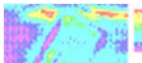
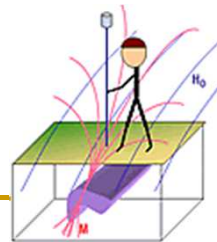


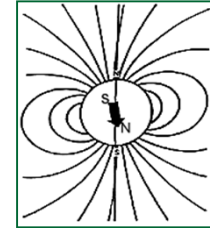
# Magnetic surveying

**After today, you will be able to**

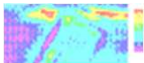
- Sketch anomalies over objects at any location, and explain how you derived the pattern.
- Explain the relation between dipoles and real targets.
- Outline the needs of a field survey.
- Outline necessary & some optional processing.



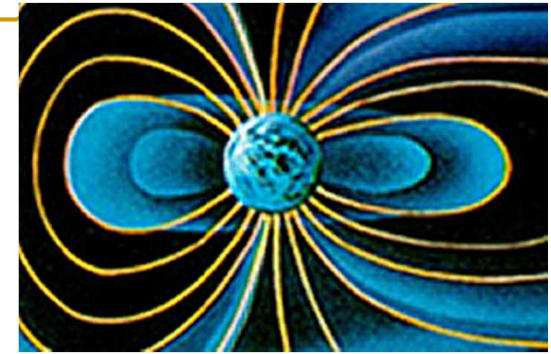
# *Basics of Magnetism Surveying*



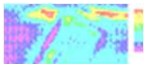
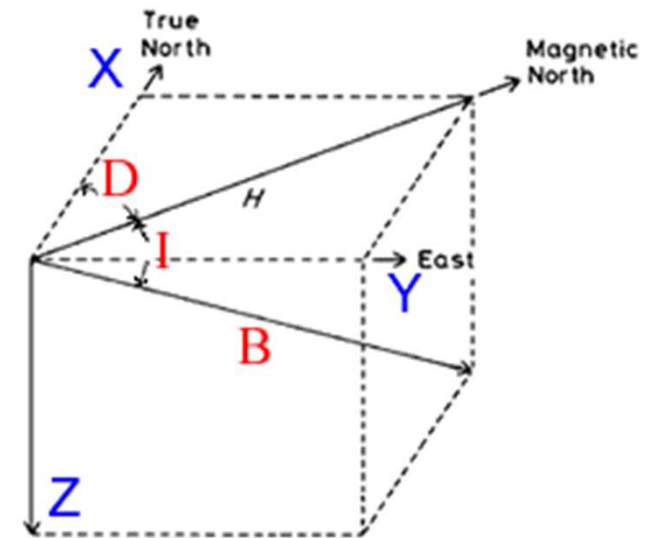
1. Earth's magnetic field is the source:
2. Materials in the earth become magnetized  
( $M = \kappa H$  where  $H = B/\mu_0$ ) (dipole moment per unit volume)
3. Magnetized material creates anomalous field (applet)  
magnetic moment  $m = M \times (\text{volume})$
4. Magnetometer measures the total field
5. Anomalous field obtained by subtracting off the earth's field



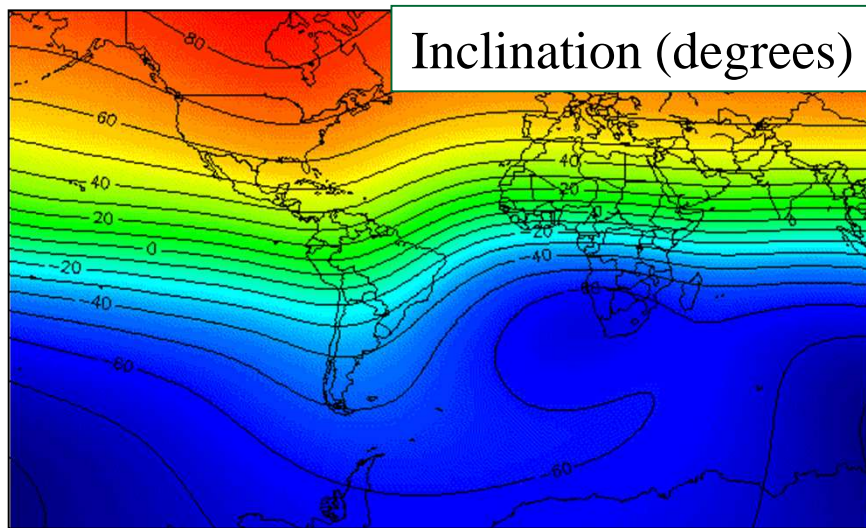
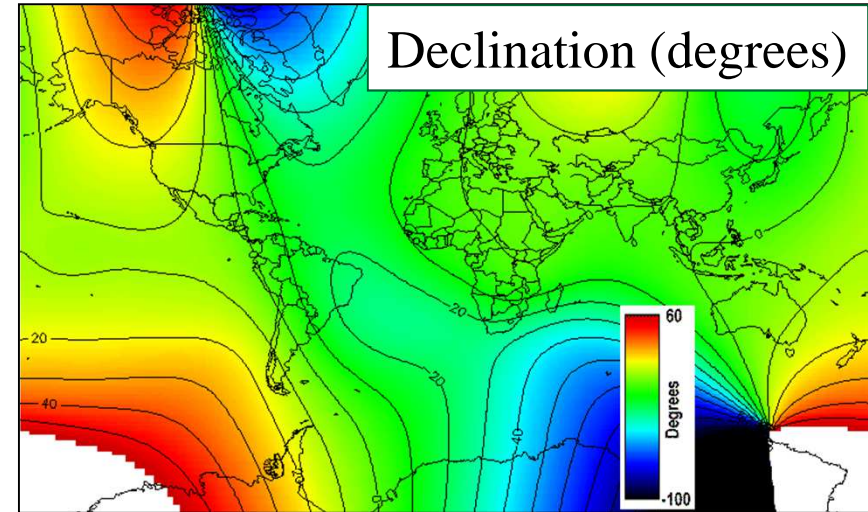
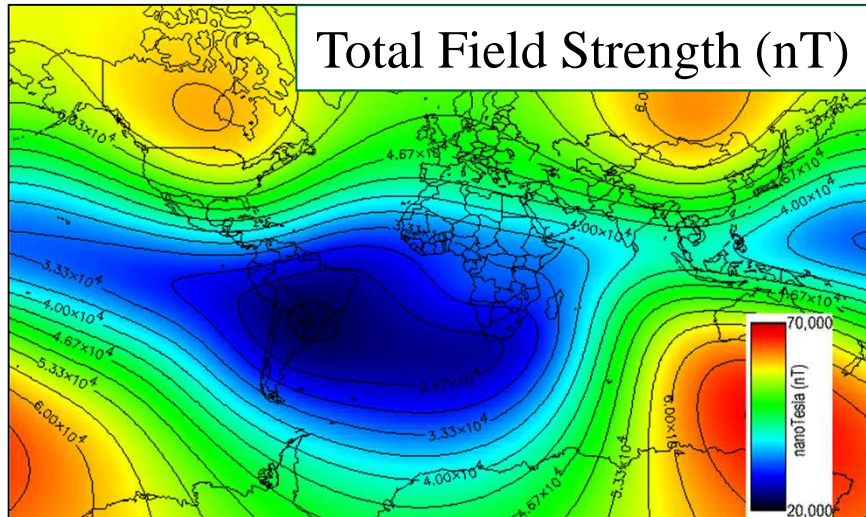
# Magnetics – Earth's field



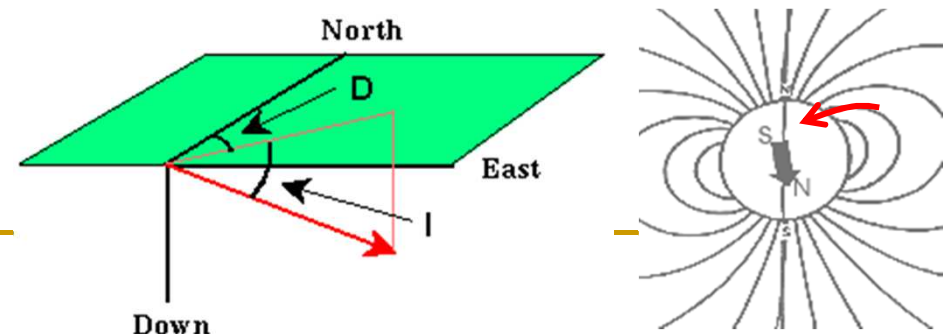
- Web Notes, GPG Ch.3.d.7.
- How is the field described anywhere?
  - X, Y, Z
  - Inclination, Declination, Magnitude
- Compass? Inclination?
- Declination?
- Earth's field strength vs anomalies.



# Earth's magnetic field: Strength $|B|$ Inclination $I$ Declination $D$



$$\begin{aligned} B_{\max} &= 70,000 \text{ nT} & H_{\max} &= 55.7 \text{ A/m} \\ B_{\min} &= 20,000 \text{ nT} & H_{\min} &= 15.9 \text{ A/m} \end{aligned}$$



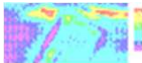
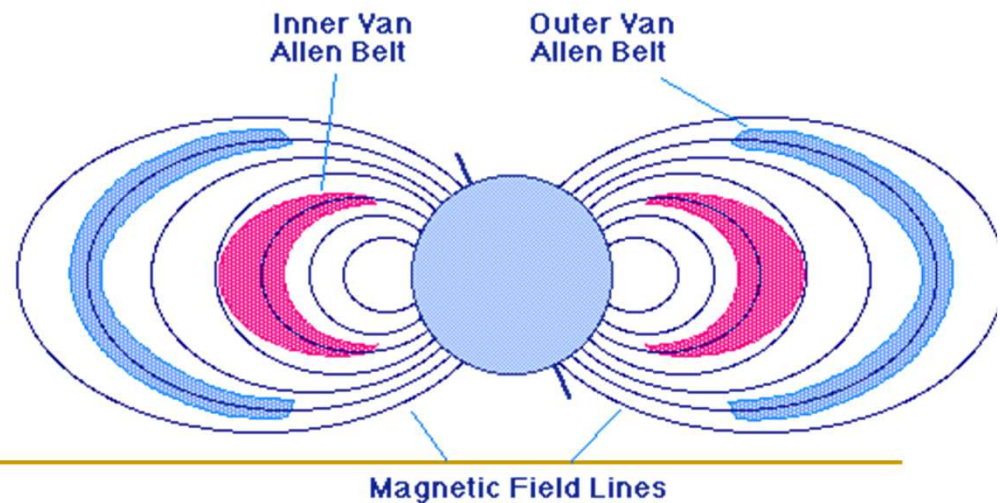
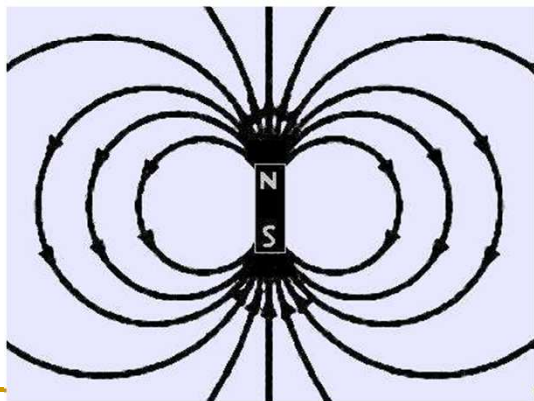
<http://www.ngdc.noaa.gov/cgi-bin/seg/gmag/igrfpg.pl>



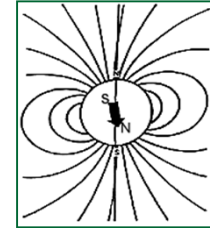
# Magnetic field due to a dipole

- A “dipole” is the basic quantity in magnetostatics

$$\mathbf{B} = \frac{\mu_0}{4\pi} \frac{\mathbf{m}}{r^3} (3 (\hat{\mathbf{m}} \cdot \hat{\mathbf{r}}) \hat{\mathbf{r}} - \hat{\mathbf{m}})$$



# *Basics of Magnetism Surveying*



1. Earth's magnetic field is the source:

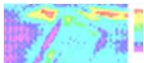
2. Materials in the earth become magnetized

( $\mathbf{M} = \kappa \mathbf{H}$  called **Magnetization** (dipole moment per unit volume)

. where  $\mathbf{H} = \mathbf{B}/\mu_0$ )

3. Magnetized material creates anomalous field (applet)

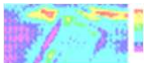
**magnetic moment  $\mathbf{m} = \mathbf{M} \times (\text{volume})$**



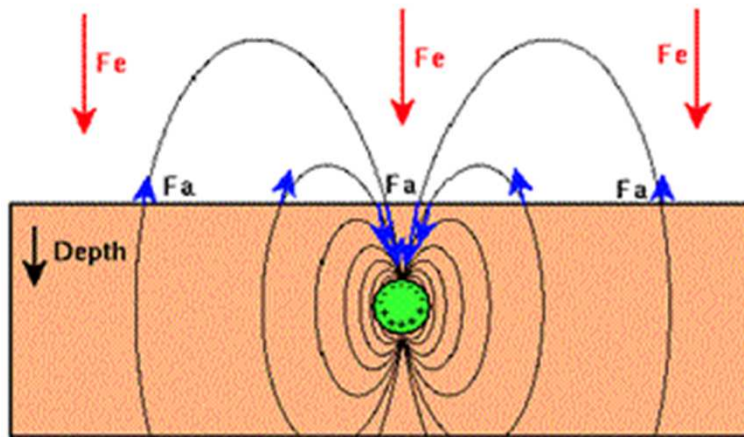
---

# Drawing the field due to buried dipoles

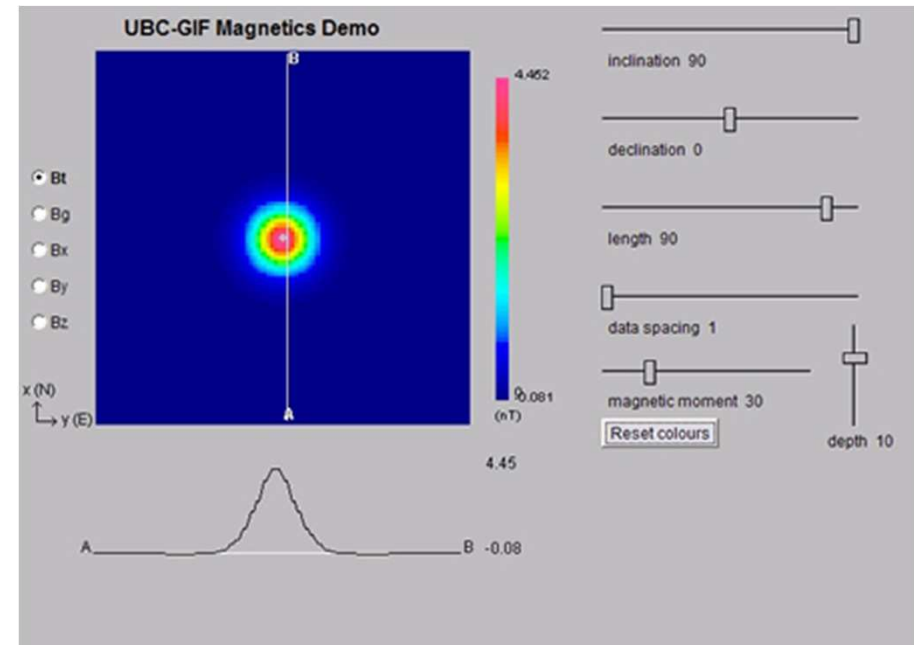
- Use the java applet on the website:
- Via GPG 8.c “Start the applet alone here”
- Or via:
- [http://www.eos.ubc.ca/courses/eosc350/content/exercises/meth\\_3a/dipoleapp.html](http://www.eos.ubc.ca/courses/eosc350/content/exercises/meth_3a/dipoleapp.html)
- (there will be a link on the main EOSC 350 page)



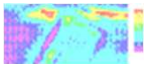
# Examples



**Fe – Earth's Main Magnetic Field**  
**Fa – Induced Anomalous Magnetic Field**

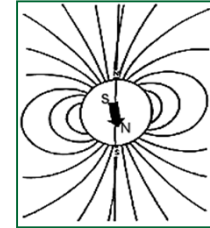


Note: To plot data we need a sign convention. Here we say that if a field points in the same direction as the source field, it is plotted as a positive value.





# *Basics of Magnetics Surveying*



1. Earth's magnetic field is the source:

2. Materials in the earth become magnetized

( $\mathbf{M} = \kappa \mathbf{H}$  called **Magnetization** (dipole moment per unit volume)

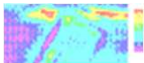
where  $\mathbf{H} = \mathbf{B}/\mu_0$ )

3. Magnetized material creates anomalous field (applet)

**magnetic moment  $\mathbf{m} = \mathbf{M} \times (\text{volume})$**

4. Magnetometer measures the total field

5. Anomalous field obtained by subtracting off the earth's field



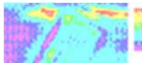
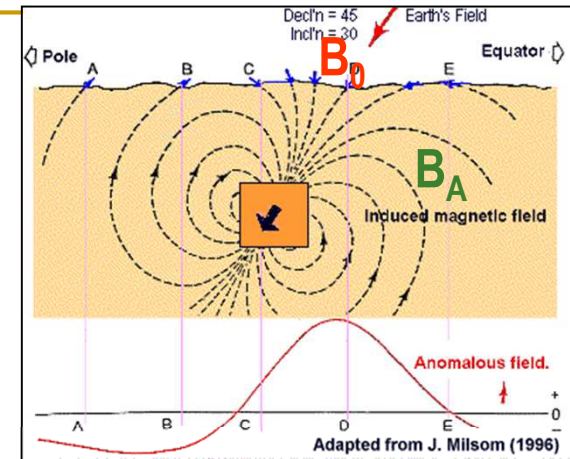
# The composite field

$$\text{Composite field } \mathbf{B} = \mathbf{B}_0 + \mathbf{B}_A$$

- The field components are

- $\mathbf{B} = \{ \mathbf{B}_x \ \mathbf{B}_y \ \mathbf{B}_z \}$

— — — — —



# The Anomalous field

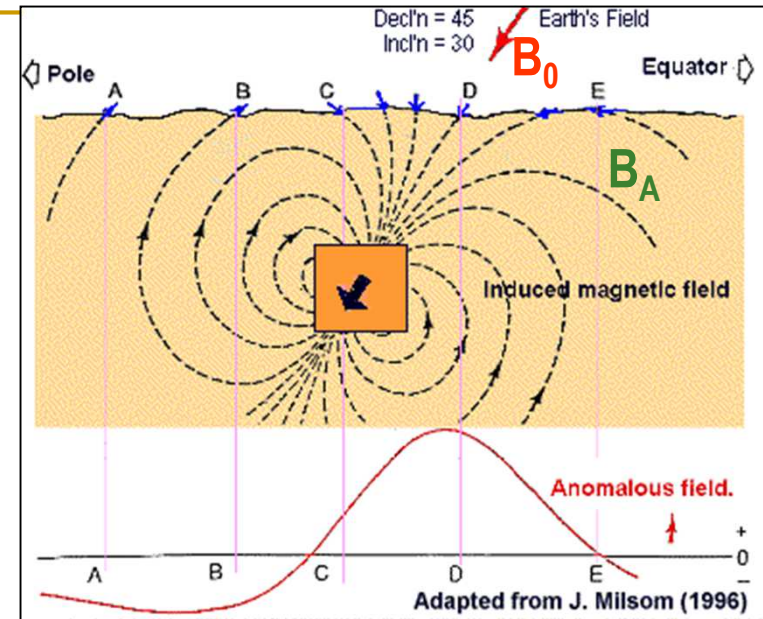
Measured field  $\mathbf{B} = \mathbf{B}_0 + \mathbf{B}_A$

- Therefore components are:

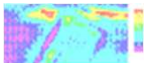
$$B_{AX} = B_X - B_{0X},$$

$$B_{AY} = B_Y - B_{0Y},$$

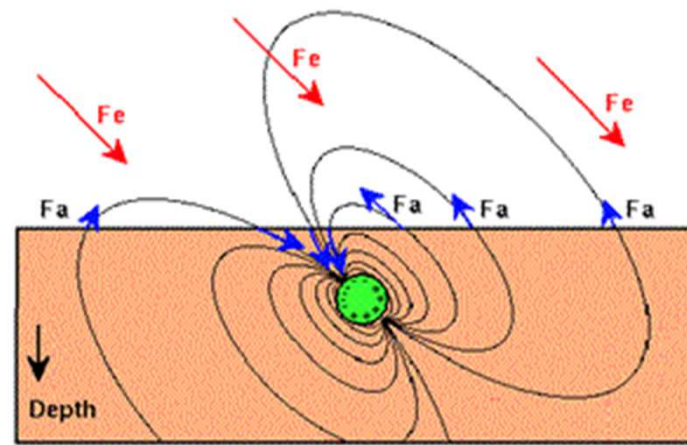
$$B_{AZ} = B_Z - B_{0Z}$$



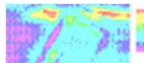
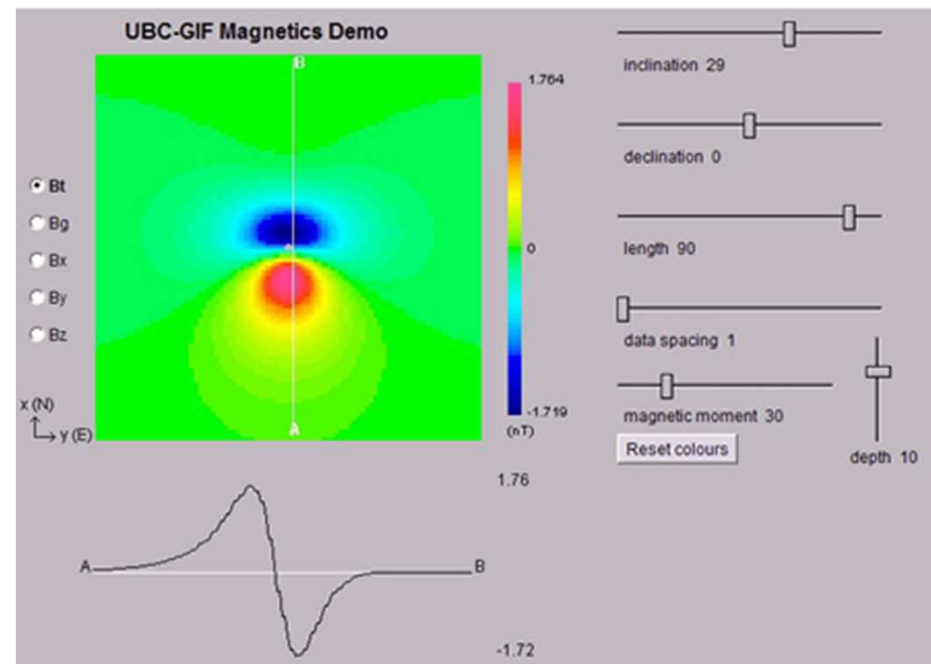
- The *total field anomaly*:  $\Delta \mathbf{B} = |\mathbf{B}| - |\mathbf{B}_0|$
- If  $|\mathbf{B}_A| \ll |\mathbf{B}_0|$  then 
$$\Delta B \cong (\mathbf{B}_A \cdot \hat{\mathbf{B}}_0)$$
- That is, total field anomaly  $\Delta \mathbf{B}$  is the projection of the anomalous field onto the *direction* of the inducing field.



# Examples



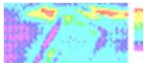
Fe = Earth's Main Magnetic Field  
Fa = Induced Anomalous Magnetic Field



---

## Details on Anomalous Field

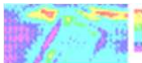
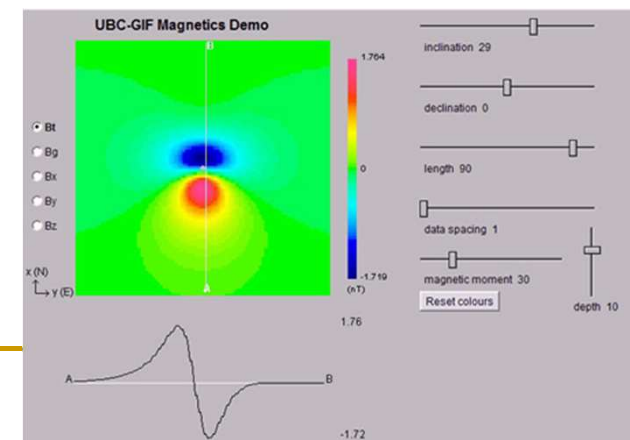
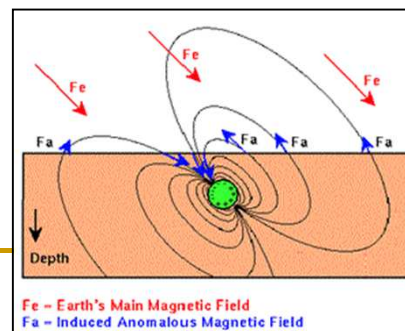
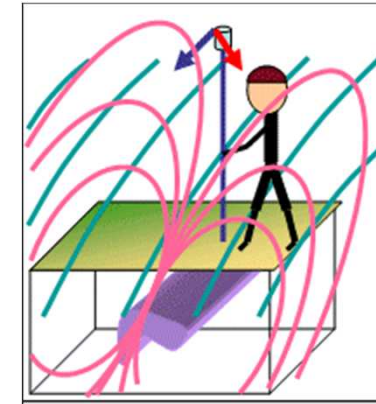
- See GPG d.8 Principles (anomalous fields)
- Also read: Magnetics GPG 3.d.0 – 3.d.13





# Magnetics – Data

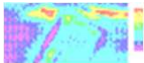
- What exactly is measured?
  - GPG Ch.3.d.1.
  - The “**total field magnetic anomaly**”.
- Consequently, what pattern of response can be expected for buried targets? (sketch on BB)
  - Start simple – buried dipole. GPG Ch.3.d.2.
  - Response to shallow or deep dipole targets.
  - Response near magnetic poles ...  
... near magnetic equator.



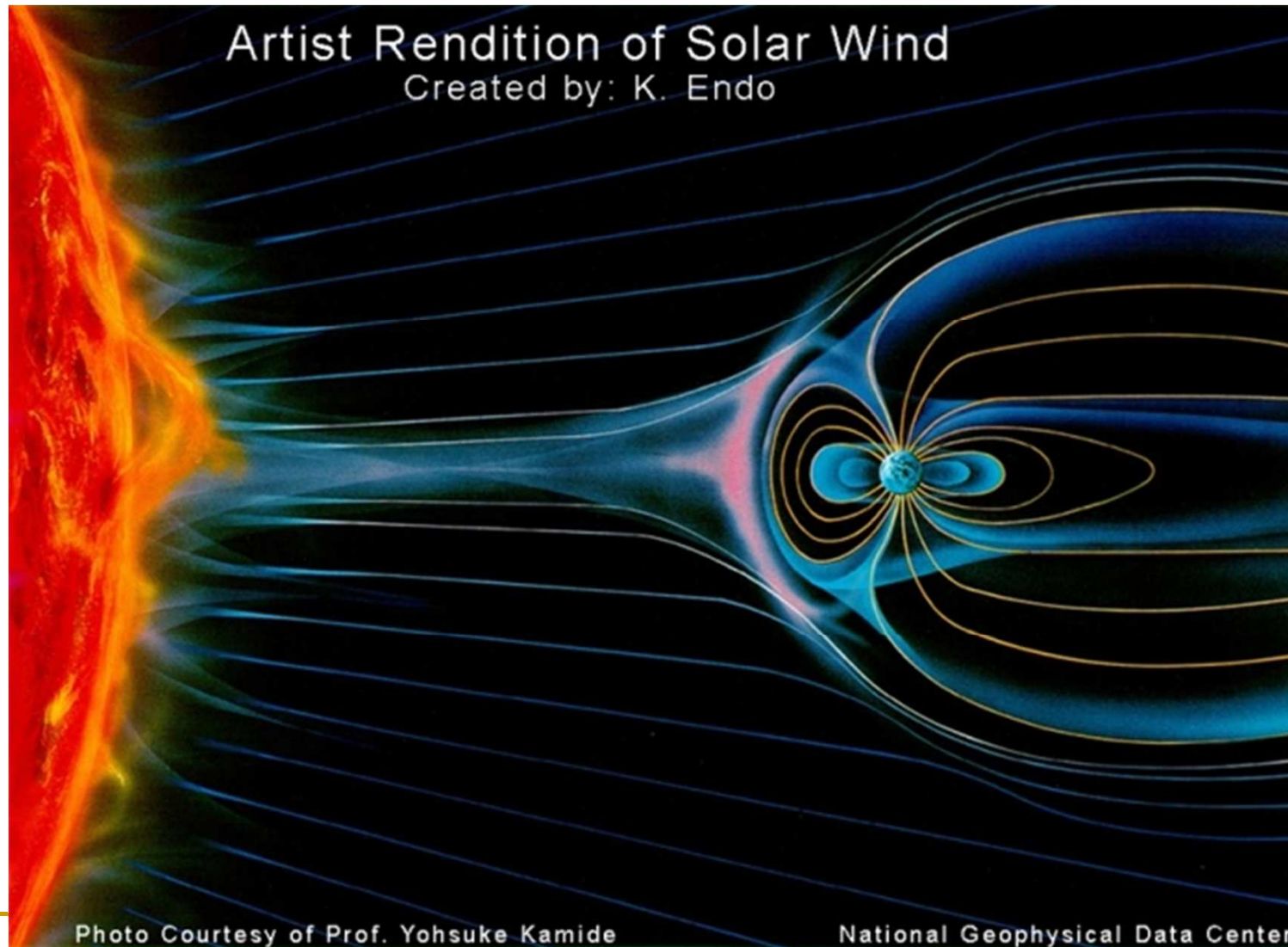
---

# Processing Magnetic Field data

- Account for time variations (need a base station)
- Remove regional



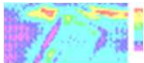
# Magnetics – Earth's field



---

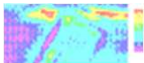
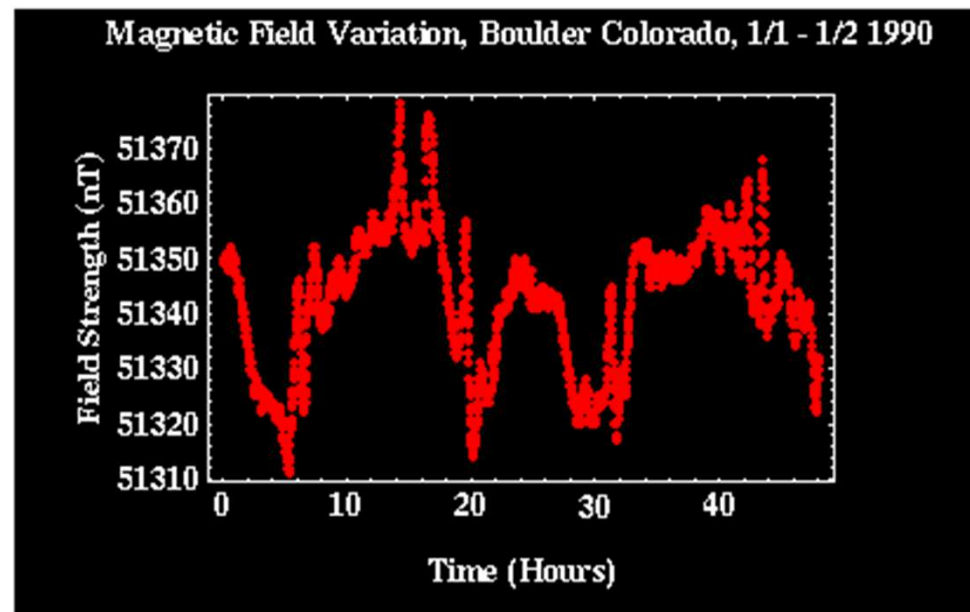
# Time Variations of the Earth's Field

- External sources
  - ❑ Solar wind (micro-seconds, minutes, hours)
  - ❑ Solar storms (hours, days, months)
- Man made sources
  - ❑ Power lines (50/60 Hz plus harmonics) DC
  - ❑ Motors, generators
  - ❑ All electronic equipment
- Internal sources
  - ❑ Fluctuations in core (days – millions of years)



# Field procedures

- Earth's magnetic field varies as a function of time
- Necessary to record the magnetic field at a fixed location to determine the Earth's field

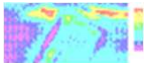




---

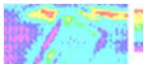
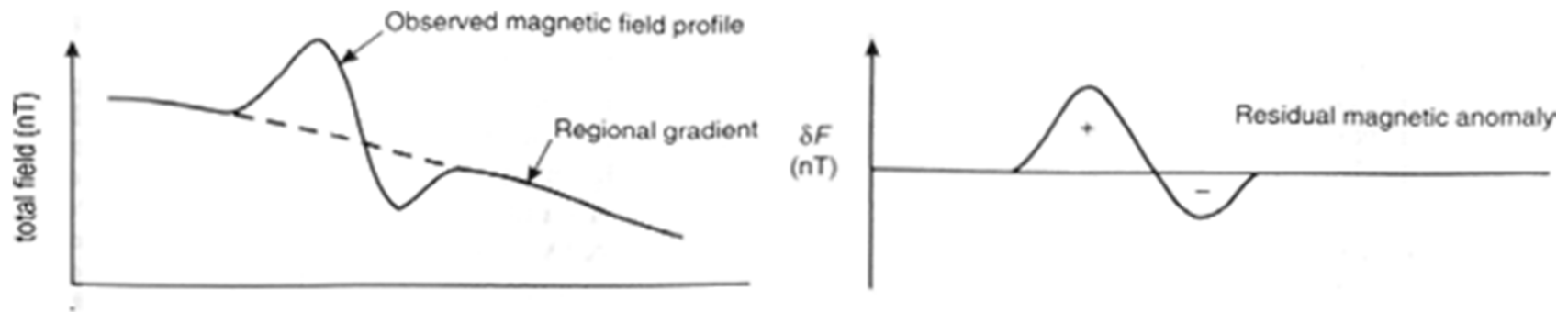
## Base station correction

- Set out another magnetometer (base station)
- Assume time variations at the base stations are the same as at the observation location
- Synchronize the times
- Perform a correction by subtraction

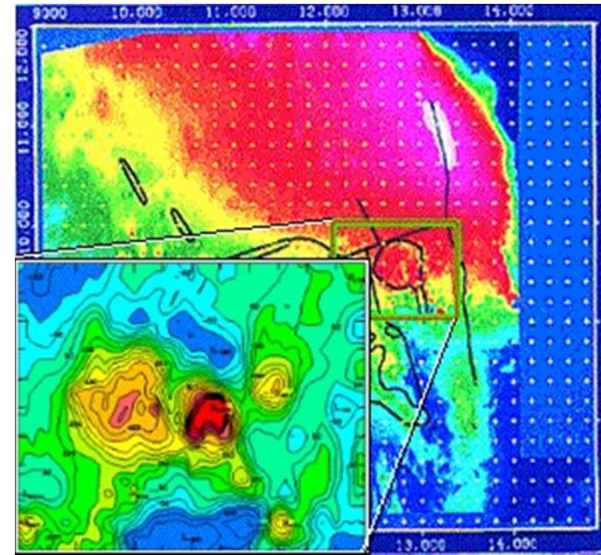
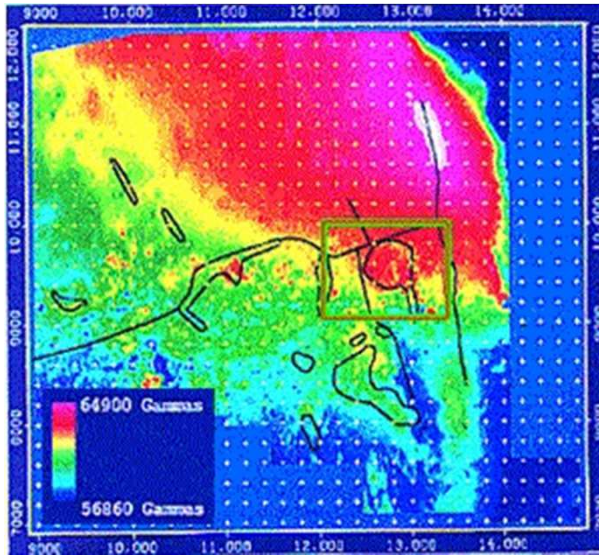


# Anomalous field

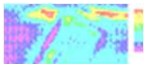
- We measure the field at the Earth's surface but we are interested in the “anomalous” features
- Regional removal



# Example of regional field removal

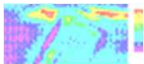


Airborne magnetic data gathered over a 25 square km area around a mineral deposit in central British Columbia. Some geological structural information is shown as black lines. The monzonite stock in the centre of the boxed region is a magnetic body, but this is not very clear in the data before removing the regional trend.



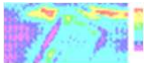
# Summary: Data Collection

- Now we know what is measured.
- How – to make measurements?
- Requirements:
  - Base station.
  - Positioning & time tied to each measurement.
  - Measurement while moving.
  - Identify potential noise sources.



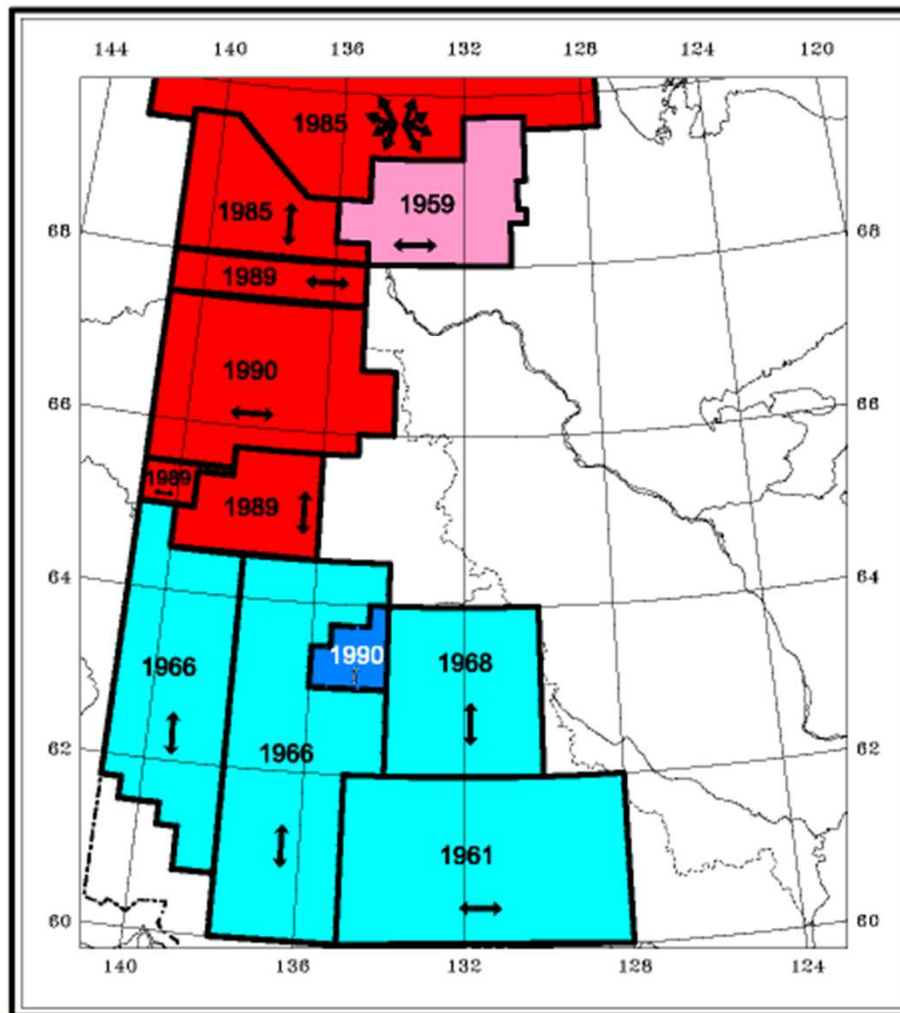
# Possible routes to extracting information

- Plot the data in various map displays
- Interpret with a dipole
- Interpret with simple bodies of uniform magnetization
- Interpret as complex bodies (inversion)








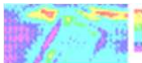


# Aeromagnetic map construction



## Legend/Légende

-  Constant altitude analogue acquisition  
Acquisition de données analogiques à altitude constante
-  Constant altitude digital acquisition  
Acquisition de données numériques à altitude constante
-  Mean terrain clearance analogue acquisition  
Acquisition de données analogiques à hauteur de sol constante
-  Mean terrain clearance digital acquisition  
Acquisition de données numériques à hauteur de sol constante
-  Flight line orientation  
Orientation des lignes de vol
- 1985 Year of survey  
Année du levé



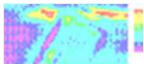
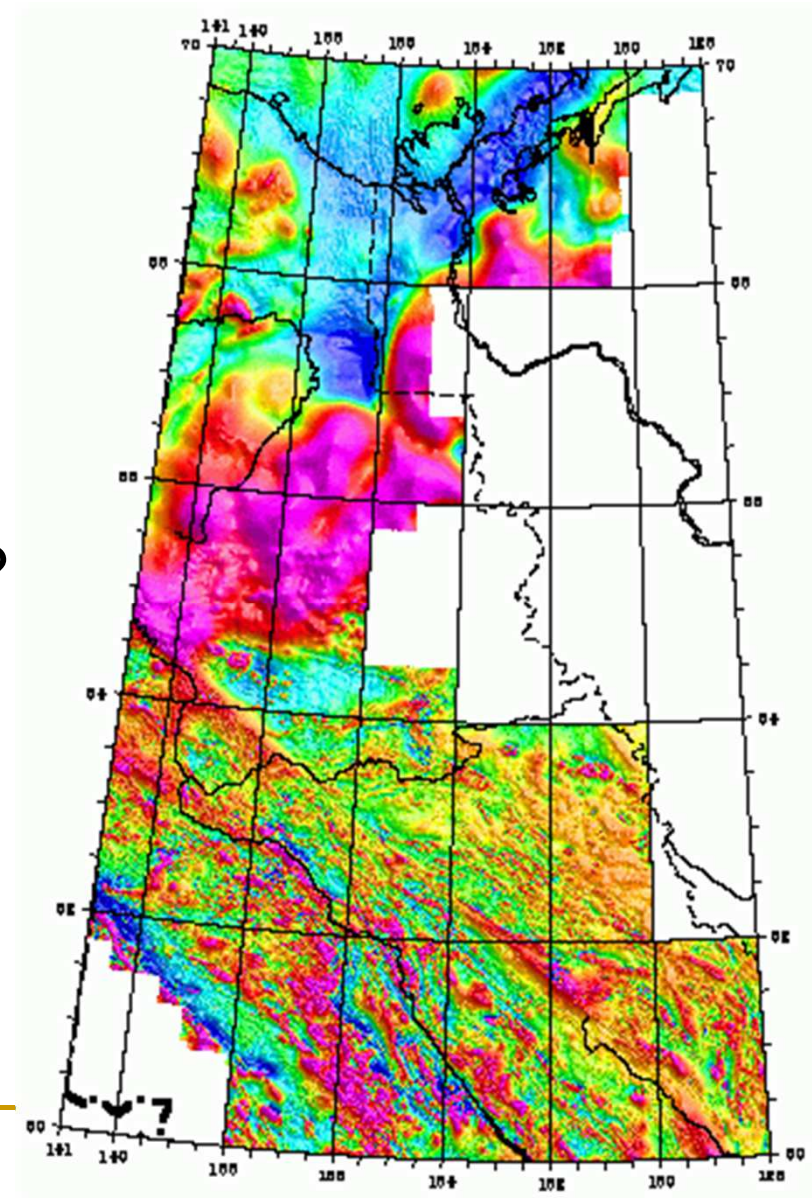
# Essential airborne data preparation (processing)

“**Levelling**” data maps

- Adjusting line locations
- drapping

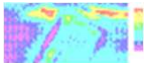
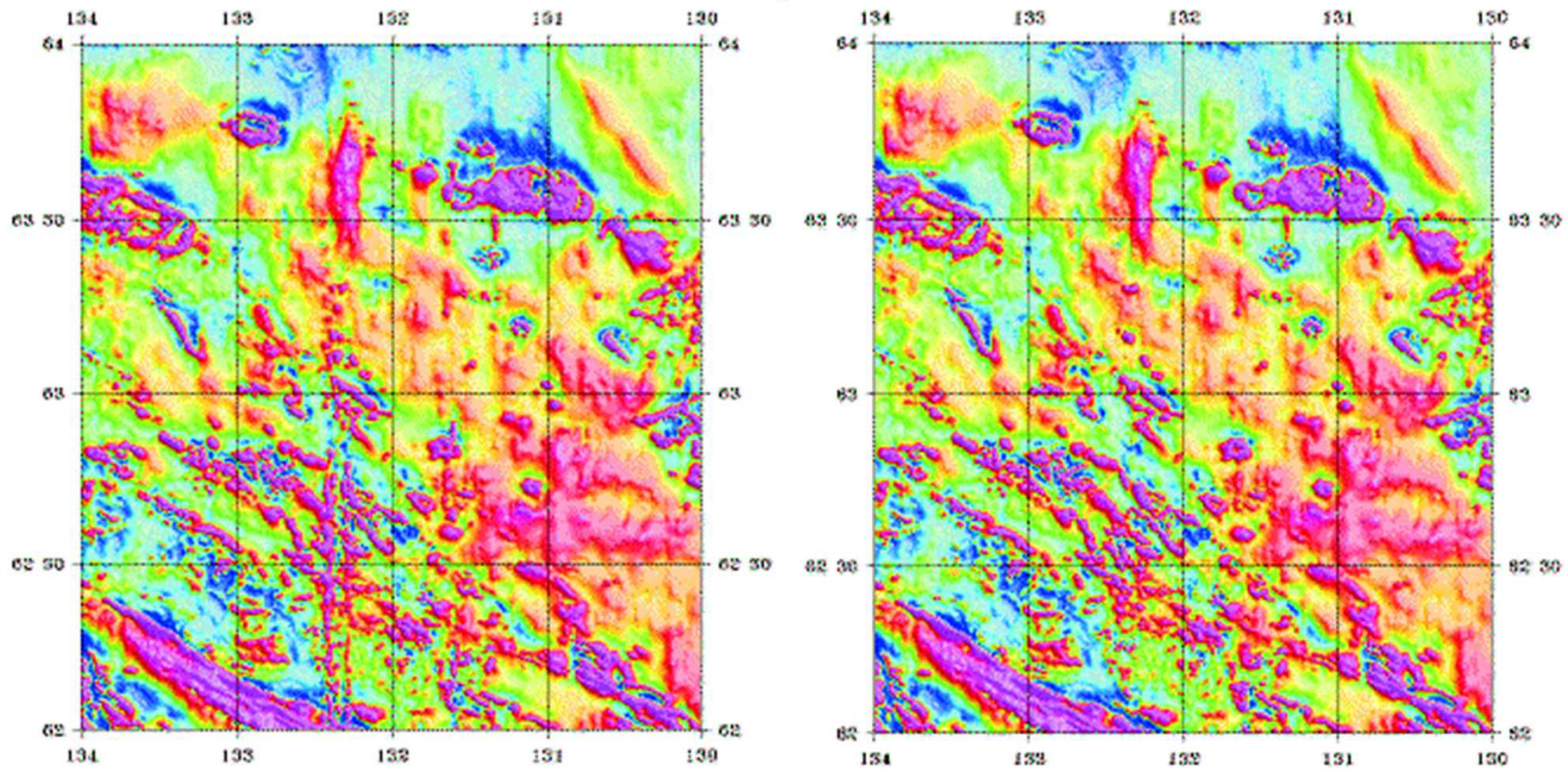
What can be learned directly?

- Trends
- Contacts
- Geologic settings





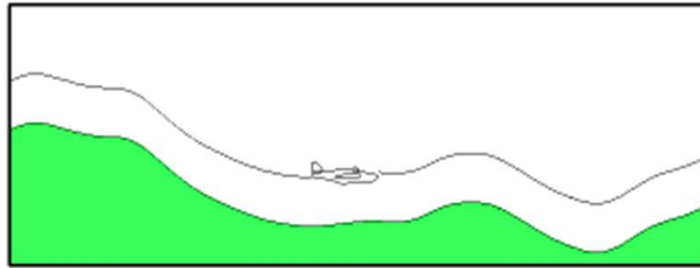
# Positioning errors of flight lines (old data)



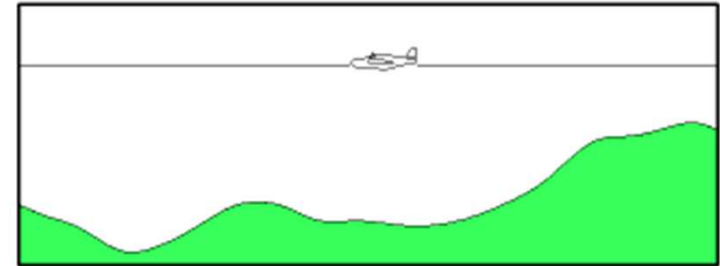
# Essential airborne data preparation (processing)

- Plotting
- Editing
- Drapping

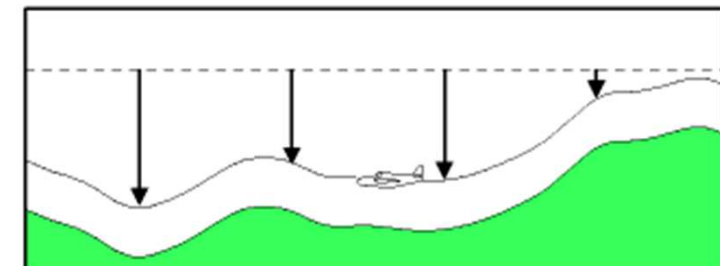
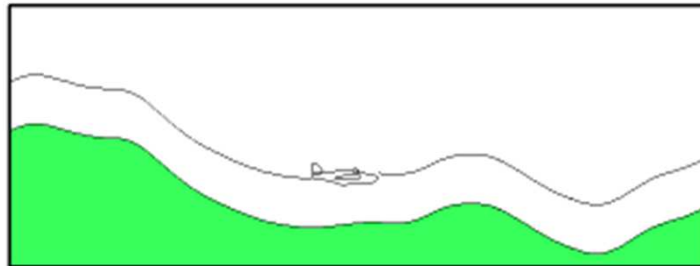
Mean Terrain Clearance  
Hauteur constante



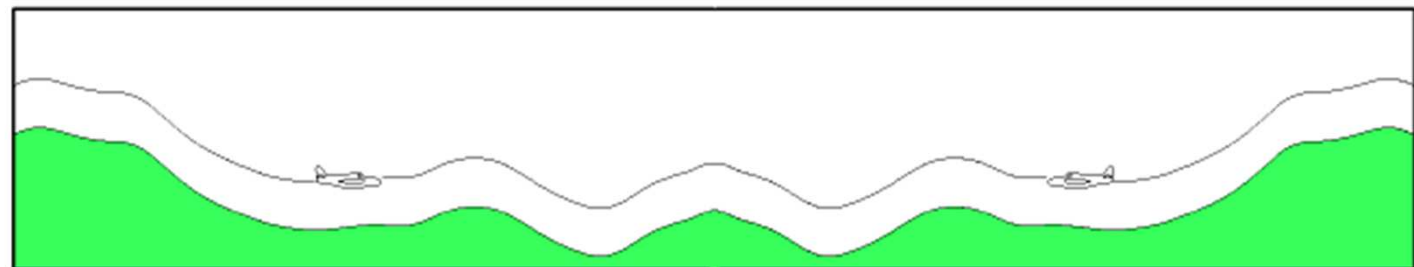
Constant altitude  
Altitude constante



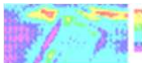
A) Adjacent mean terrain clearance and constant altitude surveys.  
Levés adjacents à hauteur constante et à altitude constante.



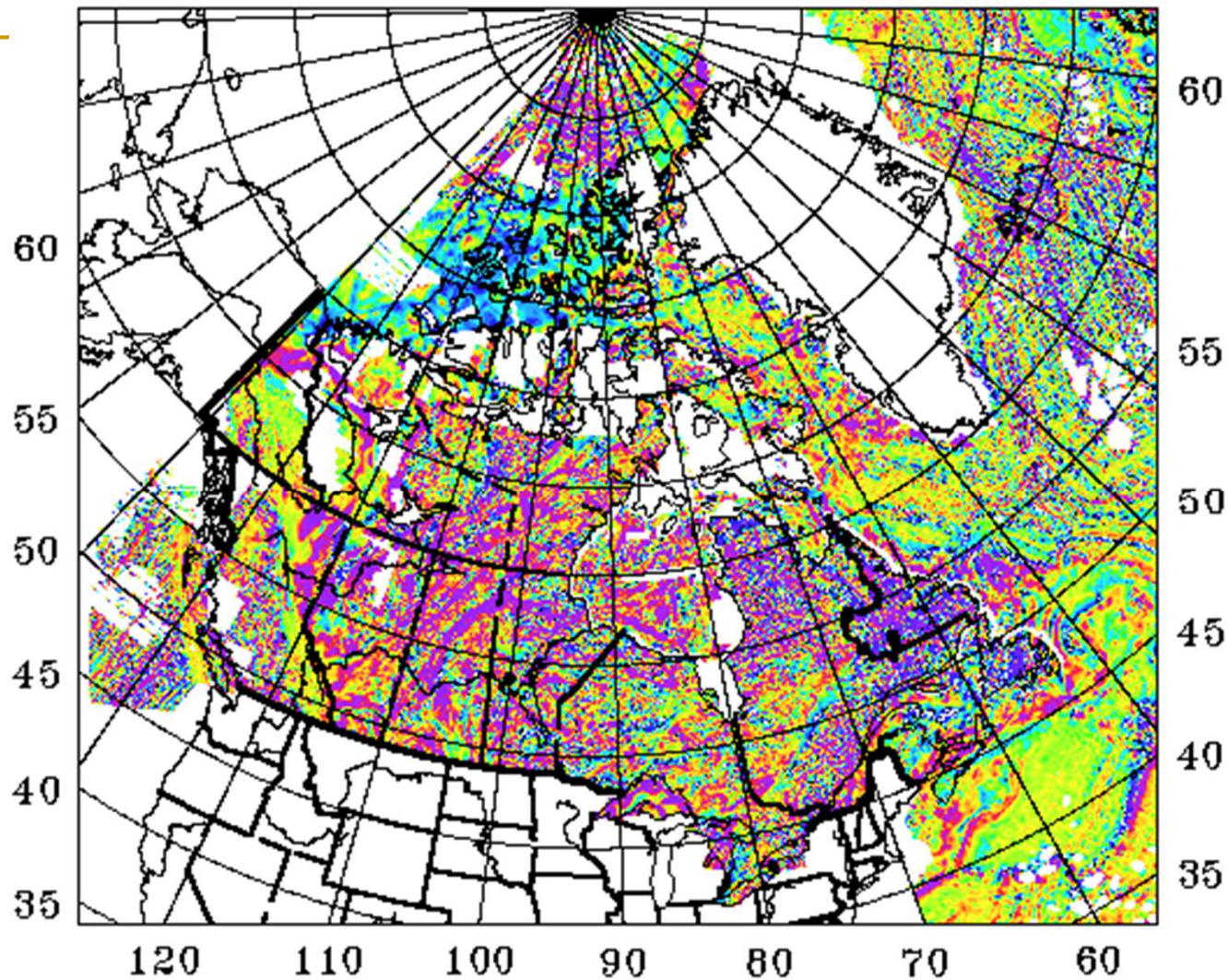
B) Draping of constant altitude survey data to idealized mean terrain clearance flying height.  
Simulation mathématique d'un levé à hauteur constante à partir d'un levé à altitude constante.



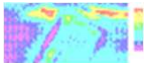
C) Draping the constant altitude survey improves levelling between surveys.  
Ce calcul facilite l'ajustement de levés adjacents.







The entire data set is available as a 200 m grid which is updated annually to reflect recent data acquisition. \$45 from the Canadian government



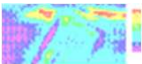
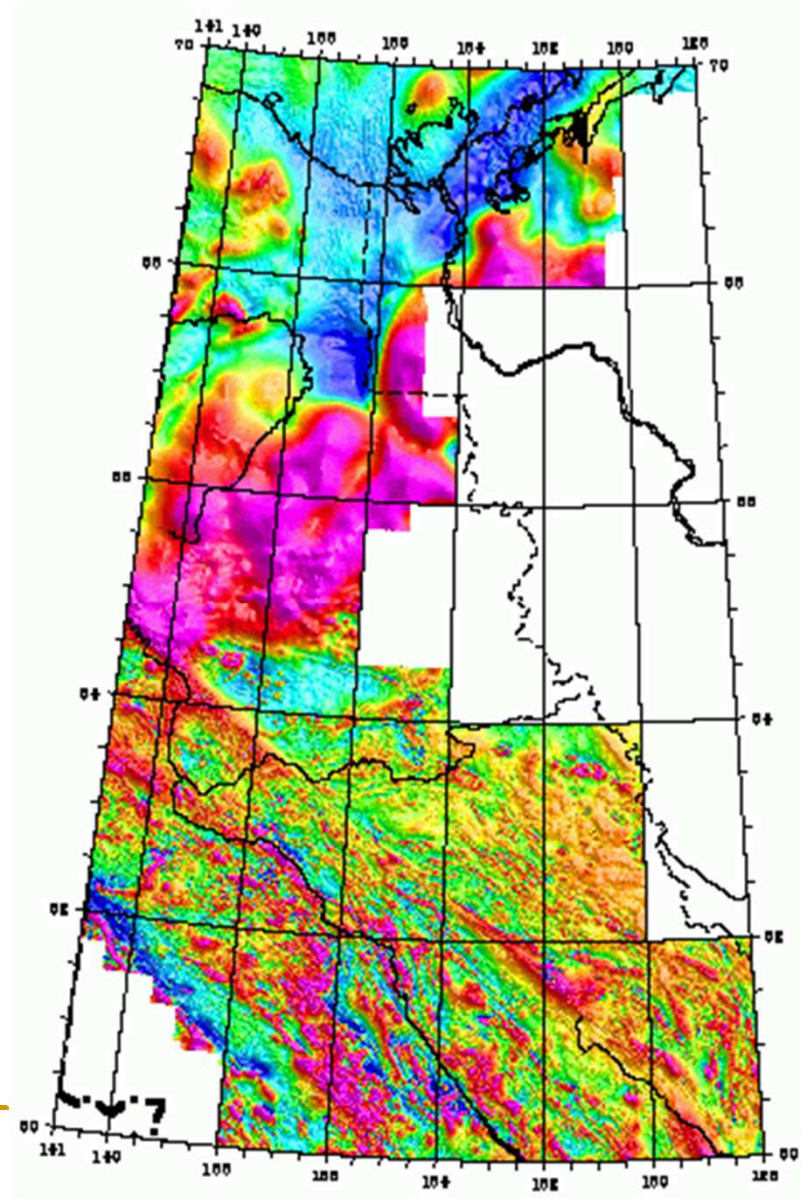


# Essential airborne data preparation (processing)

“Residual total  
magnetic field”

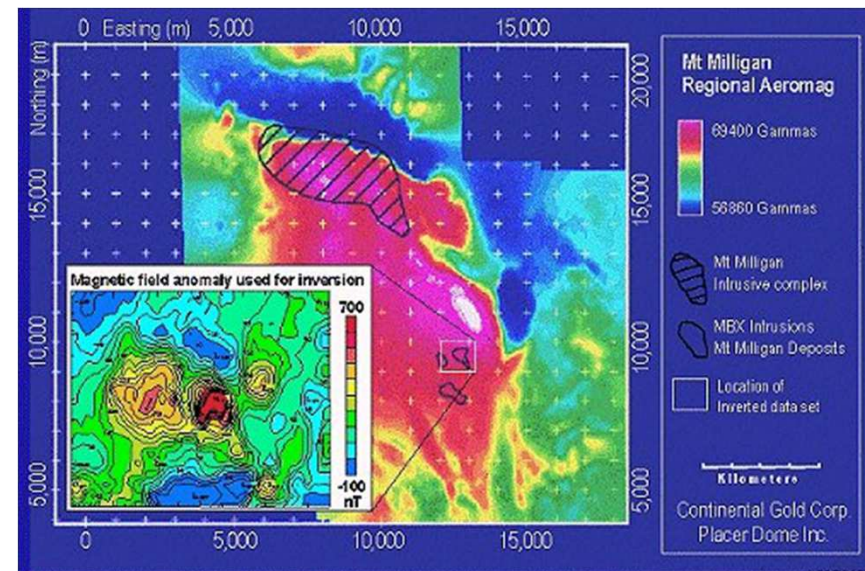
“Reduced to pole”

- What can be learned directly?
  - Trends
  - Contacts
  - Geologic settings

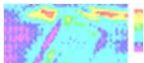
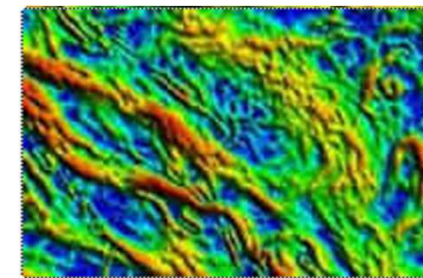


# Processing needed before interpreting

- Required
  - ❑ Temporal correction
  - ❑ Remove regional if present.
  - ❑ Noise suppression
- Optional
  - ❑ Filtering to emphasize edges, other features.
  - ❑ GPG Ch.3.d.6.



Mt Milligan, BC. GPG Ch.6.d.1

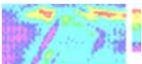
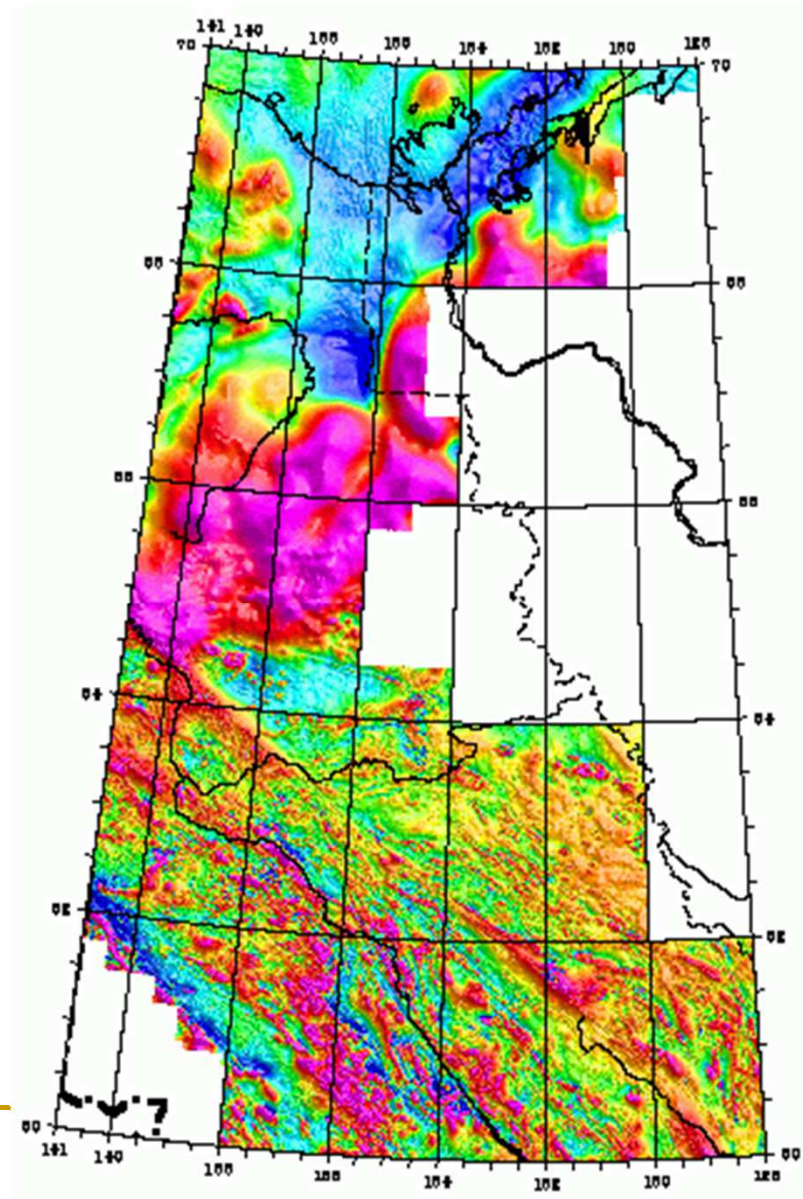


# Essential airborne data preparation (processing)

“Residual total  
magnetic field”

“Reduced to pole”

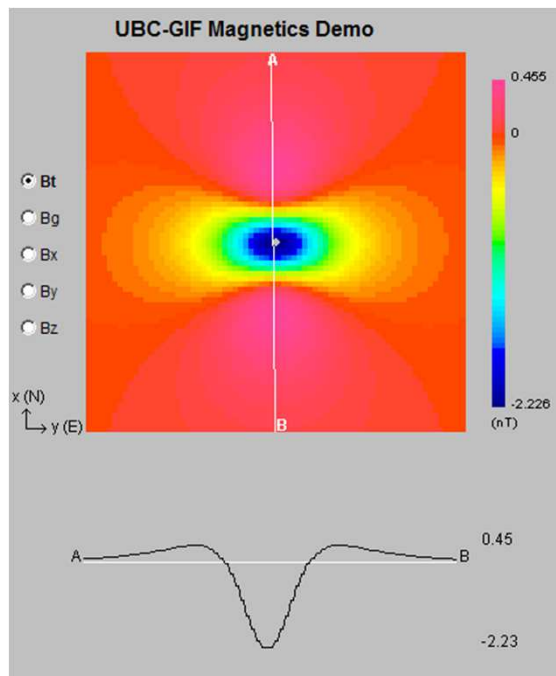
- What can be learned directly?
  - Trends
  - Contacts
  - Geologic settings



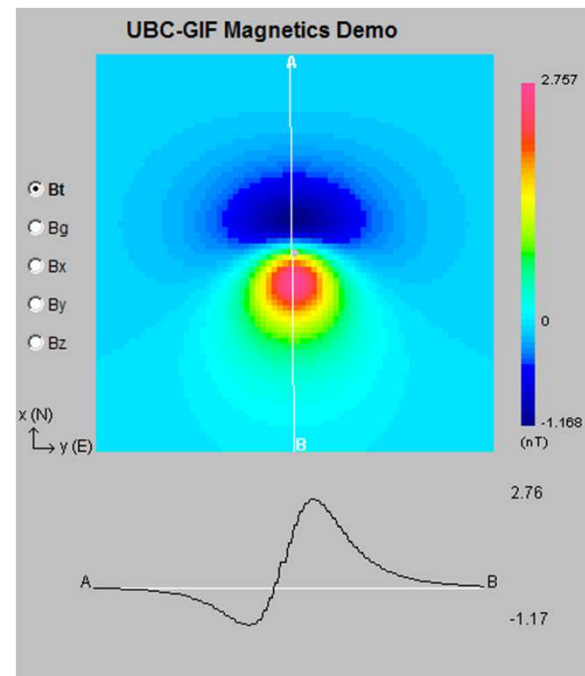


# Reduction to Pole

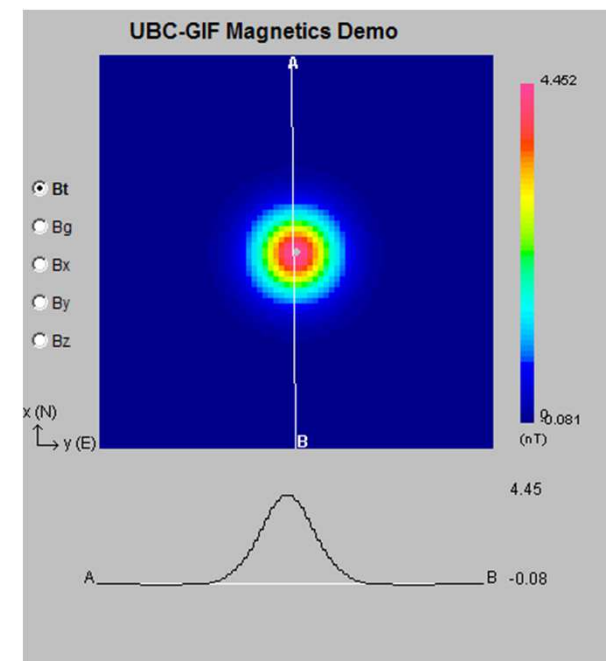
Same object buried at different locations on the earth yields different total field anomalies.



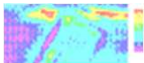
Inclination=0



Inclination=45

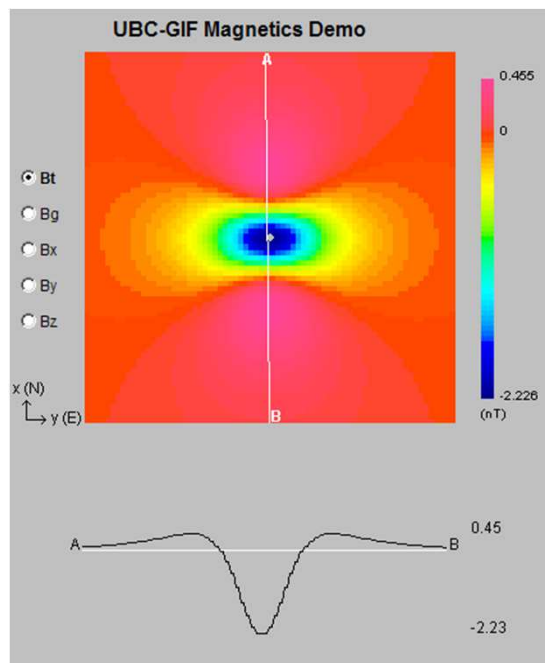


Inclination=90

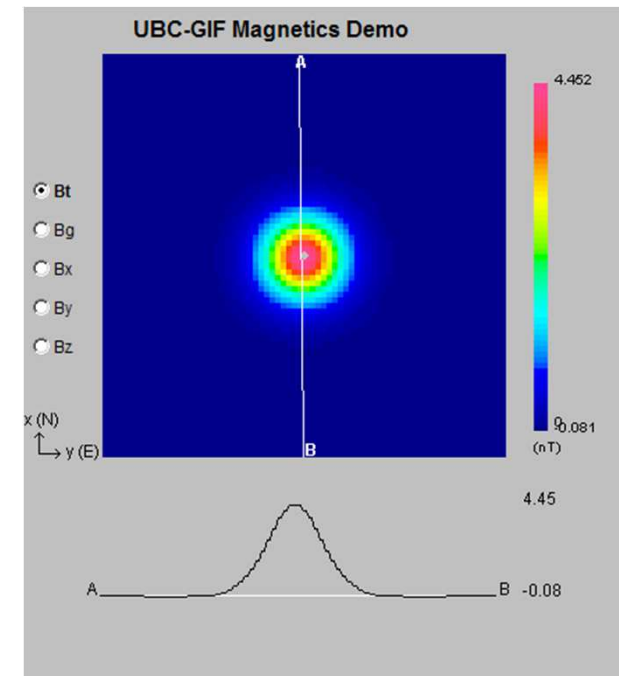


# Reduction to Pole

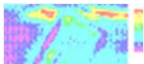
Filter the data to emulate the response as if the survey was taken at the pole. (Earth's field is vertical; measure vertical component of the anomalous field)



2D Fourier Filter



This simplifies interpretation. Causative body lies beneath the peak.



# Magnetics for Geologic Mapping



When rock outcrops are sparse we must rely on other available techniques to denote changes in geologic units and/or structures.



# Magnetic surveys

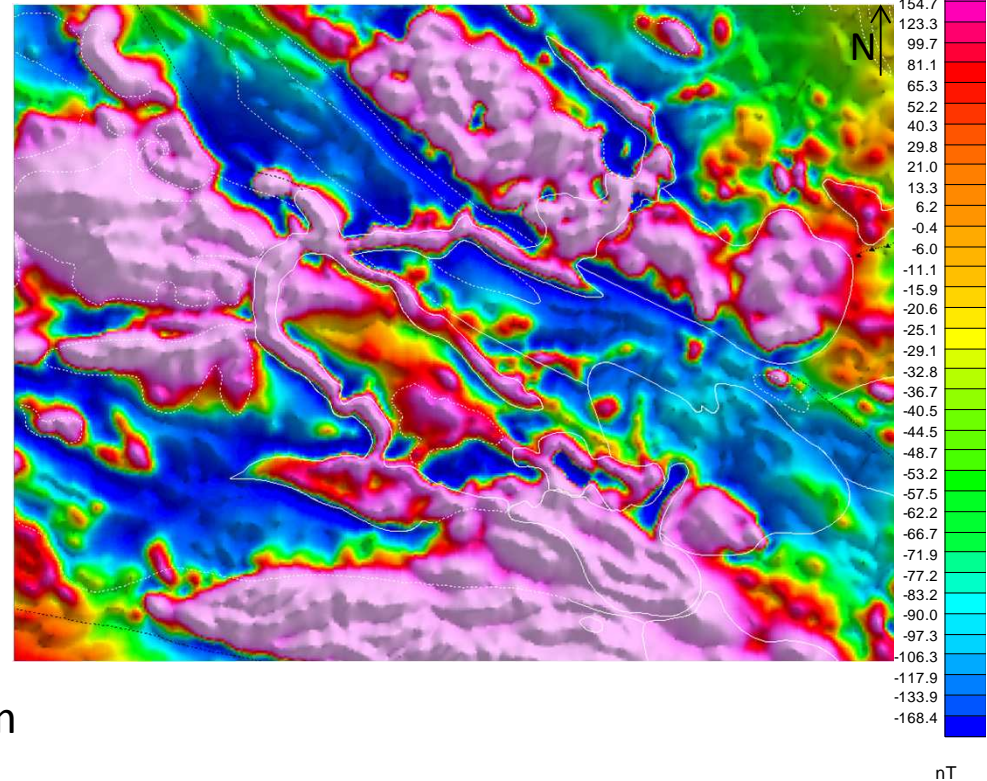
- Very common mineral exploration tool to aid with geologic mapping.
- One of the **cheapest** geophysical surveys to execute on land or with an aircraft.
- Used on regional and deposit scale to identify geologic boundaries and structures (such as faults or folds).
- Many mineral deposits are found on geology boundaries or faults so magnetic maps are useful for target prospective areas.

# Geologic boundaries

Geology map



Magnetic map

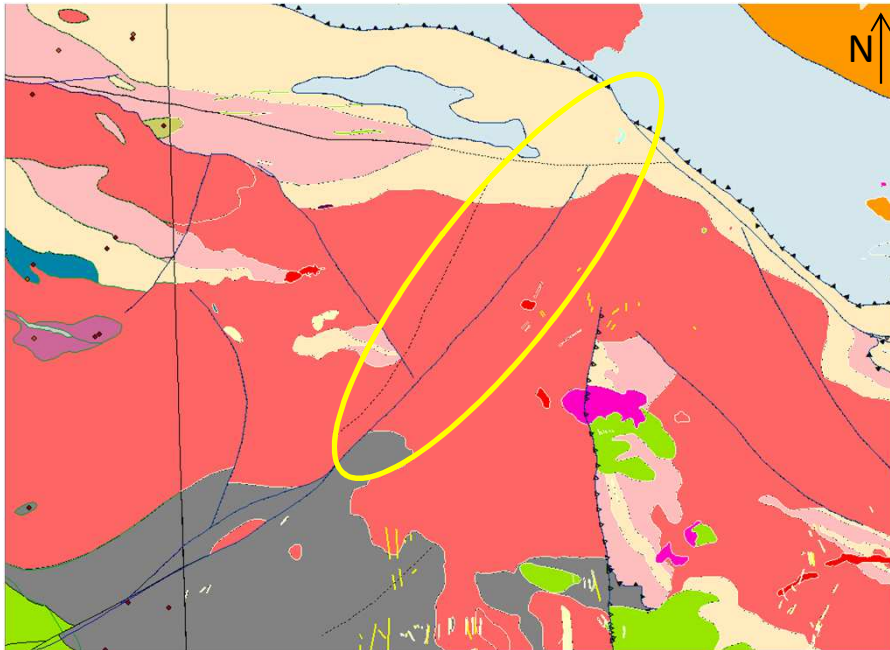


30 km

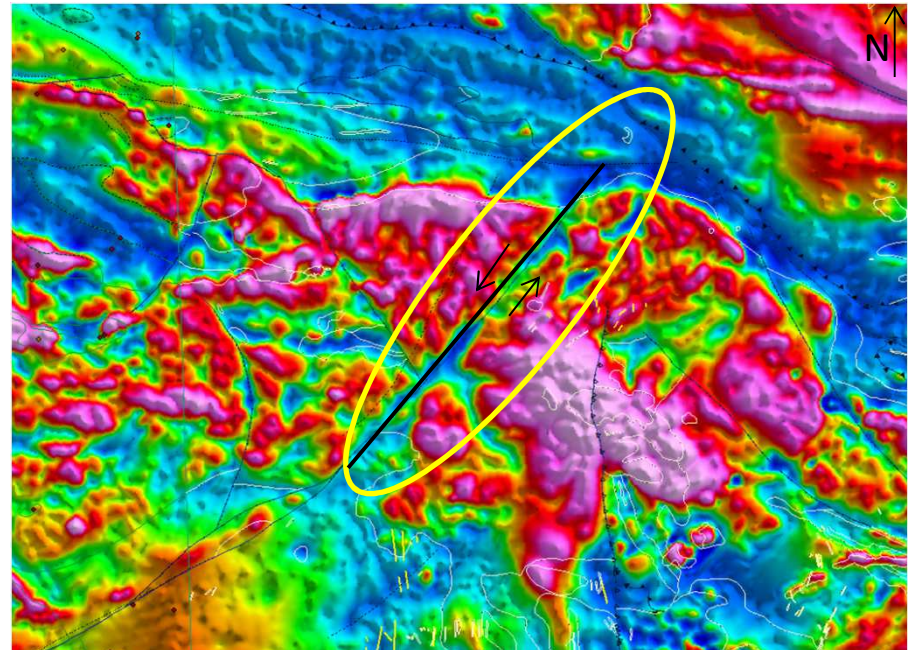
Geology contacts can be inferred from mag maps.

# Identifying regional scale faults

Geology map



Magnetic map

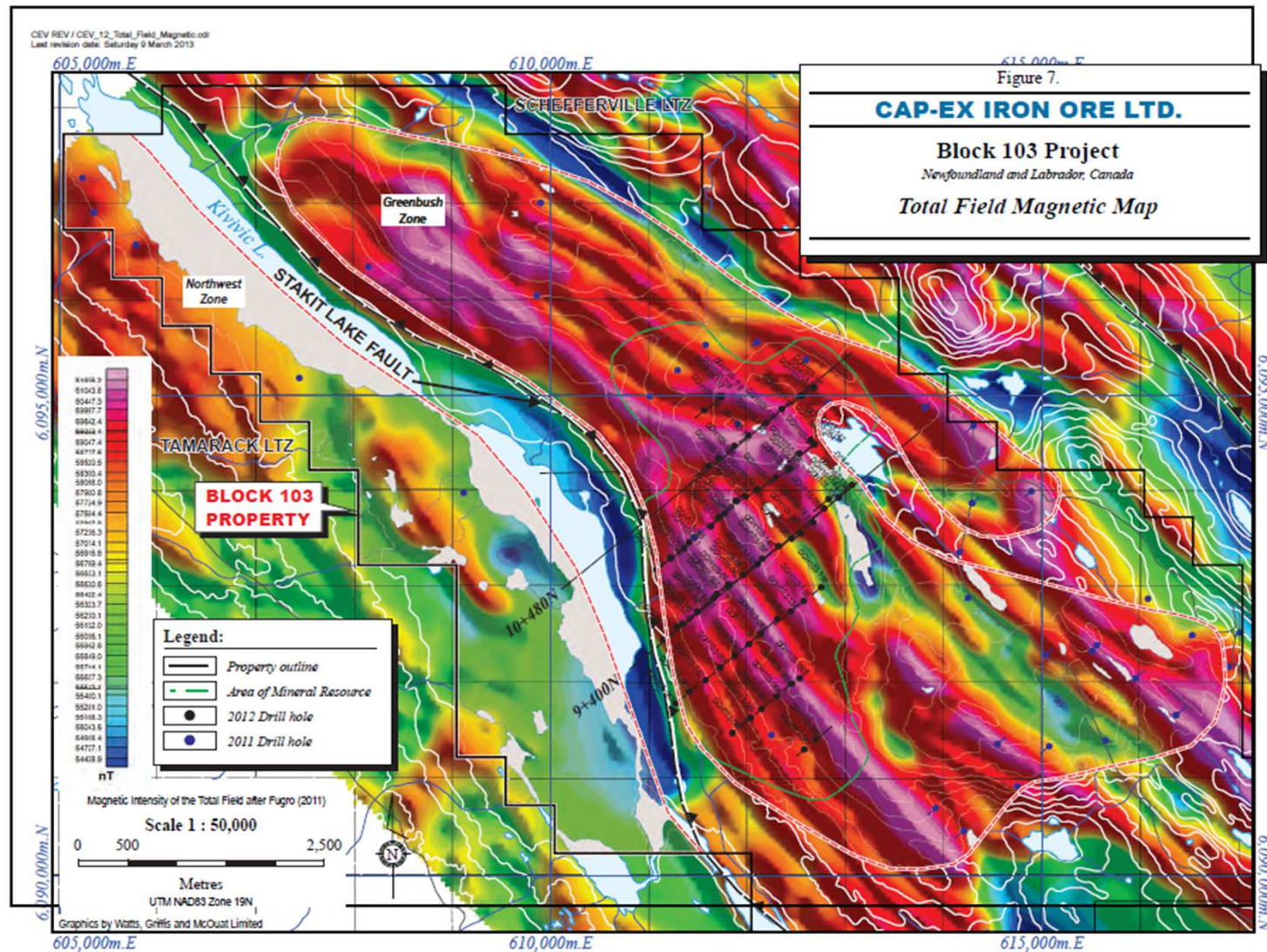


55 km

Mag map highlights faults within known gold bearing plutonic body (red) in west-central Yukon.



# Example - Iron ore deposit

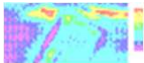


Magnetite rich rock shows as mag high anomaly

---

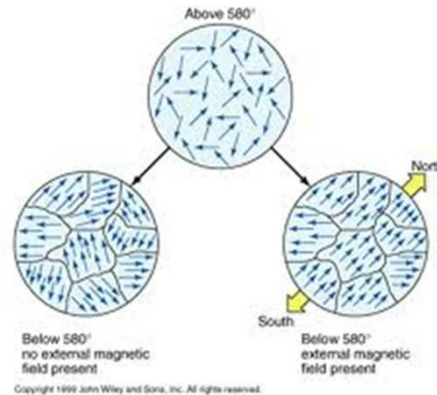
## Possible routes to extracting information

- Plot the data in various map displays
- Interpret with a dipole
- Interpret with simple bodies of uniform magnetization
- Interpret as complex bodies (inversion)

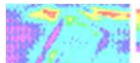


# Remanent Magnetization

- Magnetic material cooling through Curie temperature ( $\sim 550$  C) acquires a magnetic field in the direction of the earth's field.



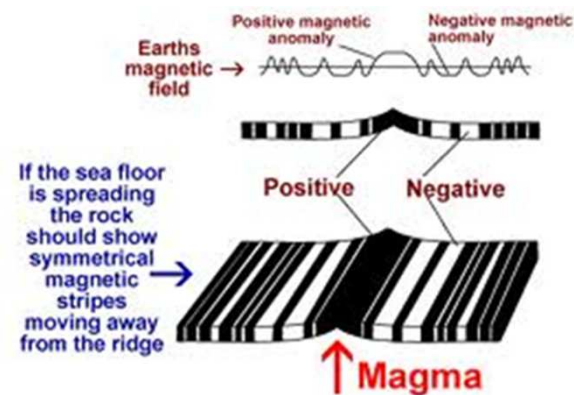
- Final magnetization sum of induced and remanent magnetization:  $\vec{m} = \vec{m}_I + \vec{m}_R$





# Remanent Magnetism at different scales

- Small scale: UXO, rebar, drums
- Large scale: geologic units. Sea floor spreading

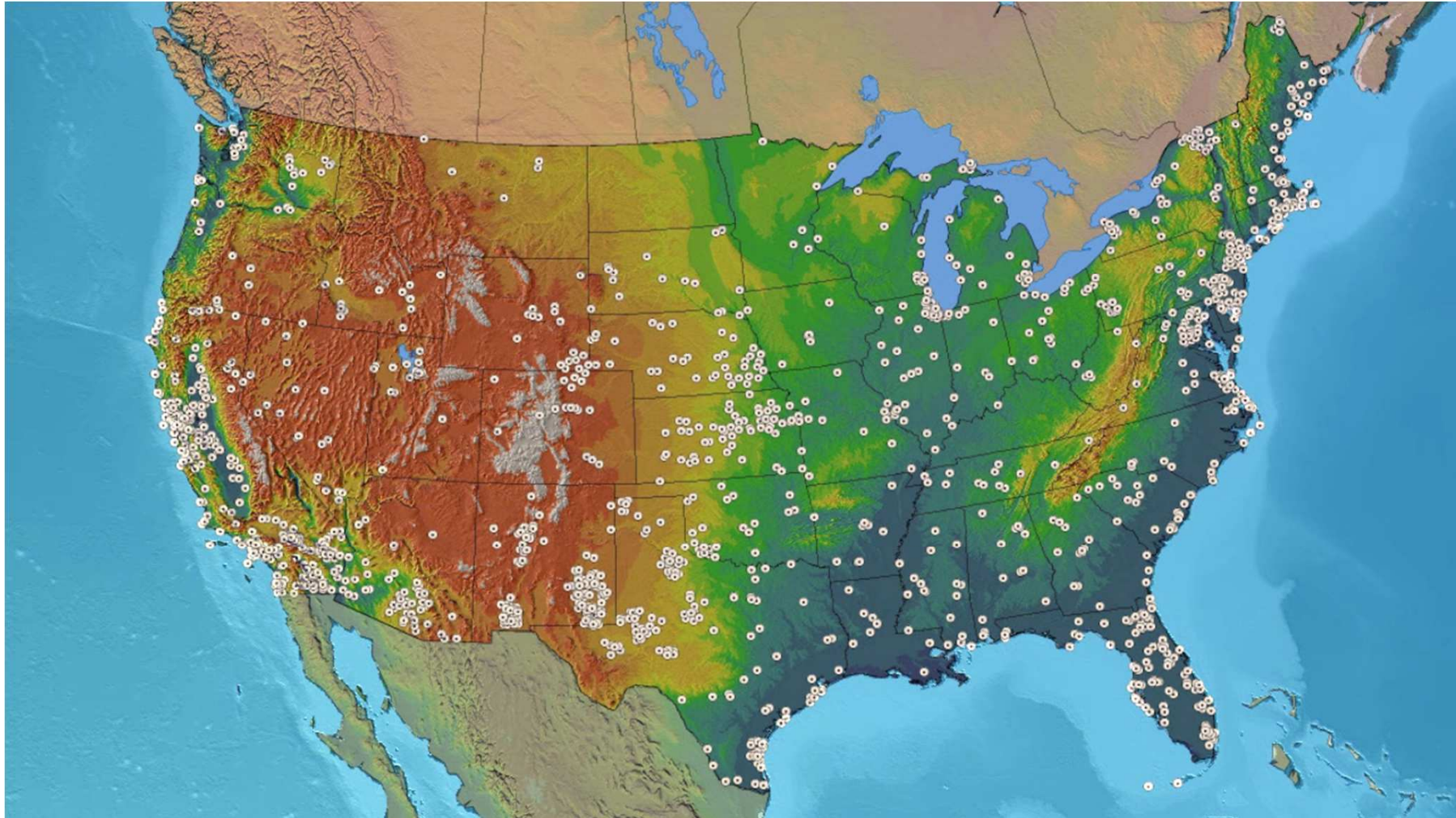




# The Munitions Problem

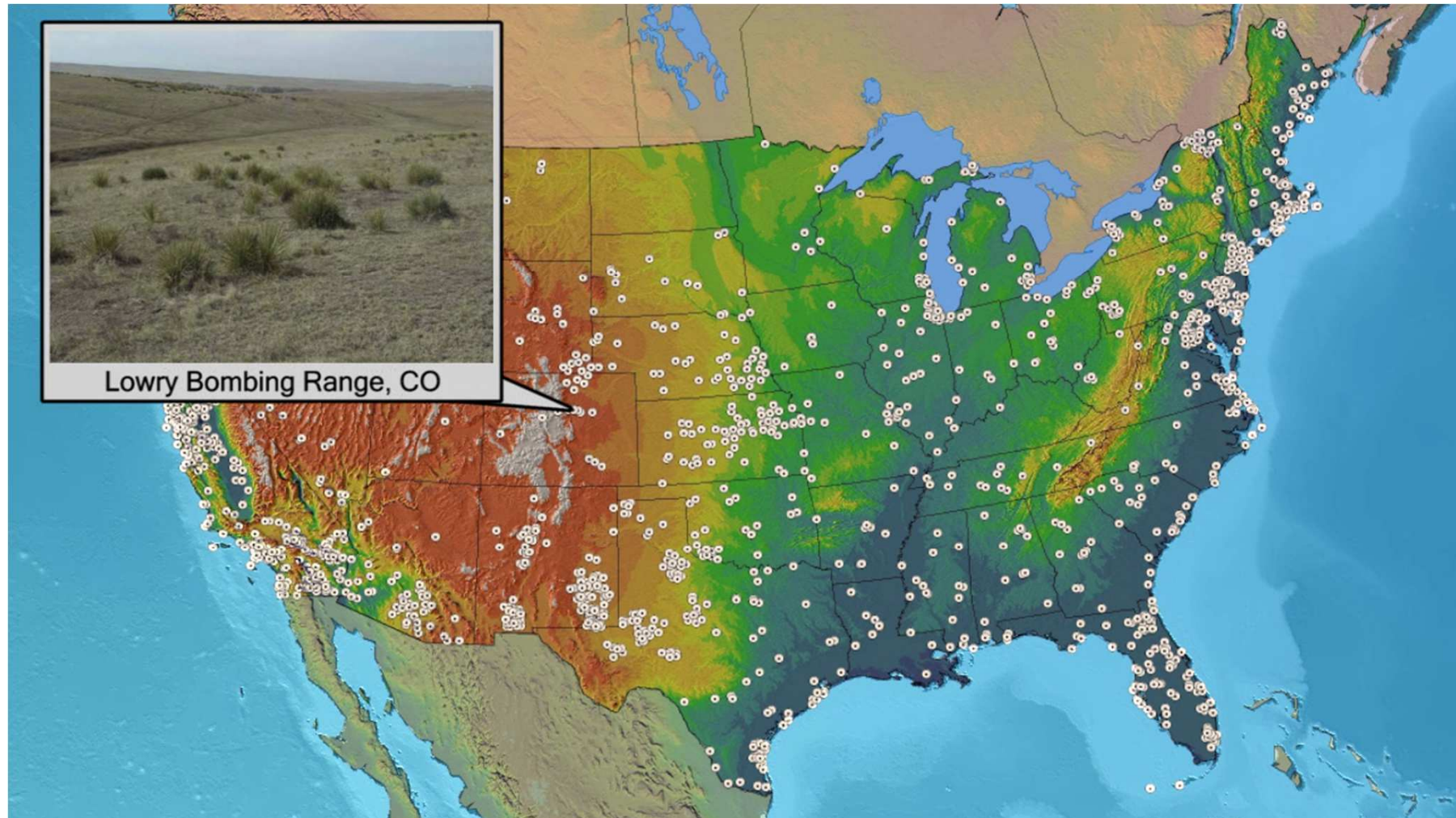
- There are over 3,000 sites suspected of contamination with military munitions
- They comprise 10s of millions of acres
- The current annual cleanup effort is on the order of 1% of the projected total cost
- To make real progress on this problem, we need a better approach

# The Munitions Problem



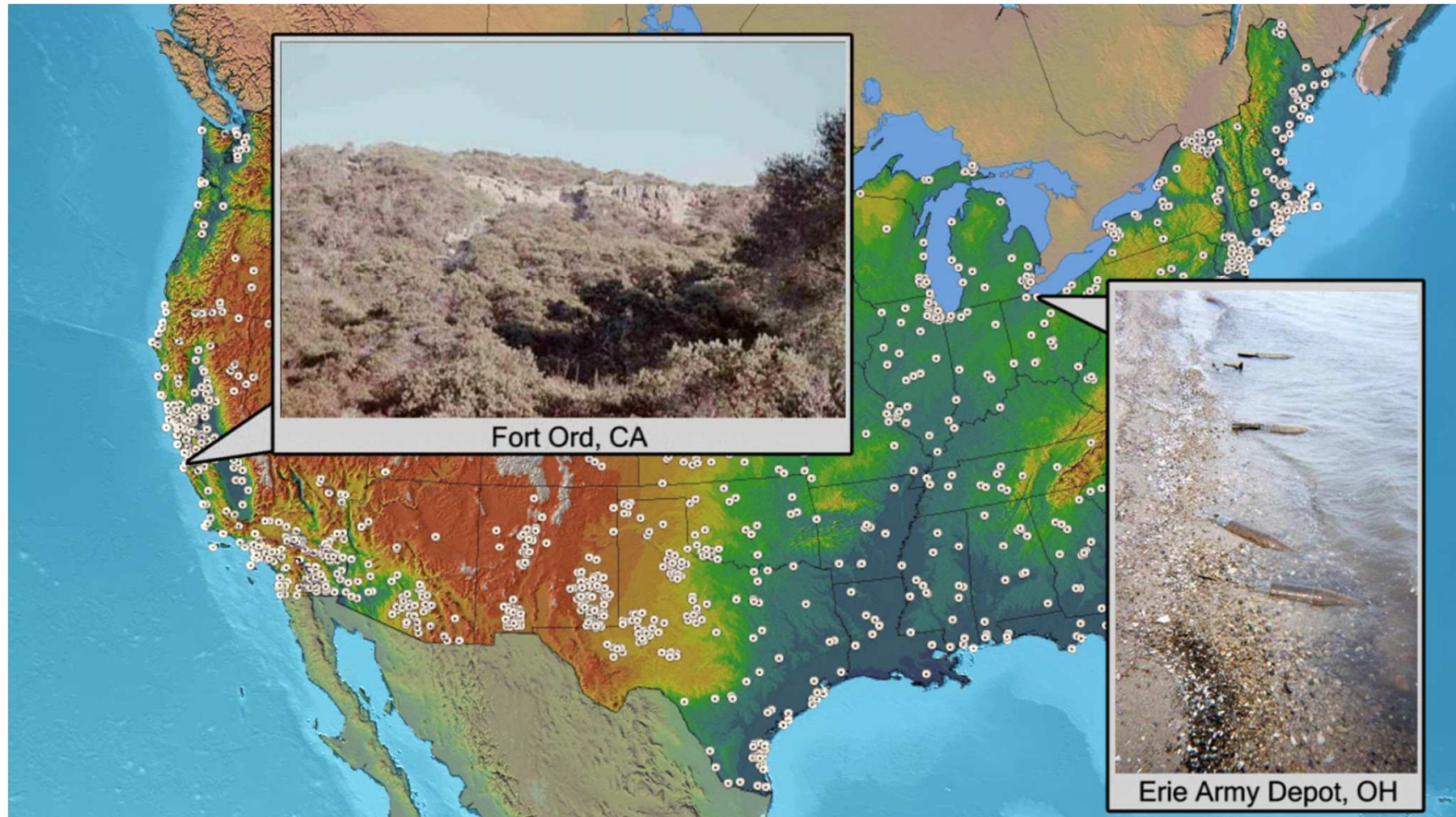


# The Munitions Problem



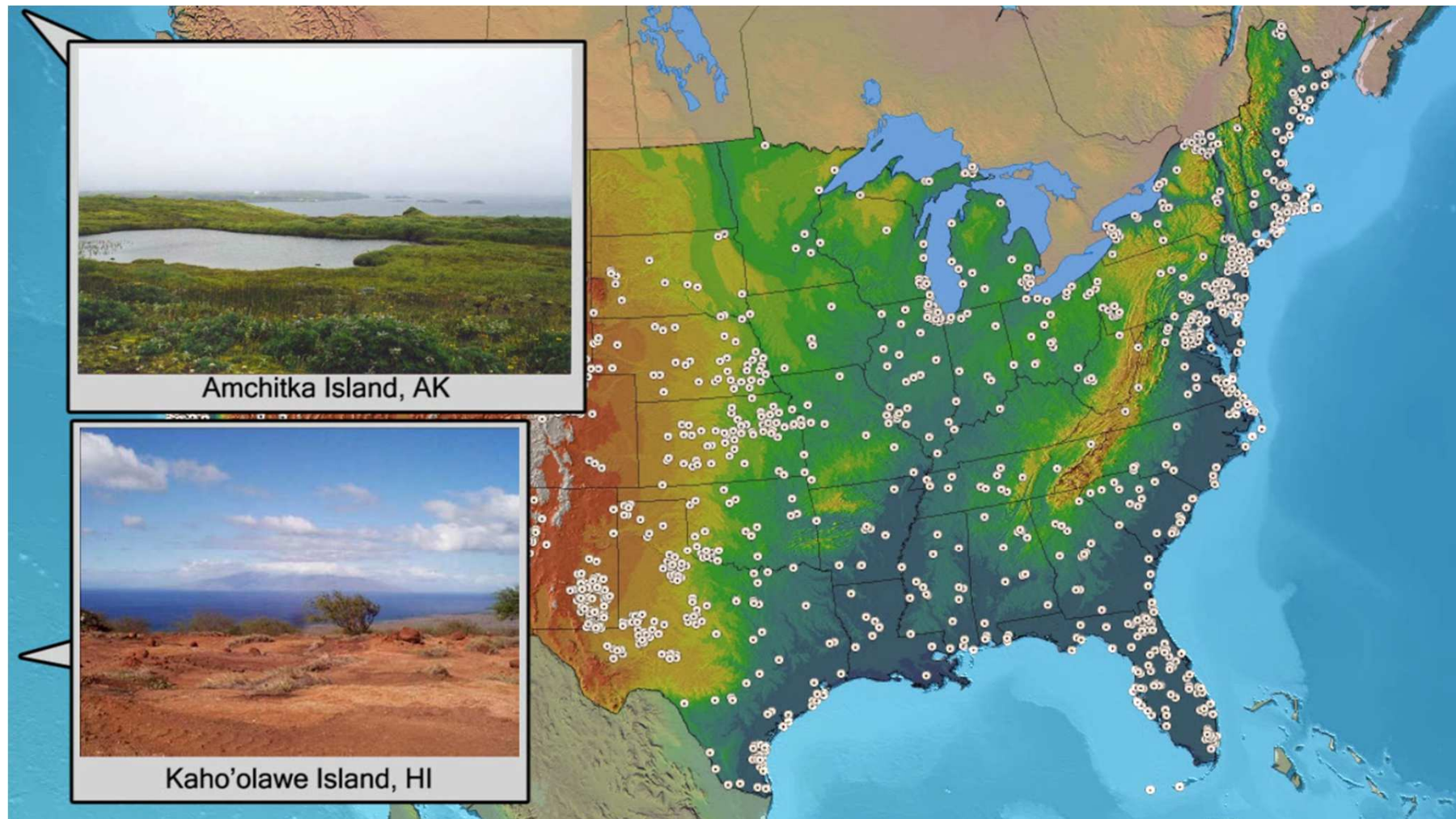


# The Munitions Problem



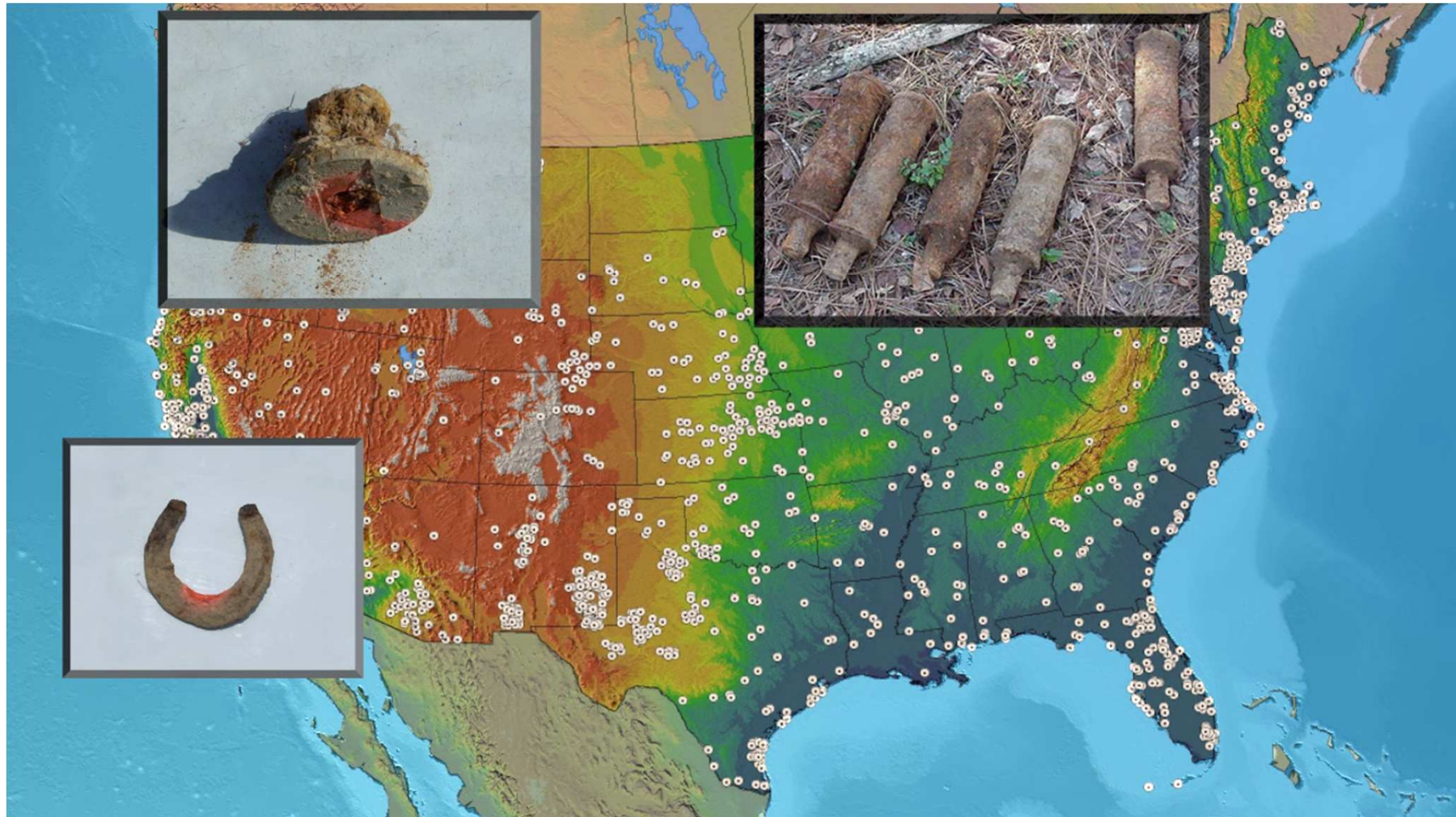


# The Munitions Problem

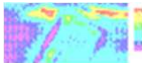




# The Munitions Problem



# Environmental: How do we find UXO?

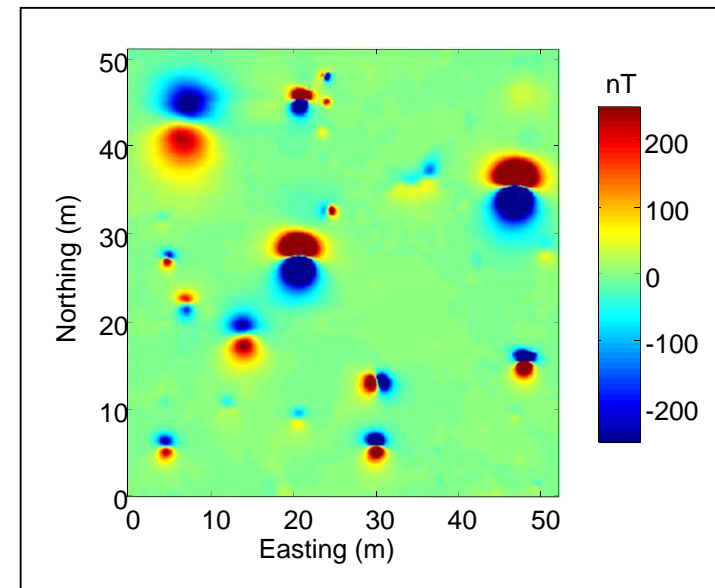




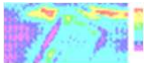
# Environmental : Magnetic Survey



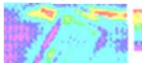
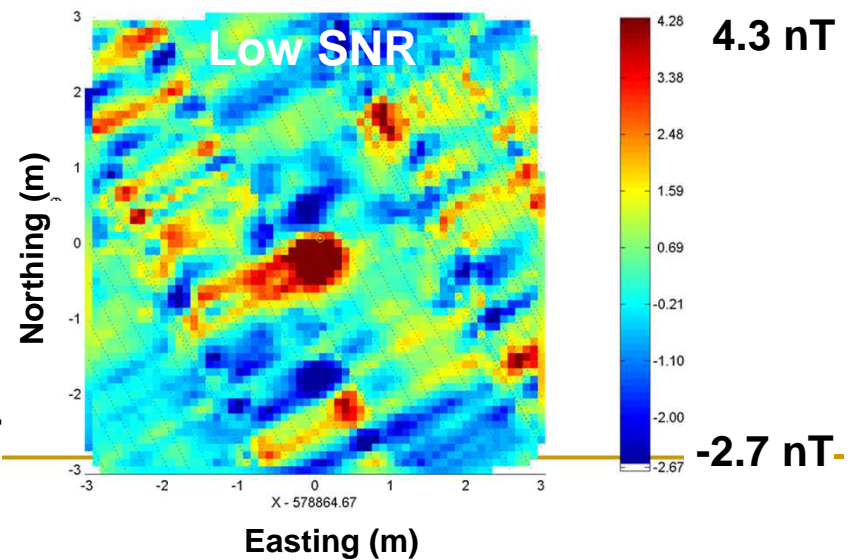
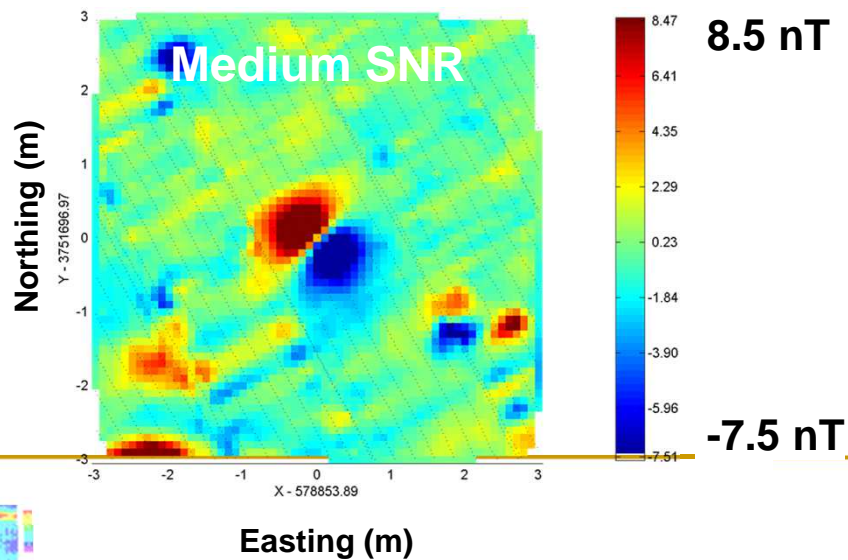
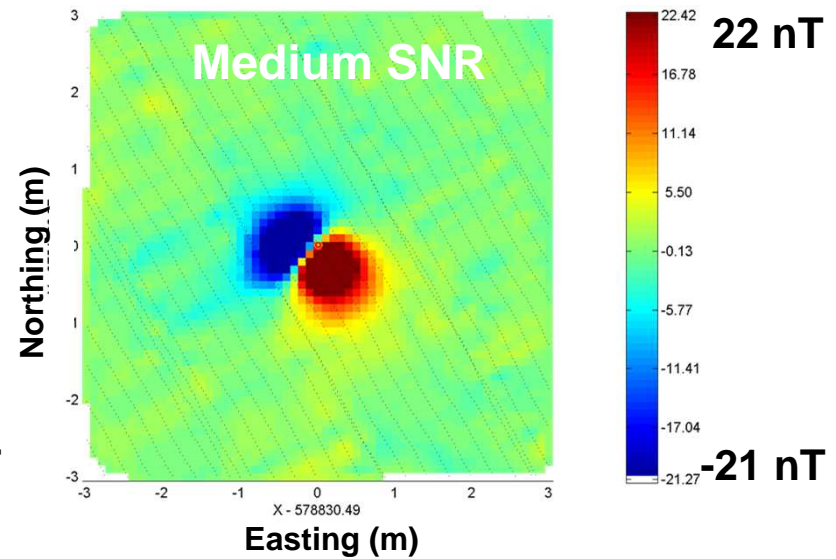
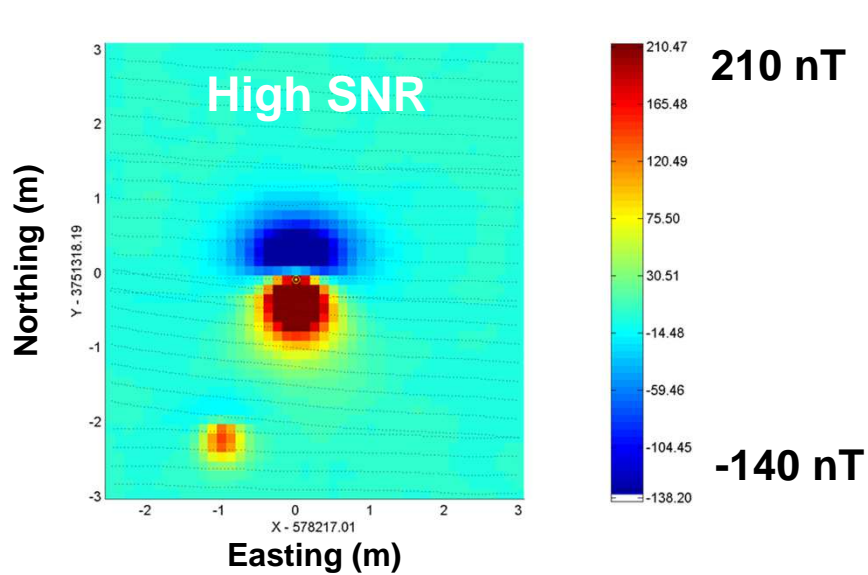
Ferrex



TM4



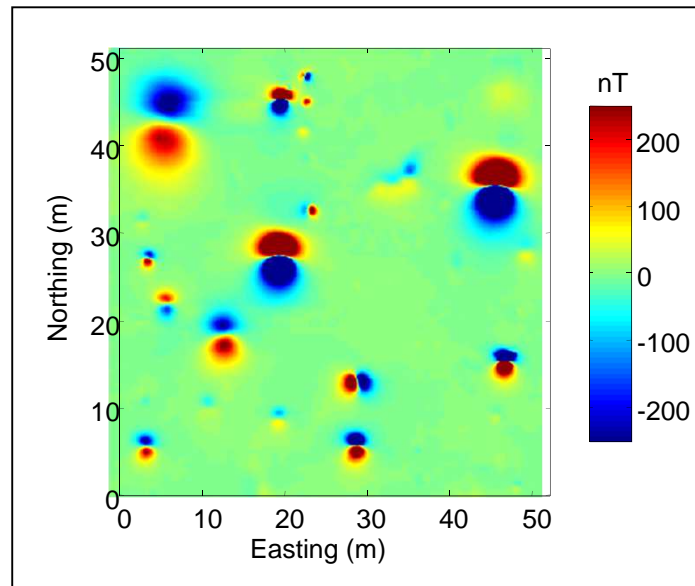
# Examples of “good” data





# What is the formula for a magnetic dipole

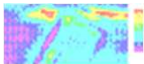
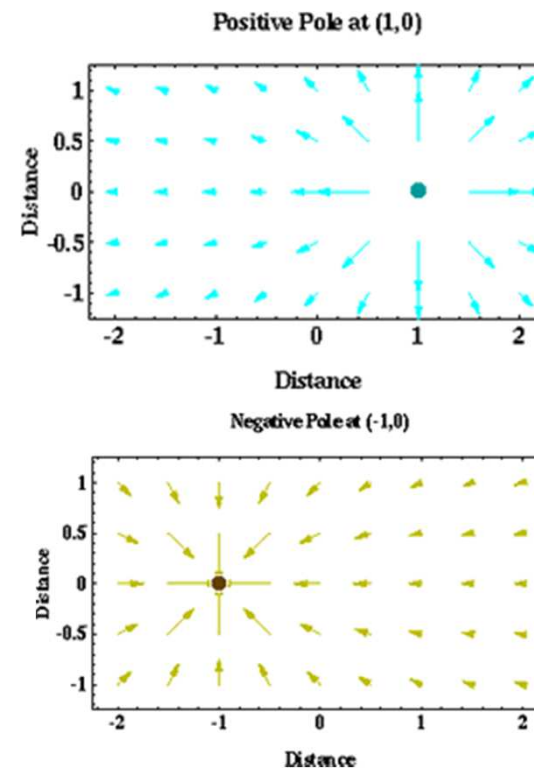
- These look like dipoles but how do we analyze the signal?



# Magnetic Charges (or Poles) (GPG d3 & d8)

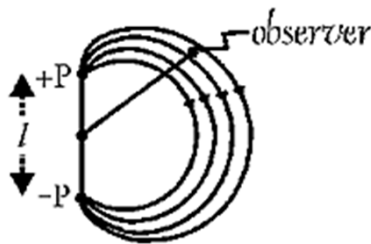
- A magnetic charge creates a magnetic field  $\vec{H}$

$$\vec{H} = \frac{\vec{F}}{Q_b} = \frac{Q_a}{4\pi\mu_0 r^2} \hat{r}$$



# Magnetic Charges (or Poles)

In nature: magnetic poles always appear in pairs with a positive and negative pole yielding a dipole.



$$\vec{H} = \frac{P}{4\pi\mu_0} \left( \frac{\hat{r}_1}{r_1^2} - \frac{\hat{r}_2}{r_2^2} \right)$$

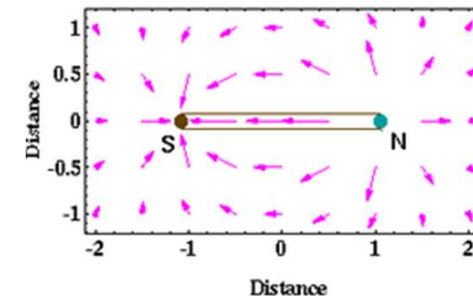
Magnetic moment

$$\mathbf{m} = \frac{Pl}{\mu_0}$$

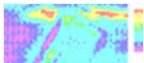
Magnetic field  
of dipole

$$\vec{H} = \frac{\mathbf{m}}{4\pi r^3} (2 \cos \theta \hat{r} + \sin \theta \hat{\theta})$$

Field Due to a Dipolar Source



Magnetic field of dipole  
decays as  $1/r^3$ .



---

# Magnetics

## Magnetics fundamentals

Sensor systems  
Data examples and demo



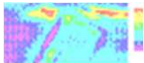
## Parameter extraction

Concepts  
Real-world examples



## Classification

Using the parameters to make  
discrimination decisions



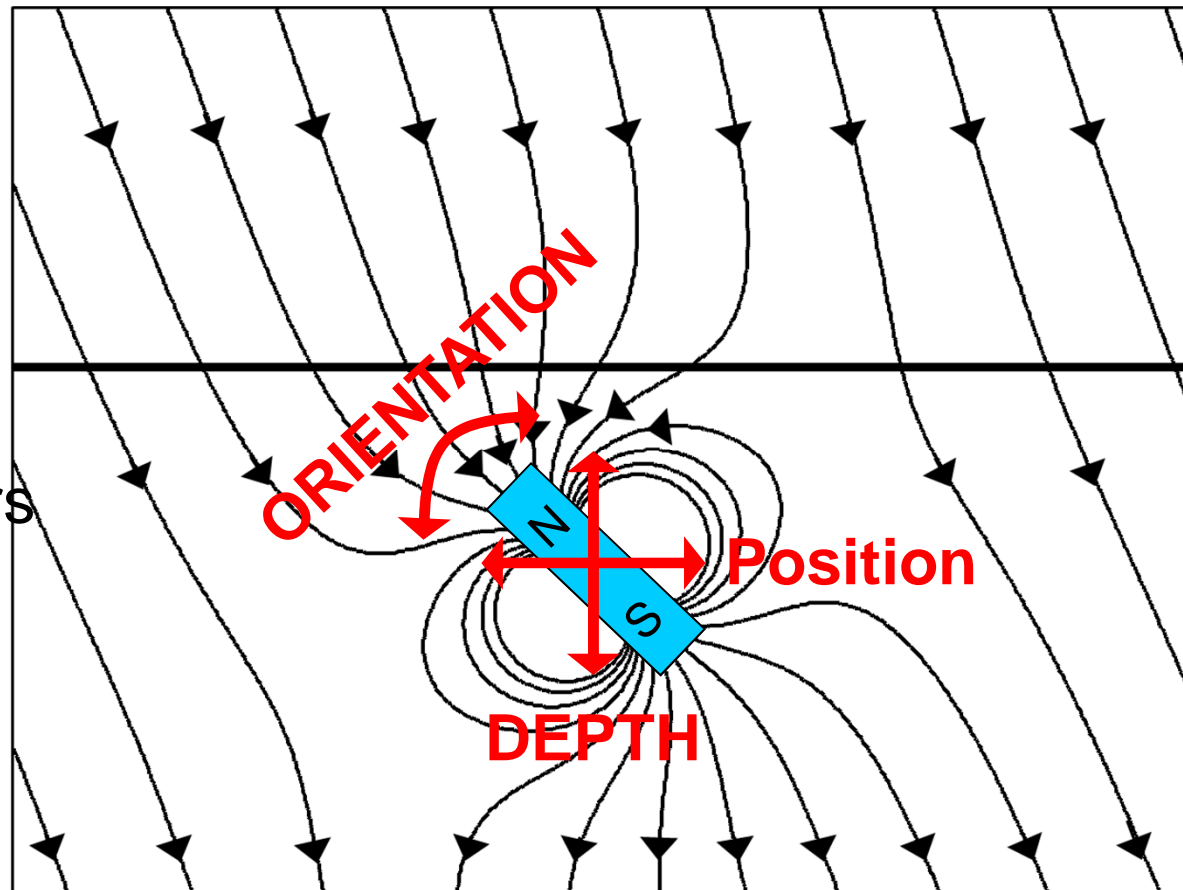




# The model

- We model the response of buried items by a dipole (equivalent to a bar-magnet):

- ☐ Position
- ☐ Depth
- ☐ Orientation
- ☐ Size
- ☐ 6 parameters



# Parameter extraction

- Need six parameters (location, strength and orientation)

$$\vec{H} = \frac{m}{4\pi r^3} (2 \cos \theta \hat{r} + \sin \theta \hat{\theta})$$

- Inversion or “parameter extraction” is used to estimate the parameters of an underlying model that encapsulates some useful attributes of the buried object

**Model Parameters:  $m$**



**Forward Operator**

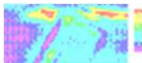
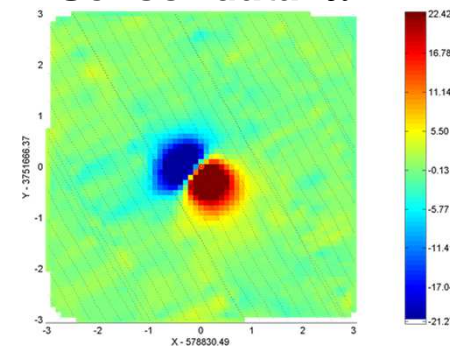
$$d = g[m]$$



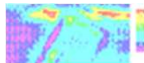
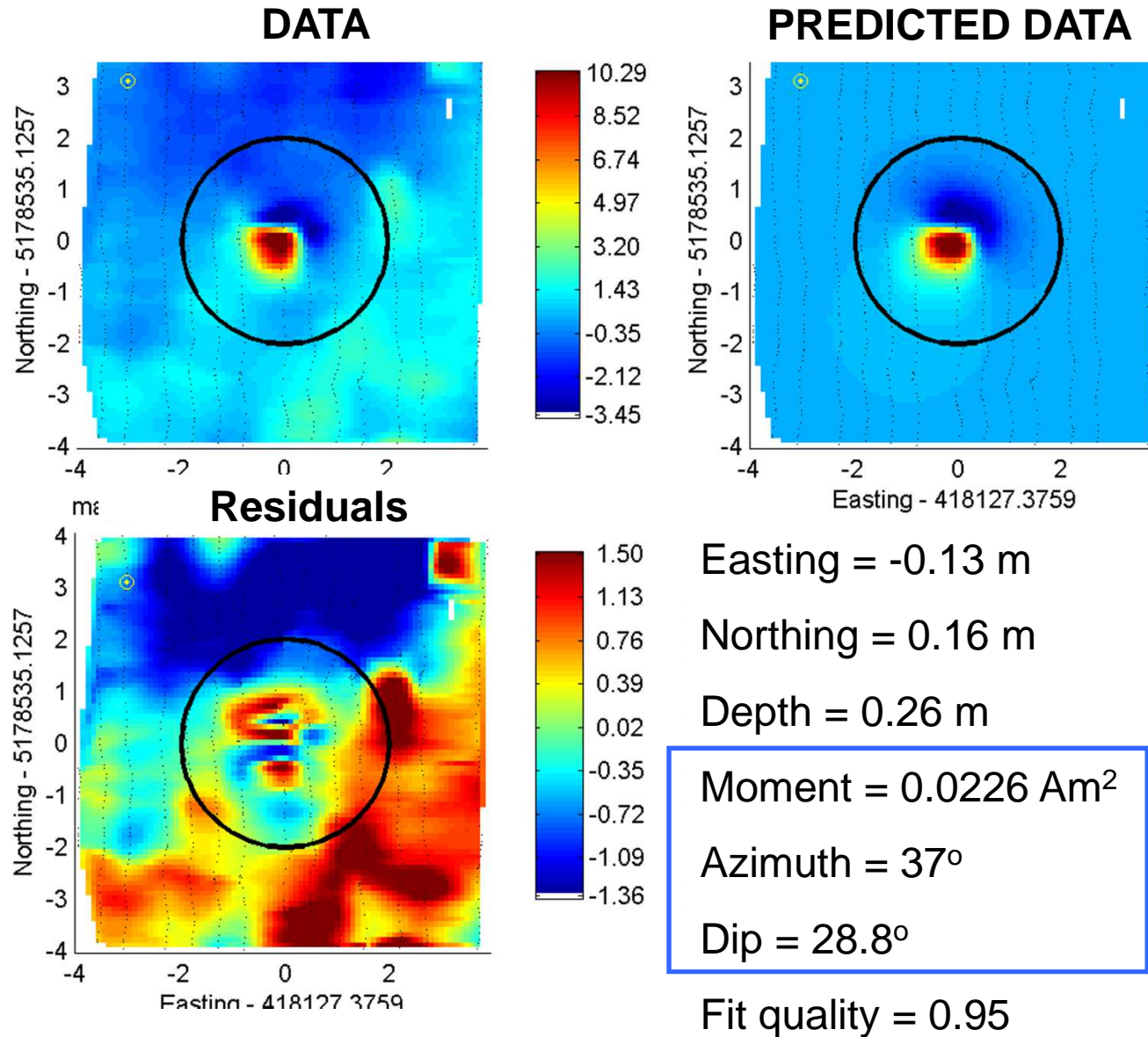
$$m = g^{-1}[d]$$

**Inverse Operator**

**Sensor data:  $d$**



# Parameter extraction

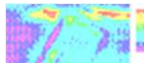
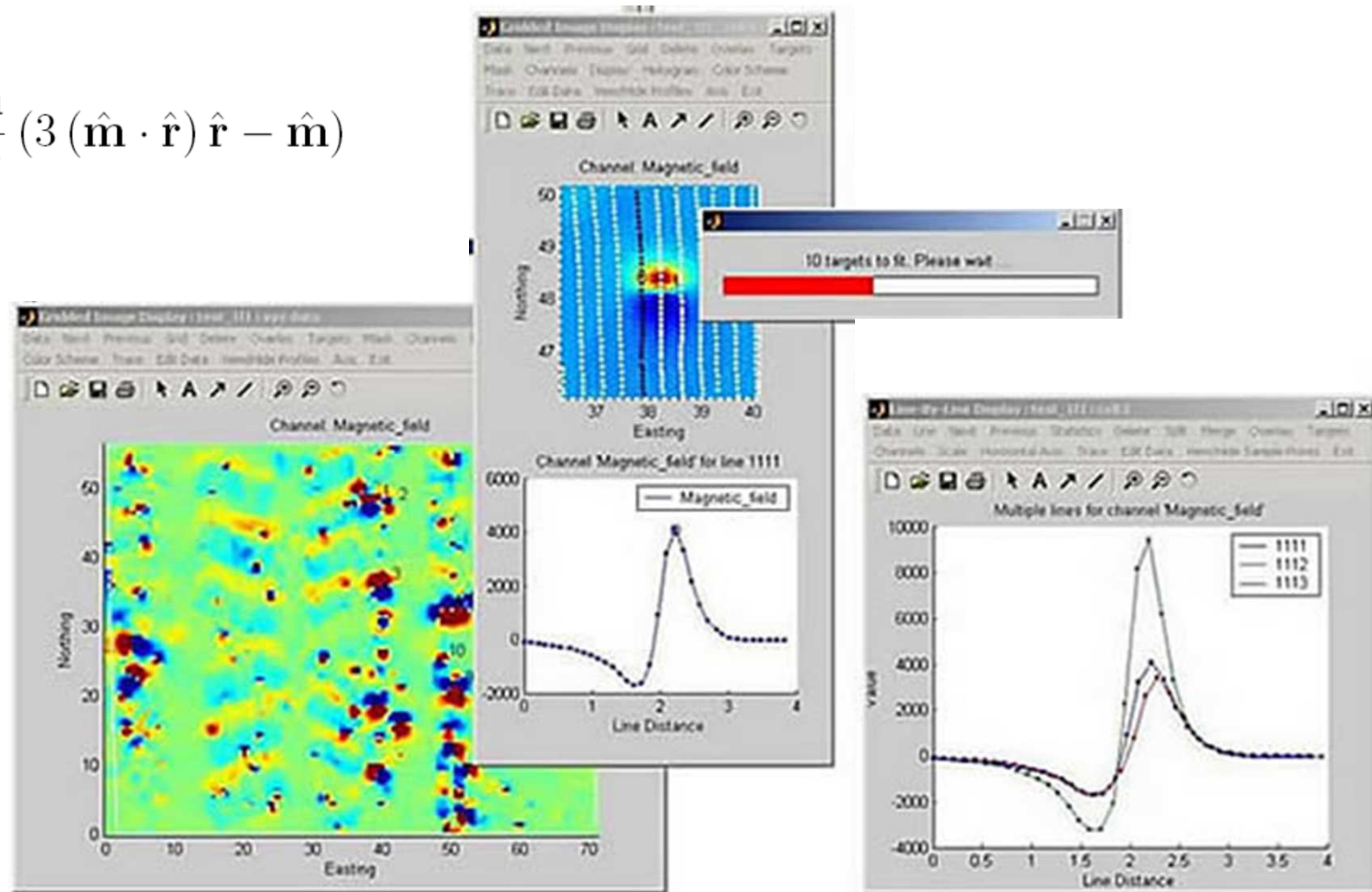


# Eg of “dipoles” UXO data



The Unexploded  
Ordnance and Landmine  
Research Group

$$\mathbf{B} = \frac{\mu_0}{4\pi} \frac{\mathbf{m}}{r^3} (3(\hat{\mathbf{m}} \cdot \hat{\mathbf{r}}) \hat{\mathbf{r}} - \hat{\mathbf{m}})$$

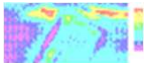




---

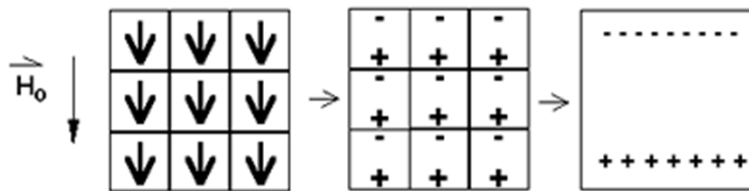
## Possible routes to extracting information

- Plot the data in various map displays
- Interpret with a dipole
- Interpret with simple bodies of uniform magnetization
- Interpret as complex bodies (inversion)

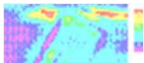
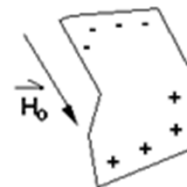
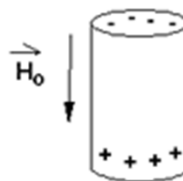


# Beyond dipoles – real targets

- When is a buried feature like a simple dipole?
  - When it's diameter is much less than depth to it's centre.
  - GPG Ch.3.d.3. Ch.3.d.4 . Ch.3.d.5.
- Fields from some buried bodies, (cylinders, dykes) can be estimated by using charge concepts.

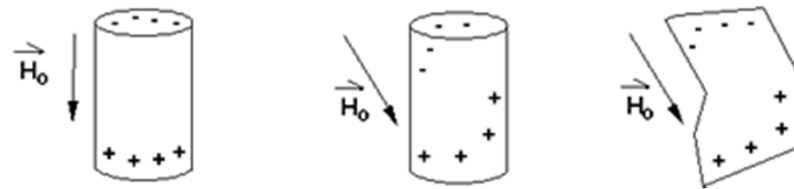


$$\text{Charge strength} = \vec{M} \bullet \hat{n}$$

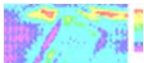
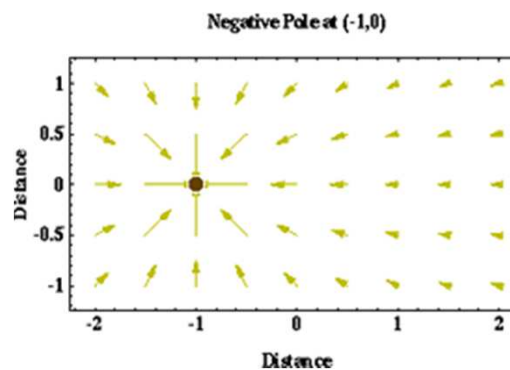


# A simple model for a vertical pipe

- Fields from some buried bodies, (cylinders, dykes) can be estimated by using charge concepts.

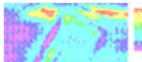
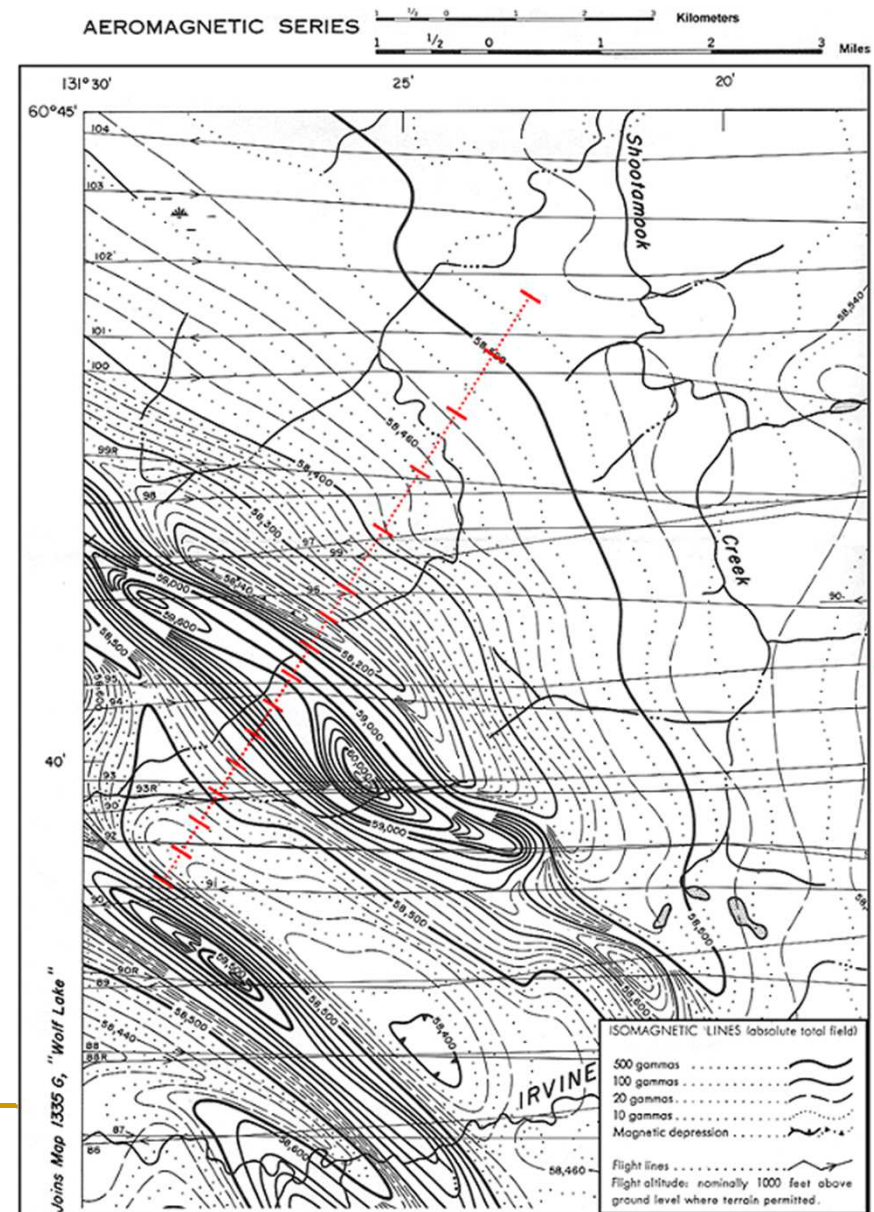


- A vertical pipe has anomaly like a single pole.(TBL 2)



# Magnetics Interpretation – 2D modelling

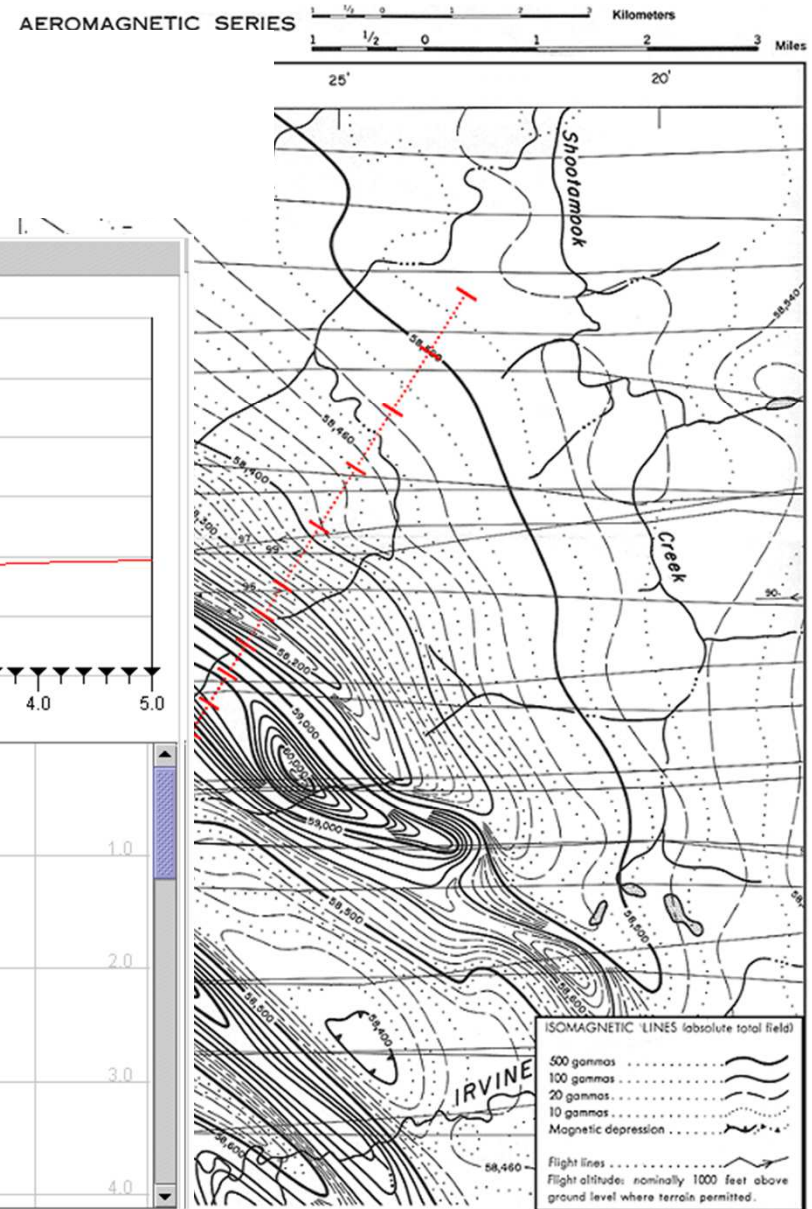
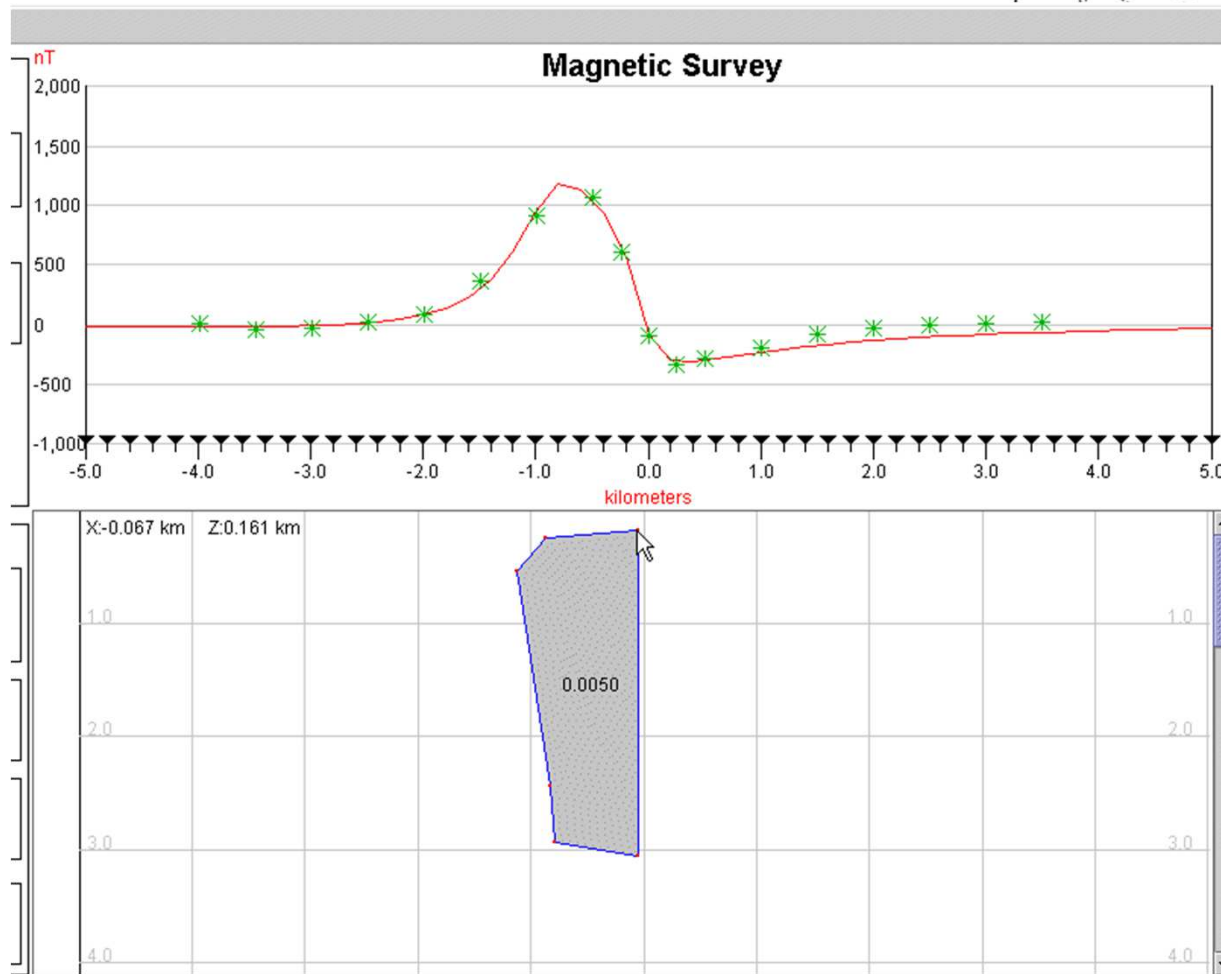
- Forward modelling
  - Line profiles might indicate 2D structure
- First identify the feature of interest
- Analyse data perpendicular to the structure
- Forward model in 2D





## Interpretation using Forward modelling:

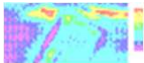
- Response depends on  $\kappa$  and size / shape.
- Solution is non-unique



---

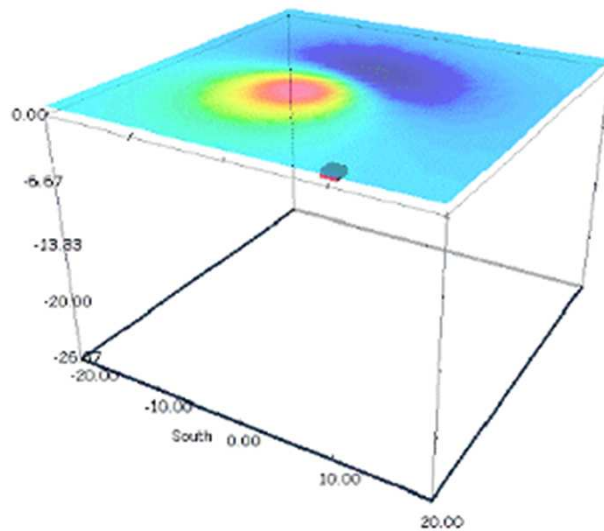
## Possible routes to extracting information

- Plot the data in various map displays
- Interpret with a dipole
- Interpret with simple bodies of uniform magnetization
- Interpret as complex bodies (inversion)

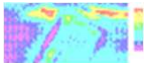
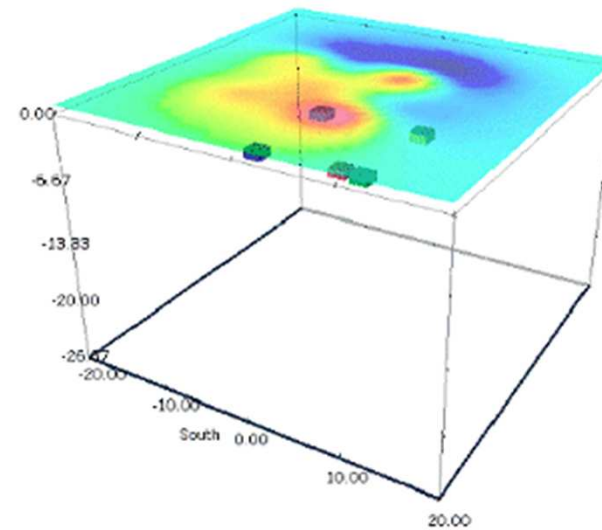


# Superposition for Magnetics Data (GPG d5)

Magnetic field for one prism

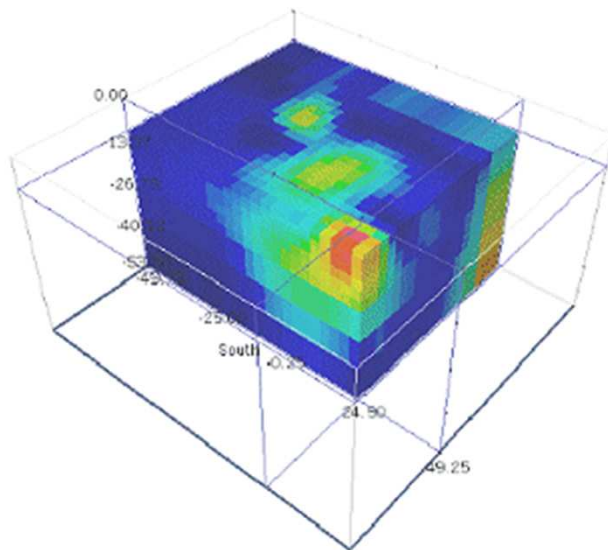


Magnetic field for 5 prisms

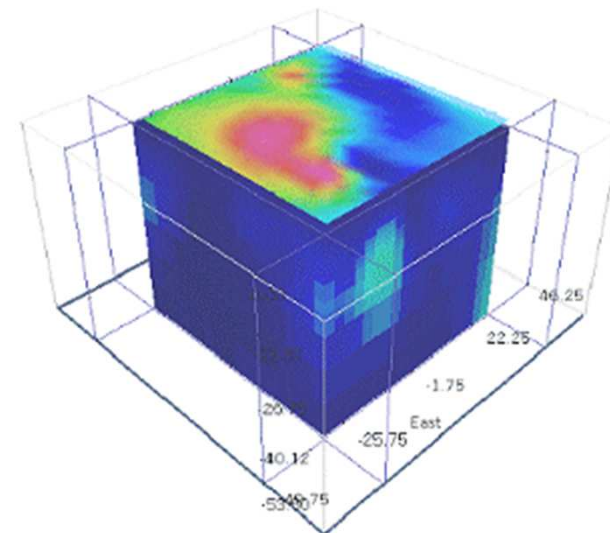


# Earth can be complicated

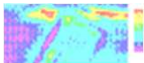
A complicated earth model



Magnetic data for a complicated earth model.

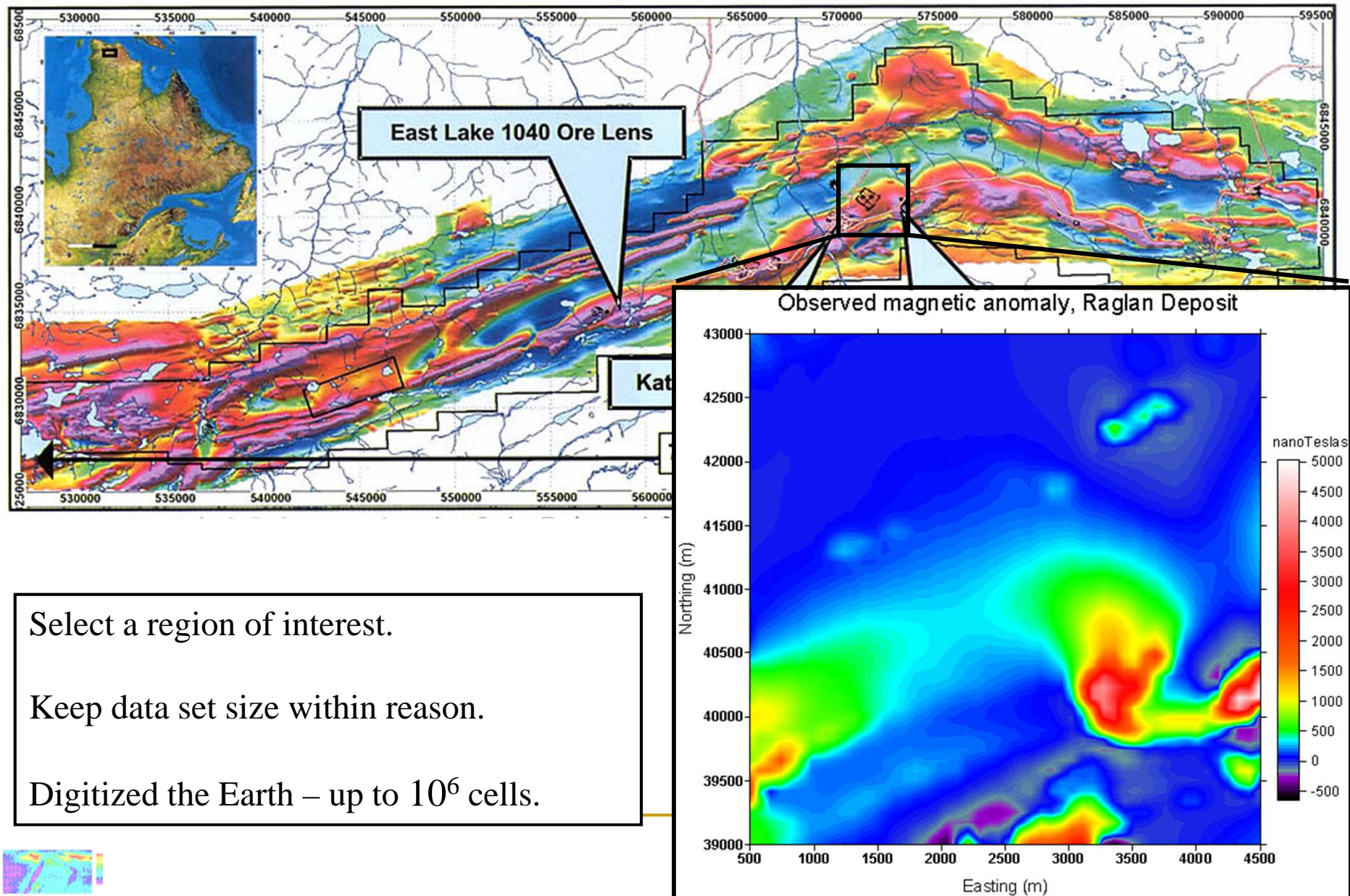


To interpret field data from a complicated earth we need to have formal inversion procedures that recognize non-uniqueness.



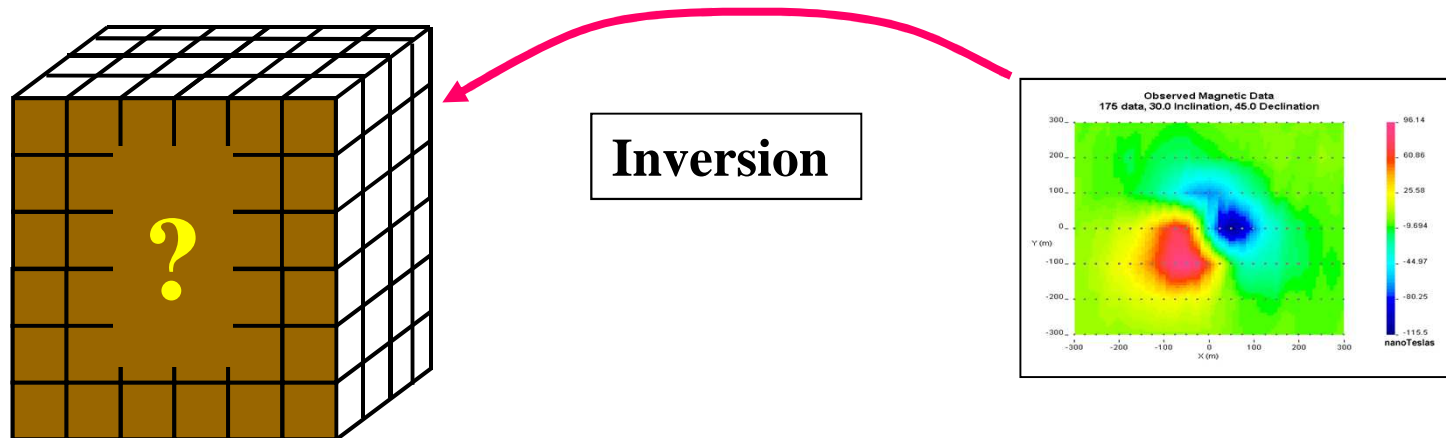


# Example: Raglan aeromagnetic data

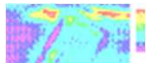


## Inversion:

Finding an earth model that generated the data



**Divide the earth into many cells of constant but unknown susceptibility**  
**Solve the large inverse problem to estimate the value of each cell**



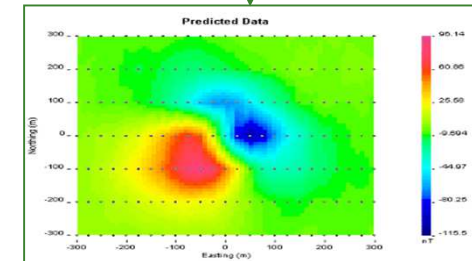
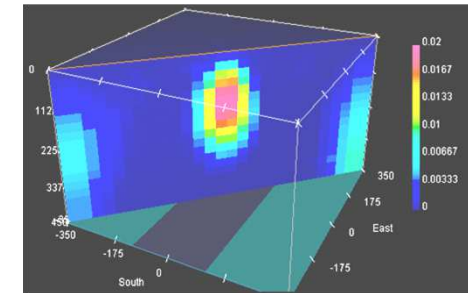
# Misfit: comparing predictions to measurements

Once a model is estimated ...

- Calculate data caused by that model.

- Compare predictions to these measurements.

- Is comparison within errors?



YES

Compare

NO

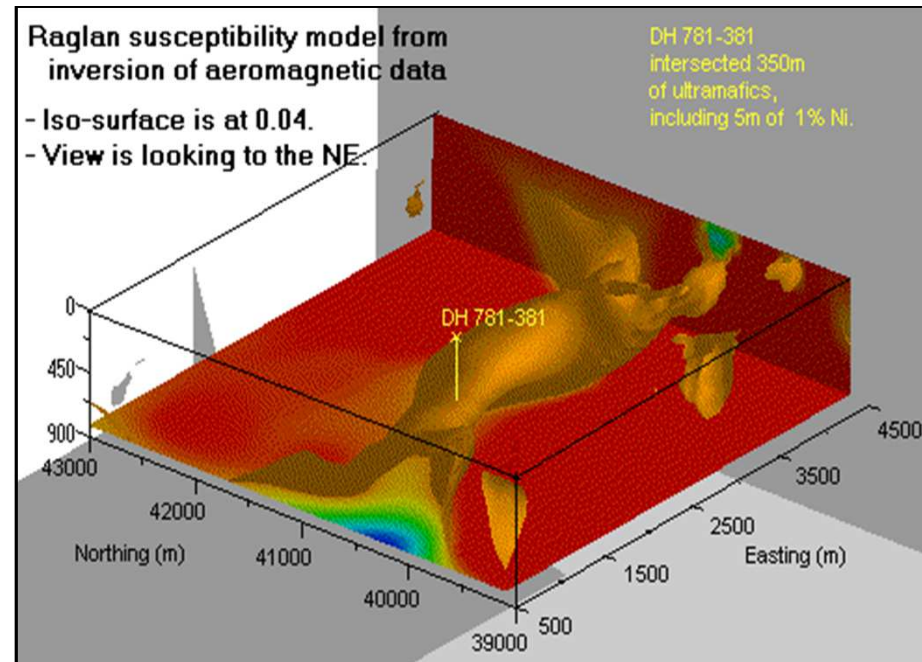
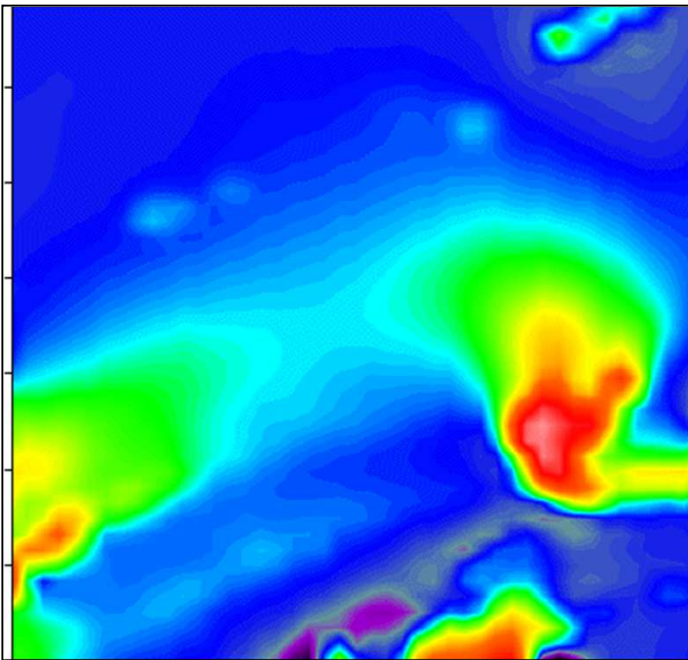
Modify model and try again

Proceed to check for acceptability



# Raglan aeromagnetic data

- Estimate a model for the distribution of subsurface magnetic material.
- Model will be “smooth”, and close to pre-defined reference.
- Display result as cross sections and as isosurfaces.



- Are “sills” connected at depth? Inversion result supports this idea.
- It helped justify a 1050m drill hole.
- 330m of peridotite intersected at 650m 10m were ore grade.
- Image shows all material which has  $k > 0.04$  SI.





# Summary: Magnetism – interpretation

1. Qualitative:
  - Correlate magnetic patterns to geology
2. Quantitative interpretation
  - Determine shapes, volumes, contacts, materials
3. Direct interpretation of patterns
4. Forward modelling
  1. “Guess” geology
  2. Calculate result - Compare to data
  3. Iterate.
5. **Inversion:** Given data, estimate possible configurations of susceptible material that could cause those data.

