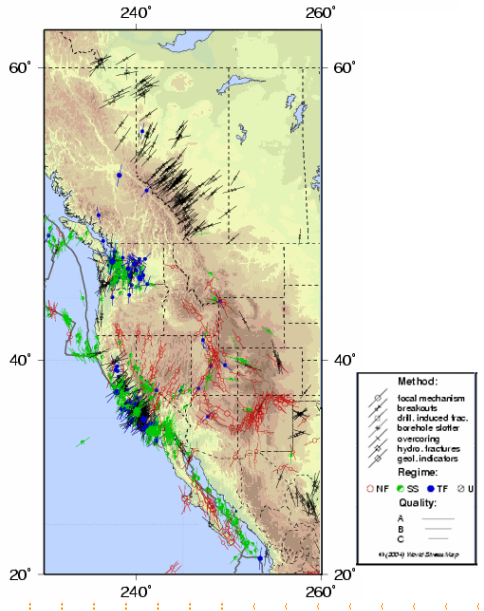
EOSC433:

Geotechnical Engineering Practice & Design

Lecture 7:

***In Situ* Stresses & Stress Measurement**



Why Study Stress?

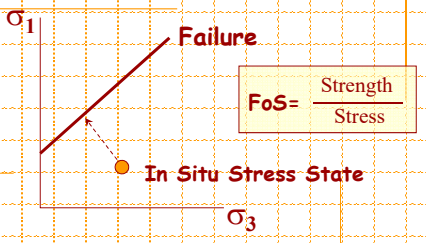
Stress is a concept which is fundamental to rock mechanics principles and applications. There are three basic reasons to understand stress in the context of engineering rock mechanics:

- There is a pre-existing stress state in the ground and we need to understand it, both directly and as the stress state applies to analysis and design.
- During rock excavation, the stress state can change dramatically. This is because rock, which previously contained stresses, has been removed and the loads must be redistributed.
- Stress is not familiar: it is a tensor quantity and tensors are not encountered in everyday life.

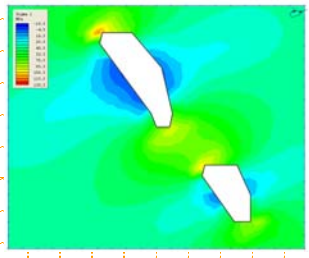
Why Determine *In Situ* Stress?

The basic motivations for *in situ* stress determination are two-fold:

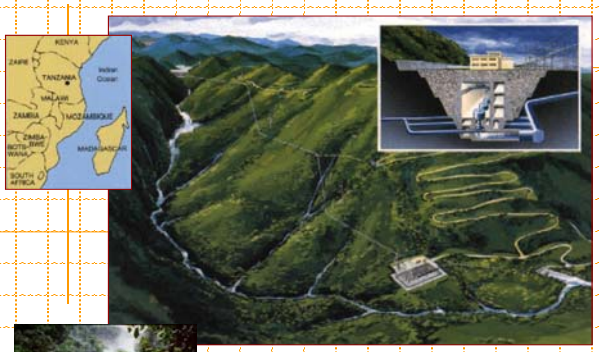
- Engineering analyses require boundary conditions. One of the most important boundary conditions for the analysis of underground excavations is *in-situ* stress.

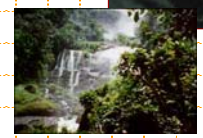


- To have a basic knowledge of the stress state (e.g. the direction and magnitude of the major principal stress; the direction in which the rock is most likely to fail; etc.).



Lower Kihansi Hydropower Project, Tanzania

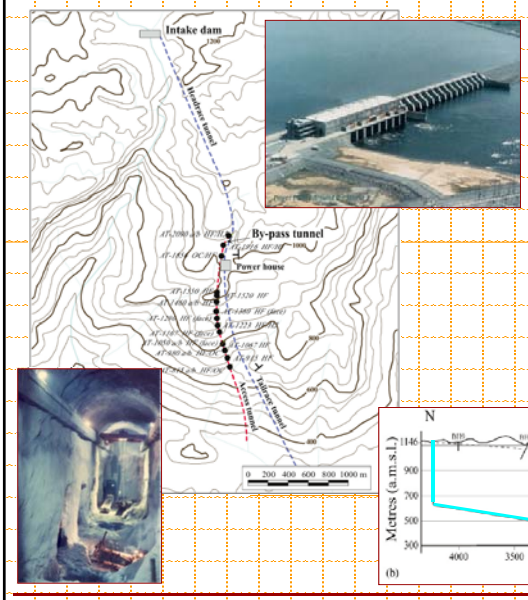




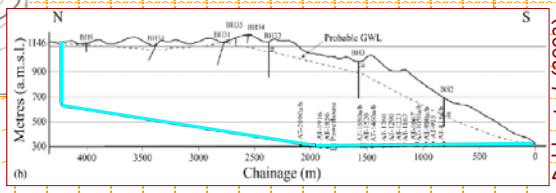
The Lower Kihansi hydroelectric project seeks to utilise the waters of the Kihansi river by channelling part of the river flow upstream of the Kihansi Falls into an inclined high pressure headrace tunnel. The headrace tunnel was planned to be largely unlined.

Unlined tunnels cost 3 to 5 times less than lined tunnels; in this case a cost savings on the order of $10-15 million.

Lower Kihansi Hydropower Project, Tanzania



To permit this, the minimum principal stress along the tunnel trajectory under operational conditions would have to be at least equal to the water head times a 1.2 safety factor.



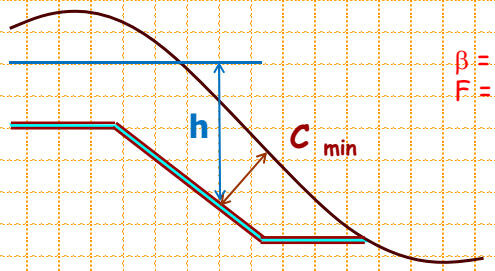
Dahlø et al. (2003)

"Norwegian Rule" to Find Minimum Cover

Unlined pressure tunnels
"Norwegian Rule" to find minimum cover

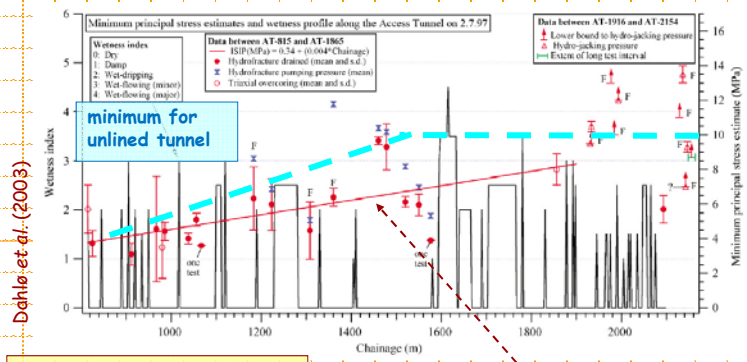
$$C_{min} = \frac{h\gamma_w F}{\gamma \cos\beta}$$

β = slope angle
F = Safety Factor



Broch (1982)

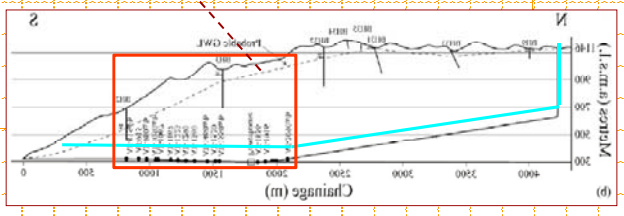
Case History: Lower Kihansi Hydropower Project



Dahlø et al. (2003)

Pressure tunnel

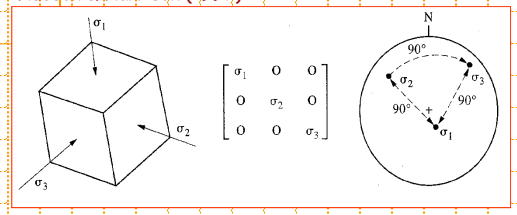
Minimum principal stress estimates indicated levels of at least 9.5MPa (thus meeting the 10 MPa threshold required for an unlined tunnel).



Presentation of In Situ Stress Data

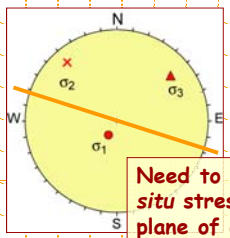
The stress state at a point in a rock mass is generally presented in terms of the magnitude and orientation of the principal stresses (remember that the stress state is completely described by six parameters).

Hudson & Harrison (1997)



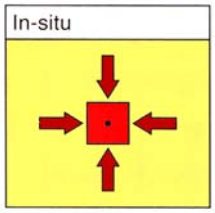
… principal stresses acting on a cube (left), expressed in matrix form (centre), and shown on a hemispherical projection in terms of their orientation.

Stress	(MPa)	Trend (°)	Plunge (°)
Sigma 1	10	210	70
Sigma 2	8	320	10
Sigma 3	5	50	15



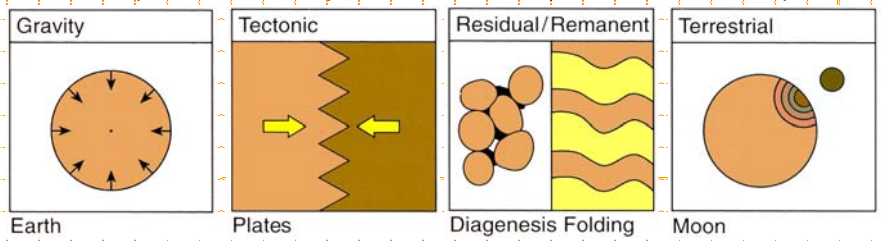
Need to know the *in-situ* stress in the plane of a tunnel for plane strain analysis.

Components of Rock Stress



Continuum

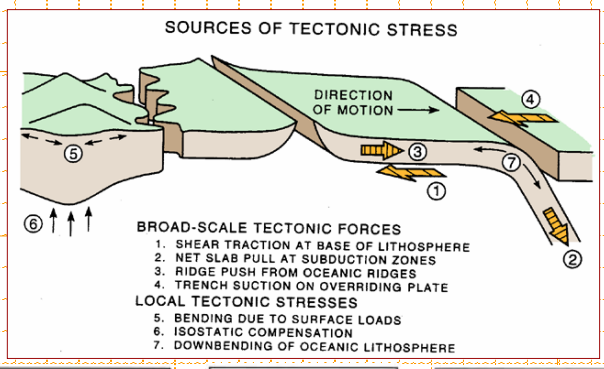
When considering the loading conditions imposed on the rock mass, it must be recognized that an *in situ* pre-existing state of stress already exists in the rock.



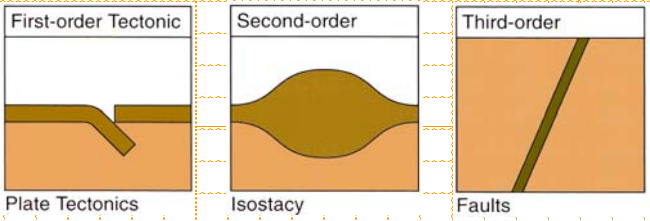
Zang & Stephansson (2010)

In Situ Stress & Tectonics

When considering the loading conditions imposed on the rock mass, it must be recognized that an *in situ* pre-existing state of stress already exists in the rock.

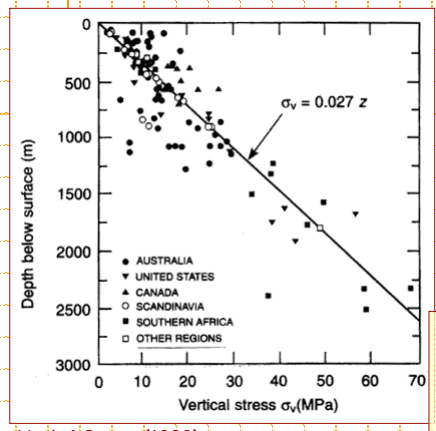


Zoback *et al.* (1989)



Estimation of *In Situ* Stresses - Vertical

As a first approximation, the principal *in situ* stresses can be assumed to act vertically (one component) and horizontally (two components).



Hoek & Brown (1980)

The vertical stress component is assumed to increase with depth due to the weight of the overburden:

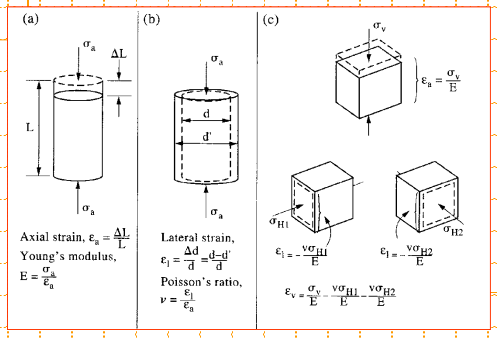
$$\sigma_v = \gamma z$$

Where z is the depth, measured in metres below ground surface and γ is the unit weight, measured in MN/m^3.

As a rule of thumb, taking the average density of rock into account, 40 m of overlying rock induces 1 MPa stress.

Estimation of *In Situ* Stresses - Horizontal

The horizontal stress can be estimated using of elastic theory. If we consider the strain along any axis of a small cube at depth, then the total strain can be found from the strain due to the axial stress, subtracting the strain components due to the two perpendicular stresses.



Hudson & Harrison (1997)

For example:

$$\varepsilon_V = \frac{\sigma_V}{E} - \frac{\nu\sigma_{H1}}{E} - \frac{\nu\sigma_{H2}}{E}$$

$$\varepsilon_{H1} = \frac{\sigma_{H1}}{E} - \frac{\nu\sigma_{H2}}{E} - \frac{\nu\sigma_V}{E}$$

Estimation of *In Situ* Stresses - Horizontal

To provide an initial estimate of the horizontal stress, two assumptions are made:

- the two horizontal stresses are equal;
- there is no horizontal strain, i.e. both ε_{H1} and ε_{H2} are zero (e.g. because it is restrained by adjacent elements of rock).

Then we can take ε_{H1} as zero:

$$0 = \frac{\sigma_{H1}}{E} - \frac{\nu\sigma_{H2}}{E} - \frac{\nu\sigma_V}{E}$$

And, because $\sigma_{H1} = \sigma_{H2}$:

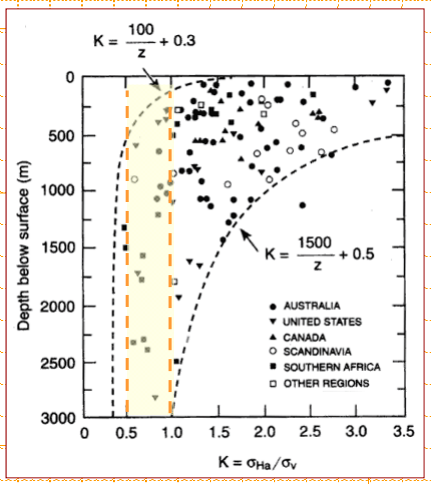
$$\sigma_H = \frac{\nu}{1-\nu}\sigma_V$$

Estimation of *In Situ* Stresses - Horizontal

Thus the ratio between the horizontal and vertical stress (referred to as $K = \sigma_H/\sigma_V$) is a function of the Poisson's ratio:

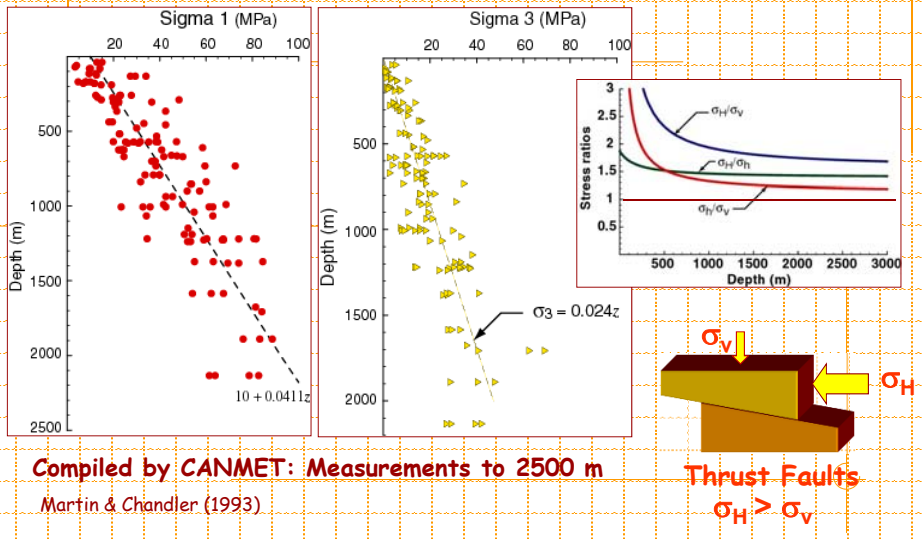
$$\frac{\sigma_H}{\sigma_V} = \frac{\nu}{1-\nu}$$

For a typical Poisson's ratio (ν) of 0.25, the resulting K ratio is 0.33. For a theoretical maximum of ν = 0.5, the maximum K ratio predicted is 1.0.



Hoek & Brown (1980)

In Situ Stresses – Canadian Database

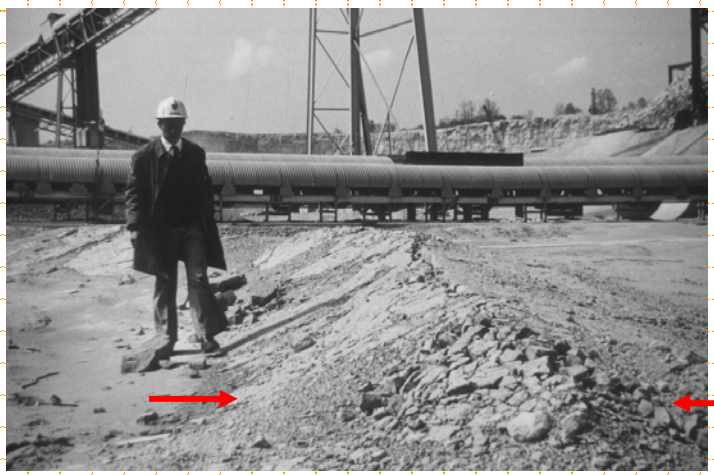


Compiled by CANMET: Measurements to 2500 m

Martin & Chandler (1993)

Evidence of high ground stress: Quarry pop-up

(Dufferin Quarry, Guelph, Lockport Dolomite, Niagara Escarpment)



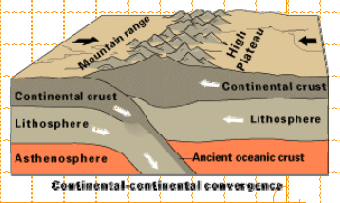
15 MPa (weight of 500m of rock)

Reasons for High Horizontal Stresses

High horizontal stresses are caused by factors relating to erosion, tectonics, rock anisotropy, local effects near discontinuities, and scale effects:

Erosion – if horizontal stresses become 'locked in', then the erosion/removal of overburden (i.e. decrease in σ_V) will result in an increase in *K* ratio (σ_H/σ_V).

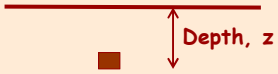
Tectonics – different forms of tectonic activity (e.g. subduction zones), can produce high horizontal stresses.



High Horizontal Stresses: A Thought Experiment

Original stress in a rock element at moderate depth

Vertical: 25z (kPa)
Horizontal: 0.33*25z → $\frac{\sigma_H}{\sigma_V} = \frac{\nu}{1-\nu}$

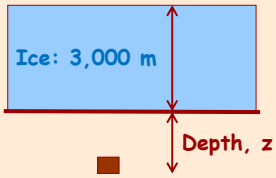


Immediately after glaciation

Vertical: (30,000 + 25z) kPa
Horizontal: 0.33*(30,000+25z) kPa

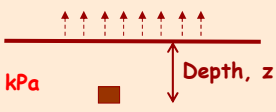
After a long time, k >>> 1.0 (plastic flow)

Vertical: 30,000 + 25z
Horizontal: 30,000 + 25z



"Sudden" deglaciation (elastic unloading)

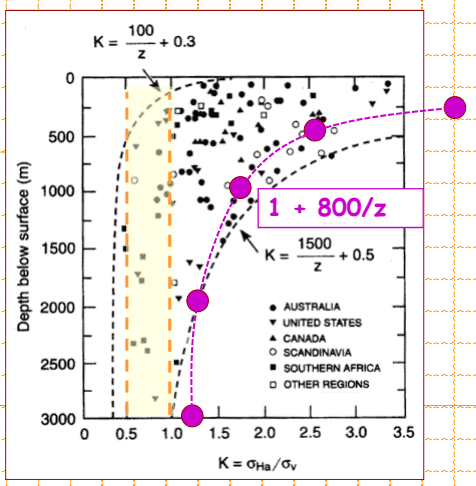
Vertical: 25z (kPa)
Horizontal: (30,000 + 25z) – (0.33 * 30,000) kPa



Final K-ratio: $\frac{\sigma_H}{\sigma_V}$ = 1 + 800/z = 9 @ 100 m depth, 3 @ 400 m depth

Estimation of *In Situ* Stresses - Horizontal

Final K-ratio: $\frac{\sigma_H}{\sigma_v} = (20{,}000 + 25z)/25z = 1 + 800/z$



Methods of Stress Determination

1. **Flatjack**

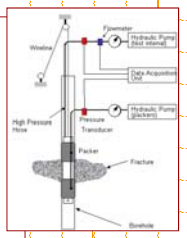
$$\begin{bmatrix} \sigma_{xx} & \tau_{xy} & \tau_{xz} \\ & \sigma_{yy} & \tau_{yz} \\ \text{Symm.} & & \sigma_{zz} \end{bmatrix}$$

One normal stress component determined, say parallel to *x*-axis.

2. **Hydraulic fracturing**

$$\begin{bmatrix} \sigma_1 & 0 & 0 \\ & \sigma_2 & 0 \\ \text{Symm.} & & \sigma_3 \end{bmatrix}$$

Principal stresses assumed parallel to axes i.e. plane of the fracture, two determined, say σ_1 and σ_3, one estimated, say σ_2.



3. **USBM overcoring torpedo**

$$\begin{bmatrix} \sigma_{xx} & \tau_{xy} & \tau_{xz} \\ & \sigma_{yy} & \tau_{yz} \\ \text{Symm.} & & \sigma_{zz} \end{bmatrix}$$

Three components in 2-D determined from three measurements of borehole diameter change.

4. **CSIRO overcoring gauge**

$$\begin{bmatrix} \sigma_{xx} & \tau_{xy} & \tau_{xz} \\ & \sigma_{yy} & \tau_{yz} \\ \text{Symm.} & & \sigma_{zz} \end{bmatrix}$$

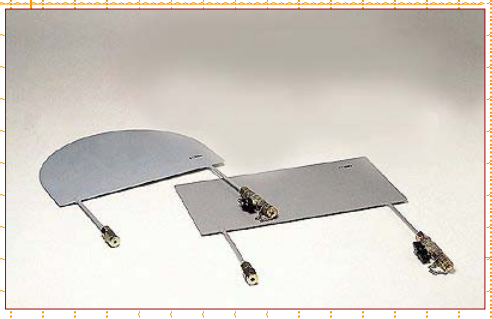
All six components determined from six (or more) measurements of strain at one time.

Hudson & Harrison (1997)

... the four ISRM suggested methods for rock stress determination and their ability to determine the 6 independent components of the stress tensor over one test/application of the particular method.

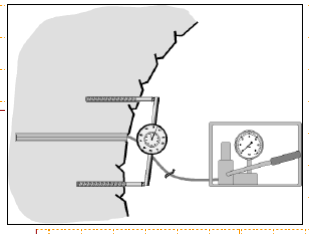
Flatjack Method

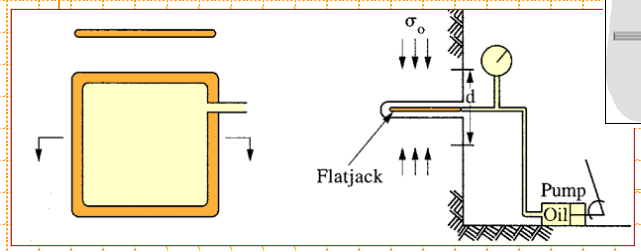
A flatjack is comprised of two metal sheets placed together and welded around their periphery. A feeder tube inserted in the middle allows the flatjack to be pressurized with oil or water.



Flatjack Method

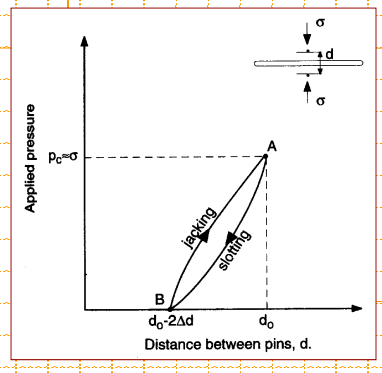
The flatjack method involves the placement of two pins fixed into the wall of an excavation. The distance, *d*, is then measured accurately. A slot is cut into the rock between the pins. If the normal stress is compressive, the pins will move together as the slot is cut. The flatjack is then placed and grouted into the slot.

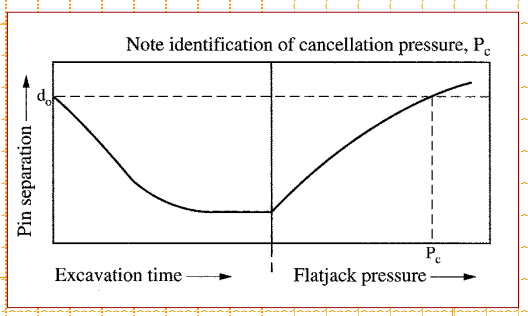




Flatjack Method

On pressurizing the flatjack, the pins will move apart. It is assumed that, when the pin separation distance reaches the value it had before the slot was cut, the force exerted by the flatjack on the walls of the slot is the same as that exerted by the pre-existing normal stress.

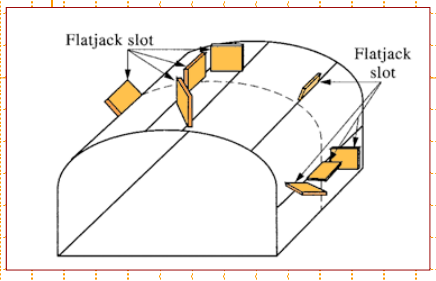




Hudson & Harrison (1997)

Flatjack Method

The major disadvantage with the system is that the necessary minimum number of 6 tests, at different orientations, have to be conducted at 6 different locations and it is therefore necessary to distribute these around the boundary walls of an excavation.



1. **Flatjack**

$$\begin{bmatrix} \sigma_{xx} & \tau_{xy} & \tau_{xz} \\ & \sigma_{yy} & \tau_{yz} \\ \text{Symm.} & & \sigma_{zz} \end{bmatrix}$$

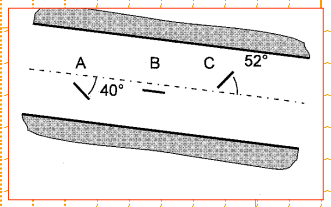
One normal stress component determined, say parallel to x-axis.

Hudson & Harrison (1997)

It is also important to note that the excavation from which the tests are made will disturb the pre-existing stress state, and so the new redistribution of stresses should be accounted for.

Flatjack Method - Example

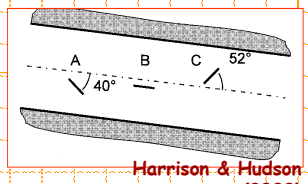
Q. Three flatjack tests have been made along a tunnel wall, the axis of which dips at 7°. The measurement position is approximately 250 m below ground surface. The slots for the flatjacks were cut normal to the wall as shown. The cancellation pressures for each flatjack were: A = 7.56 MPa; B = 6.72 MPa; C = 7.50 MPa. Compute the principal stresses and their directions.



A. One way of solving this problem is to use the stress transformation equations, i.e.:

$$\begin{bmatrix}\sigma_A\\ \sigma_B\\ \sigma_C\end{bmatrix} = \begin{bmatrix}\cos^2\theta_A & \sin^2\theta_A & 2\sin\theta_A\cos\theta_A\\ \cos^2\theta_B & \sin^2\theta_B & 2\sin\theta_B\cos\theta_B\\ \cos^2\theta_C & \sin^2\theta_C & 2\sin\theta_C\cos\theta_C\end{bmatrix}\begin{bmatrix}\sigma_x\\ \sigma_y\\ \tau_{xy}\end{bmatrix} \quad \text{or } \boldsymbol{\sigma}_{\text{jack}} = \mathbf{R}\boldsymbol{\sigma}_{\text{global}}$$

Flatjack Method - Worked Example



Harrison & Hudson (2000)

1. Taking the x-axis horizontal directed to the right, and the y-axis vertical upwards, and all measurements measured anticlockwise positive from the positive x-axis, we have the following dip angles:

$$\beta_{\text{tunnel}} = -7^\circ; \quad \beta_A = -40^\circ + \beta_{\text{tunnel}} = -47^\circ;$$
$$\beta_B = 0^\circ + \beta_{\text{tunnel}} = -7^\circ; \quad \beta_C = 52^\circ + \beta_{\text{tunnel}} = 45^\circ.$$

2. Because each flatjack measures the normal stress component perpendicular to it, we add 90° to each of these directions to obtain the direction of the normal stress on each flatjack:

Jack A $\sigma_A = 7.56$ MPa; $\theta_A = \beta_A + 90^\circ$; $\theta_A = 43^\circ$
Jack B $\sigma_B = 6.72$ MPa; $\theta_B = \beta_B + 90^\circ$; $\theta_B = 83^\circ$
Jack C $\sigma_C = 7.50$ MPa; $\theta_C = \beta_C + 90^\circ$; $\theta_C = 135^\circ$

3. Assembling the stress transformation equation for all three flatjacks into matrix form gives:

$$\begin{bmatrix}\sigma_A\\ \sigma_B\\ \sigma_C\end{bmatrix} = \begin{bmatrix}\cos^2\theta_A & \sin^2\theta_A & 2\sin\theta_A\cos\theta_A\\ \cos^2\theta_B & \sin^2\theta_B & 2\sin\theta_B\cos\theta_B\\ \cos^2\theta_C & \sin^2\theta_C & 2\sin\theta_C\cos\theta_C\end{bmatrix}\begin{bmatrix}\sigma_x\\ \sigma_y\\ \tau_{xy}\end{bmatrix} \quad \text{or } \boldsymbol{\sigma}_{\text{jack}} = \mathbf{R}\boldsymbol{\sigma}_{\text{global}}$$

Flatjack Method – Worked Example

④ Evaluation of this matrix gives:

$$\begin{bmatrix} 7.56 \\ 6.72 \\ 7.50 \end{bmatrix} = \begin{bmatrix} 0.535 & 0.465 & 0.998 \\ 0.015 & 0.985 & 0.242 \\ 0.500 & 0.500 & -1.000 \end{bmatrix} \begin{bmatrix} \sigma_x \\ \sigma_y \\ \tau_{xy} \end{bmatrix}$$

Which upon inversion gives $\sigma_{global} = R^{-1}\sigma_{jack}$, or:

$$\begin{bmatrix} \sigma_x \\ \sigma_y \\ \tau_{xy} \end{bmatrix} = \begin{bmatrix} 1.093 & -0.952 & 0.860 \\ -0.134 & 1.021 & 0.113 \\ 0.479 & 0.034 & -0.514 \end{bmatrix} \begin{bmatrix} 7.56 \\ 6.72 \\ 7.50 \end{bmatrix}$$

⑤ From this we find:

$$\begin{bmatrix} \sigma_x \\ \sigma_y \\ \tau_{xy} \end{bmatrix} = \begin{bmatrix} 8.31 \\ 6.70 \\ 0.00 \end{bmatrix} \text{ MPa.}$$

We see that σ_x and σ_y are principal stresses, because $\tau_{xy} = 0$, and the principal stresses are vertical and horizontal, which is a reasonable finding.

Note that the horizontal stress, σ_x, is greater than the vertical stress, σ_y, which is a common occurrence. Now if we were to compare the weight of the overburden to the computed vertical stress value:

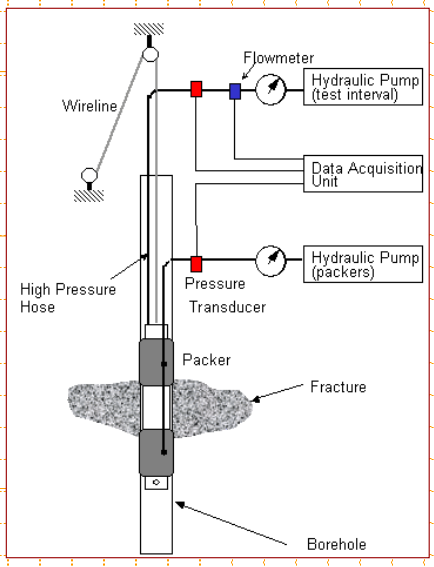
$$\gamma_{rock} = 27 \text{ kN/m}^3; \quad z = 250 \text{ m}; \quad \sigma_v = \gamma_{rock} \times z; \quad \sigma_v = 6.75 \text{ MPa.}$$

This compares well with the value found for σ_y.

Harrison & Hudson (2000)

Hydraulic Fracturing Method

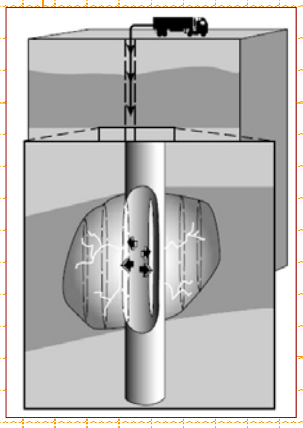
The hydraulic fracturing method involves the pressuring of a borehole interval, typically 1 m long, isolated using a straddle packer system. The isolated zone is pressurized by the hydrofrac fluid until a fracture occurs in the rock.

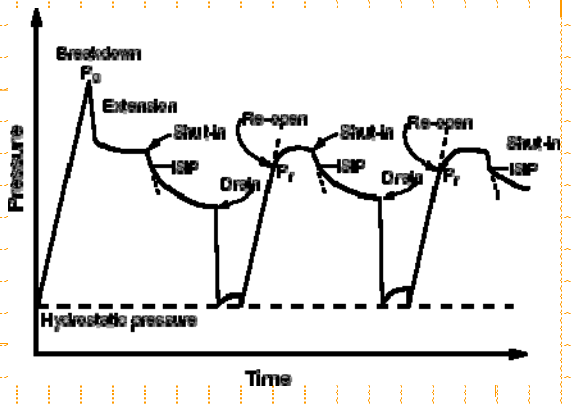


Haimson & Lee (1984)

Hydraulic Fracturing Method

The two measurements taken are the water pressure when the fracture occurs (breakdown pressure, P_c'), and the subsequent pressure required to hold the fracture open (shut-in pressure, P_s).

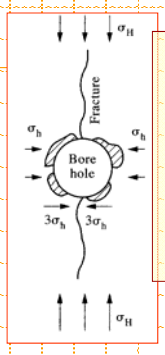




Hydraulic Fracturing Method

In calculating the *in* situ stresses, the shut-in pressure (P_s) is assumed to be equal to the minor horizontal stress, σ_h.

The major horizontal stress, σ_H, is then found from the breakdown pressure (P_c' or P_B). In this calculation, the breakdown pressure has to overcome the minor horizontal principal stress (concentrated three times by the presence of the borehole) and overcome the *in situ* tensile strength of the rock; it is assisted by the tensile component of the major horizontal principal stress.



Relationships

$\sigma_h = P_s$

$\sigma_H = 3\sigma_h - P_c' - P_o + \sigma_t$

$\sigma_t = P_c' - P_r$

$\sigma_H = 3\sigma_h - P_r - P_o$

2. **Hydraulic fracturing**

σ_1	0	0	Principal stresses assumed parallel to axes i.e. plane of the fracture, two determined, say σ_1 and σ_3, one estimated, say σ_2.
	σ_2	0	
Symm.		σ_3	

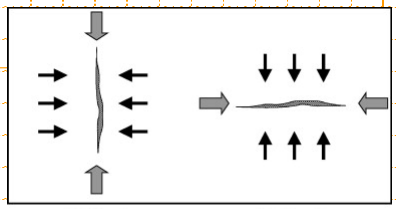
Hudson & Harrison (1997)

Hydraulic Fracturing Method

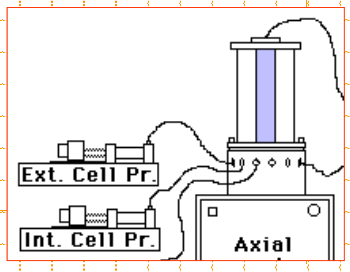
The analysis assumes that the induced fracture has propagated in a direction perpendicular to the minor principal stress.

Other assumptions include that the rock behaves elasticity (from which the borehole stress concentration factor of three is derived), and is impermeable (i.e., the pumped water has not significantly penetrated the rock and affected the stress distribution).

The tensile strength of the rock can be obtained from test performed by pressurizing hollow rock cylinders.



(a) $K_0 < 1$ Vertical fracture (b) $K_0 > 1$ Horizontal fracture

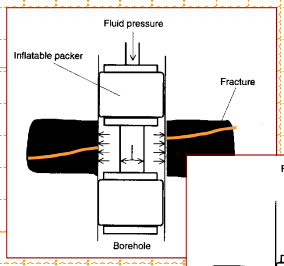


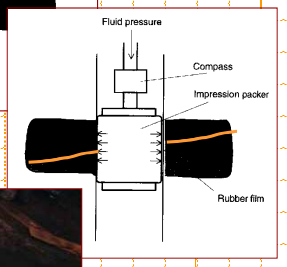
Hydraulic Fracturing Method

There are also several problems inherent in the use of this method. For example, it can often be difficult, if not impossible, to identify a 1 m length of borehole which is fracture free.

Furthermore, there can be difficulties measuring water pressures accurately, and in correctly identifying the breakdown and shut-in pressures.

Lastly, it is often an oversimplifying assumption that the borehole is parallel to a principal stress.





Hydraulic Fracturing Method – Worked Example

Q. A hydraulic fracture test in a granite rock mass yield the following results:

Depth (m)	Breakdown pressure, P_B (MPa)	Shut-in pressure, P_S (MPa)
500	14.0	8.0

Given that the tensile strength of the rock is 10 MPa, estimate the principal stresses assuming one is vertical and that the pressure values were adjusted to account for the formation pressures (i.e. P_o=0 for calculation purposes).

A. Assuming that the rock mass was behaving as an elastic material...

Relationships

$\sigma_h = P_s$

$\sigma_H = 3\sigma_h - P_c' - P_o + \sigma_t$

1. Calculate the min. horizontal stress: $\sigma_h = P_s = 8$ MPa
2. Calculate the max. horizontal stress: $\sigma_H = 3\sigma_h - P_c' - P_o + \sigma_t$

$\sigma_H = 3(8\text{ MPa}) - 14\text{ MPa} + 10\text{ MPa} \Rightarrow \sigma_H = 20$ MPa

3. The vertical stress can now be estimated from the overburden (assume γ = 27 kN/m^3 for granite): $\sigma_v = 500\text{m} * 0.0027\text{ MN/m}^3 = 13.5$ MPa

$\sigma_1 = \sigma_H = 20$ MPa $\sigma_2 = \sigma_v = 13.5$ MPa $\sigma_3 = \sigma_h = 8$ MPa

Borehole Relief Methods – Overcoring

The main idea behind relief methods is to isolate (partially or wholly) a rock sample from the stress field that surrounds it and to monitor the response. As such, the stresses are not related to applied pressures, such as with the hydraulic tests. Instead, the stresses are inferred from strains generated by the relief (unloading) process and measured directly on the rock associated with the relief process.

Overcoring methods are by far the most commonly used relief method.

Surface relief methods	• Isolate a block of rock from surrounding rock mass and monitor its surface strain or deformation response: • Monitor hole deformation due to drilling of parallel hole • Center hole drilling or undercoring
Borehole relief methods	• Overcoring of prestressed cells • Overcoring of deformation-type gages such as the USBM gage • Overcoring of a gage attached to the flat end of a borehole: Doorstopper and photoelastic disks • Overcoring of CSIR-type triaxial strain cells • Overcoring of triaxial strain cells attached to the end of a borehole (spherical and conical cells) • Overcoring of stiff, solid or hollow inclusion-type gages • Borehole jack fracturing, or slotting, or deepening • Holographic methods • Undercoring of borehole wall • Borehole tapercoring
Rock mass relief methods	• Bored raise method • Back-analysis • Under-excavation technique

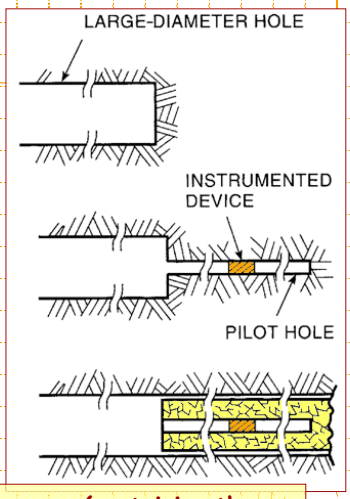
Amadei & Stephansson (1997)

Overcoring Method

First, a large diameter borehole is drilled (between 60 and 220 mm) to a sufficiently large distance so that stress effects due to any excavations can be neglected.

Second, a small pilot hole (e.g. 38 mm) is drilled. The measuring device is then inserted and fastened in this hole.

Thirdly, the large diameter hole is resumed, relieving stresses and strains in the hollow rock cylinder that is formed. Changes in strain are then recorded with the instrumented device as the overcoring proceeds past the plane of measurement.

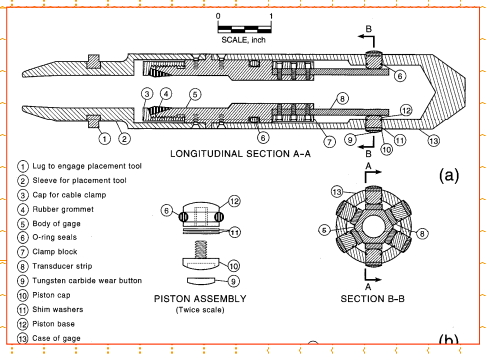


Following overcoring, the recovered overcore (containing the instrumented device) is then tested in a biaxial chamber to determine the elastic properties of the rock.

Overcoring Method – USBM Deformation Probe

The USBM (U.S. Bureau of Mines) probe allows the complete stress state to be determined from three measurements in boreholes with different orientations when the stresses are released by overcoring.

When the probe is inserted in a borehole, six 'buttons' press against the borehole wall and their diametral position is measured by strain gauges bonded to steel cantilevers supporting the buttons.

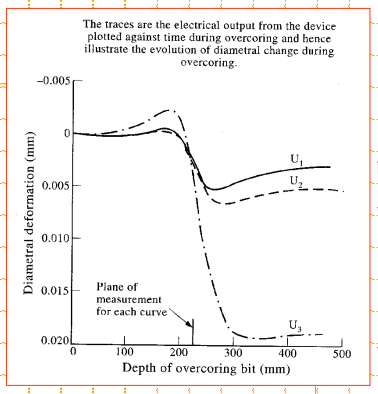


Amadei & Stephansson (1997)

Overcoring Method – USBM

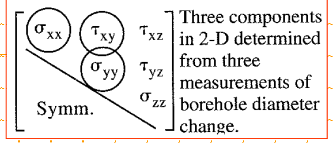
When the borehole is overcored by a larger diameter borehole, the stress state in the resulting hollow cylinder is reduced to zero, the diameter of the hole changes, the buttons move, and hence different strains are induced in the strain gauges.

From these changes, and with the use of elasticity theory, the biaxial stress state in the plane perpendicular to the borehole axis is deduced.



Hudson & Harrison (1997)

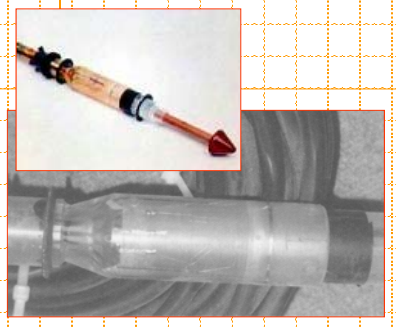
3. USBM overcoring torpedo



Three components in 2-D determined from three measurements of borehole diameter change.

Overcoring Method – CSIRO Hollow Inclusion Cell

The CSIRO device operates as a probe embedded with several strain gauges, which is glued into the borehole and can measure normal strains at a variety of orientations and locations around the borehole wall.

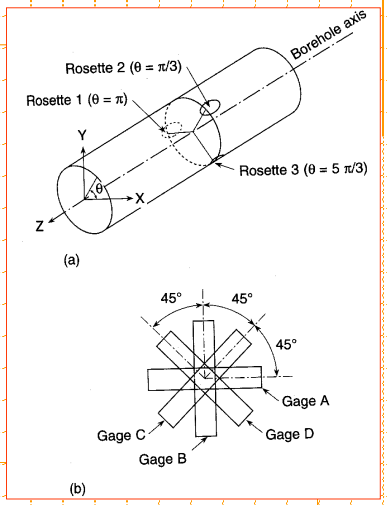


The gauge is glued into position within the pilot hole, initial readings of strain are taken and the gauge is then overcored.

Overcoring Method – CSIRO Hollow Inclusion Cell

Overcoring destresses the resulting hollow cylinder and final strain gauge readings are taken. The gauge has either 9 or 12 separate strain gauges, in rosettes of three, so there is some redundancy in the measurements- thus permitting statistical analysis of the data.

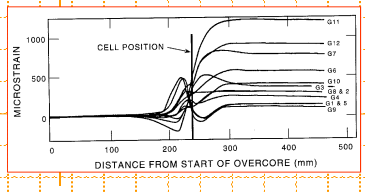
Alternatively, if the rock is assumed to be anisotropic (e.g. transverse isotropic), then the extra readings allow the stress state to be calculated incorporating the rock anisotropy.



Amadei & Stephansson (1997)

Overcoring Method – CSIRO Hollow Inclusion Cell

The CSIRO measurement cell is one of the few tests that can establish the full stress tensor with one installation.



4. **CSIRO overcoring gauge**

σ_{xx} τ_{xy} τ_{xz}
σ_{yy} τ_{yz}
Symm. σ_{zz}

All six components determined from six (or more) measurements of strain at one time.

Another advantage of the method is that the hollow rock cylinder can be retrieved and tested under controlled conditions in order to determine the elastic constants and the functionality of the system (e.g. whether strain gauges are properly bonded, whether the test was performed in intact rock, etc.).

One major problem is the environment within the borehole: water or loose material on the borehole walls may hamper bonding of the cell; and drilling fluids may generate temperature effects.

Stress Determination Methods - Summary

Eberhardt & Stead (2011)

Method	Advantages	Limitations	Suitability
Overcoring	Most developed technique in both theory and practice; 3-D.	Scatter in data due to small rock volume; requires drill rig.	Measurement depths down to 1000m.
Doorstopper	Works in jointed and high stressed rocks.	Only 2-D; requires drill rig.	For weak or high stressed rocks.
Undercoring	Simple measurements; low cost; can utilize existing underground excavation.	Measures local stresses (must be related to far-field stresses); rock may be disturbed.	During excavation.
Hydraulic fracturing	Can utilize existing boreholes; tests large rock volume; low scatter in results; quick.	Only 2-D; theoretical limitations in the evaluation of s_H.	Shallow to deep measurements.
HTPF	Can utilize existing boreholes; 3-D; can be applied when high stresses exist and overcoring and hydraulic fracturing fail.	Time-consuming; requires existing fractures in the hole with varying strikes and dips.	Where both overcoring and hydraulic fracturing fail.

Stress Determination Methods - Summary (cont.)

Eberhardt & Stead (2011)

Method	Advantages	Limitations	Suitability
ASR/DSCA/ RACOS	Usable for great depths.	Complicated measurements on the micro-scale; sensitive to several factors	Estimation of stress state at great depth.
Acoustic emissions (Kaiser effect)	Simple measurements.	Relatively low reliability; requires further research.	Rough estimations.
Focal mechanisms	For great depths; existing information from earthquake occurrence.	Information only from great depths.	Seismically active areas.
Core discing	Information, obtained from borehole drilling.	Only qualitative estimation.	Stress estimation at early stage.
Borehole breakouts	Existing information obtained at an early stage; relatively quick.	Orientation information only; theory needs to be further developed to infer stress magnitudes.	Deep boreholes or around deep excavations.
Back analysis	High certainty due to large rock volume.	Theoretically, not unique solution.	During excavation.
Geological indicators	Low cost; 2-D/3-D.	Very rough estimation; low reliability.	At early stage of project.

Methods of Stress Determination

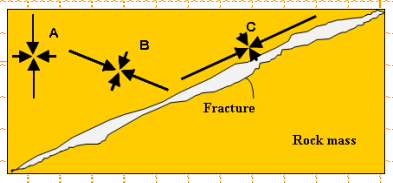
Stress measurement methods vary both in how they measure stress and with respect to the volume of rock tested. A measure of verification, or stress estimates in the absence of measurement data, may also be obtained via 'indirect' or 'indicator' methods.

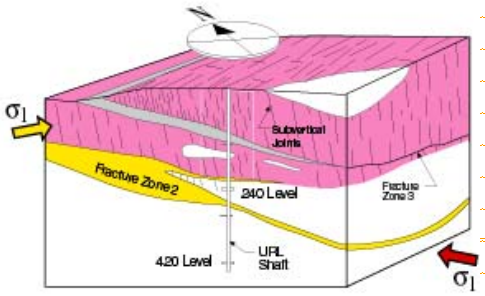
Method		Volume (m^3)
Hydraulic methods	Hydraulic fracturing	0.5–50
	Sleeve fracturing	10^{-2}
	Hydraulic tests on pre-existing fractures (HTPF)	1–10
Relief methods	Surface relief methods	1–2
	Undercoring	10^{-3}
	Borehole relief methods (overcoring, borehole slotting, etc.)	10^{-3}–10^{-2}
	Relief of large rock volumes (bored raise, under-excavation technique, etc.)	10^{2}–10^{3}
Jacking methods	Flat jack method	0.5–2
	Curved jack method	10^{-2}
Strain recovery methods	Anelastic strain recovery (ASR)	10^{-3}
	Differential strain curve analysis (DSCA)	10^{-4}
Borehole breakout method	Caliper and dipmeter analysis	10^{2}–10^{2}
	Borehole televiewer analysis	10^{-2}–10^{2}
Other methods	Fault slip data analysis	10^{8}
	Earthquake focal mechanisms	10^{9}
	Indirect methods (Kaiser effect, etc.)	10^{-4}–10^{-3}
	Inclusions in time-dependent rock	10^{-2}–1
	Measurement of residual stresses	10^{-5}–10^{-3}

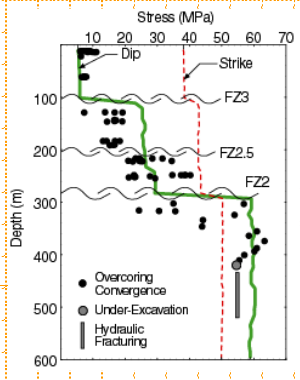
Amadei & Stephansson (1997)

In Situ Stresses & Geological Structure

Discontinuities, e.g. fault zones, act to dramatically perturb the stress field and thus the magnitudes and orientations of the principal stresses. This may lead to bias if the stress measurements are made near an isolated fracture.





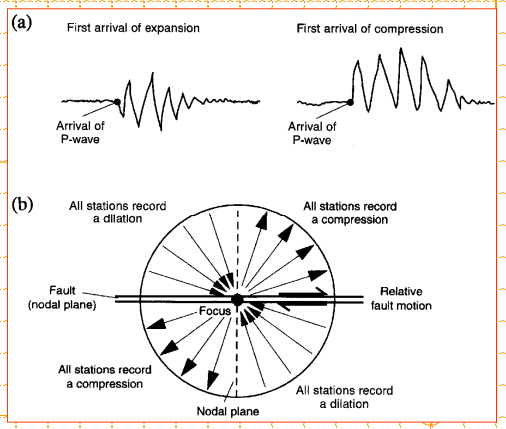


Martin & Chandler (1993)

Indicator Methods of Stress Determination

By careful study of earthquake waves recorded by seismographs, it is possible to tell the direction of motion of the fault that caused the earthquake.

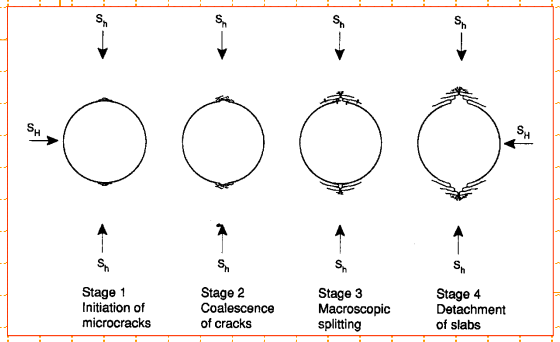
By analyzing the earthquake fault-plane solution (i.e. focal mechanism), a best fit regional stress tensor can be determined by means of an inversion technique.

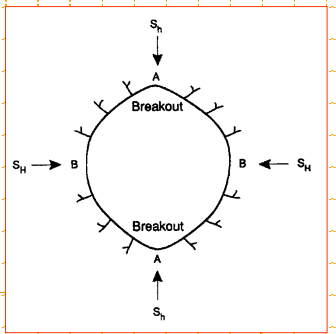


Amadei & Stephansson (1997)

Indicator Methods of Stress Determination

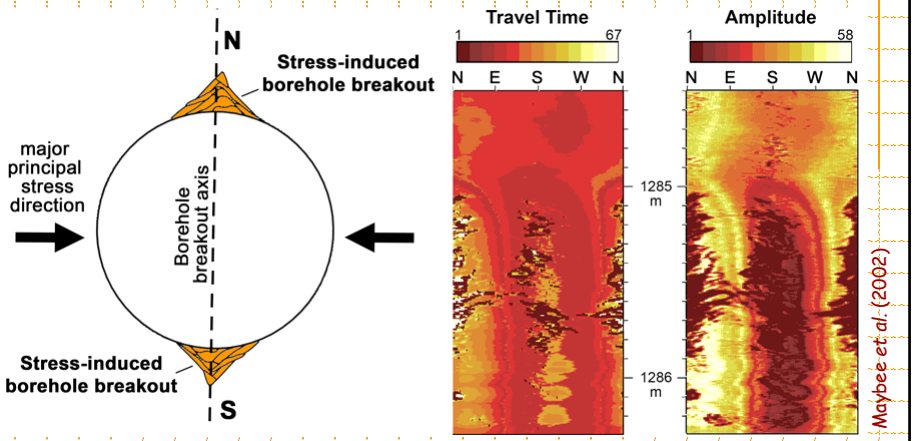
The rock around a circular excavation may not be able to sustain the compressive stress concentration induced during excavation. Failure of the rock results in zones of enlargement called 'breakouts'. There is experimental evidence that breakouts occur in the direction parallel to the minimum *in situ* stress component.





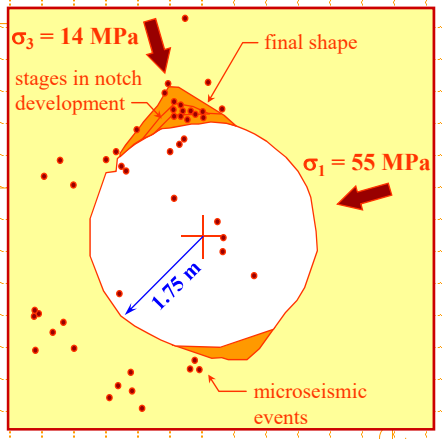
Amadei & Stephansson (1997)

Televiewer Data - Stress Indicators



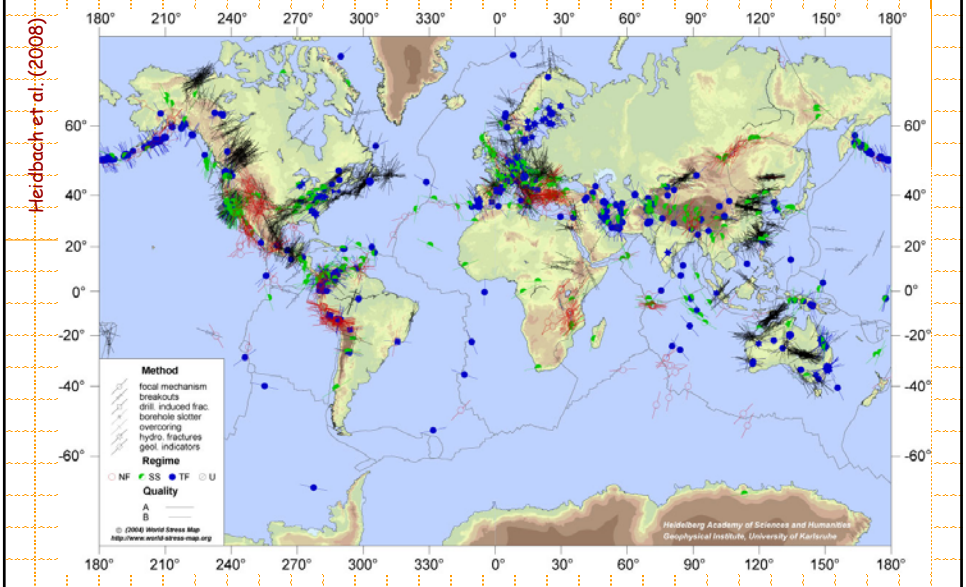
Televiewer log from INCO's Totten mine. The borehole breakout is identifiable as dark vertical bands on opposite sides of the image, indicating that the major principal stress is E-W (i.e., 90° from N-S breakout direction).

Indicator Methods of Stress Determination

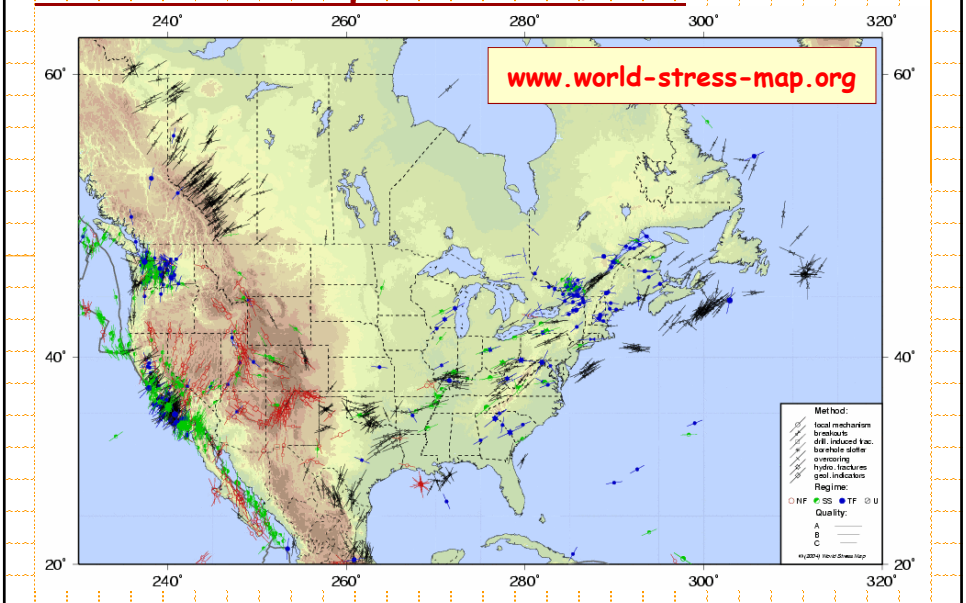


... stress-controlled tunnel breakout at the URL in Canada.

World Stress Map



World Stress Map - North America



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