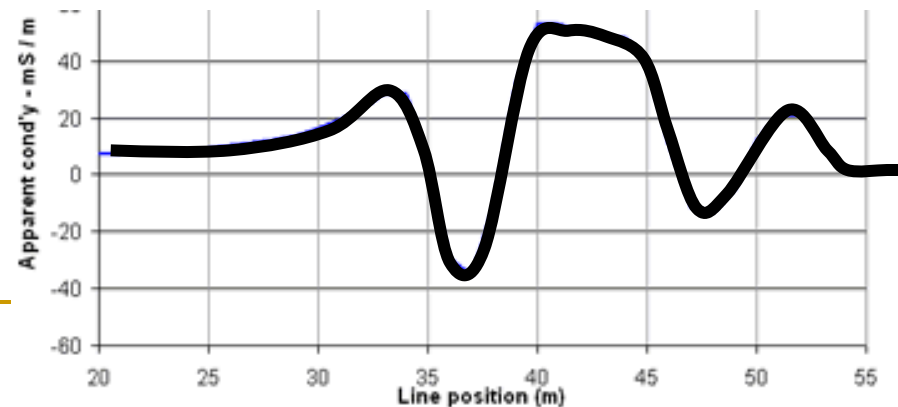
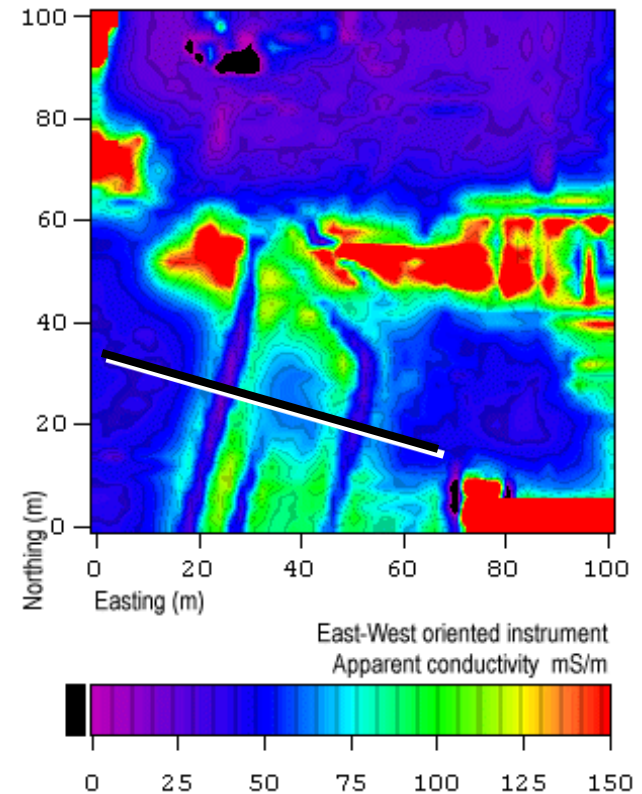


Instrument
size? ~4m



Effect of buried objects

- Contour plotted area data:
- Where are peak & trough patterns?
- Where are large responses?
- Where are negative responses?



EM Summary so far

- Basics of EM induction
- Sketch approximate anomalies for a simple system (EM31) that traverses a confined body
- Responses for EM31 and application



Readings for Electromagnetics

- Electromagnetics 1.0 Fundamentals
- GPG.h

